

1 Fuzzy-TOPSIS Analysis for Standard Alternative Selection: A  
2 Multiple Attribute Decision-Making Method and Application for  
3 Small and Medium Manufacturing Enterprises (SMEs)

4 FuzzyTOPSISAnalysisforStandardAlternativeSelectionAMulti-  
5 pleAttributesDecisionMakingMethodandApplicationforSmallandMediumMa

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10 **Abstract**

11 In the era of industrialization small and medium enterprises (SMEs) play great role in world  
12 economy. The developed as well as developing countries are being benefited from SMEs which  
13 holds a strong position creating new employment and helping in the development and  
14 supporting in local production. The job creation element of SMEs enables many poor people  
15 to feel more secure, assuring that they have a stable job to survive .But the actual situation  
16 and overall working condition of SME?s is very dreadful especially due to limitation of  
17 resources, facilities and techniques. This paper compares different performance criteria on  
18 three different SME and indicates a standard benchmark SME using fuzzy-TOPSIS analysis.  
19 The proposed method states optimum SME working condition among different performance  
20 variables with different values. Qualitative variables with multiple criteria problems have been  
21 analyzed here. As human assessment is uncertain and often subjective for qualitative  
22 characteristics, the alternatives? characteristics are expressed in linguistic terms. These  
23 linguistic terms are then evaluated through integrated fuzzy-TOPSIS method to produce  
24 numerical value which is the performance rating for each characteristic of SME alternatives.  
25 According to the fuzzy rule, the alternative with the highest value is chosen as the standard  
26 and other variables of alternatives are compared with the standard. The advantage of using  
27 fuzzy- TOPSIS is that it distinguishes benefit and cost category criteria and selects solution  
28 that is closed to the positive ideal solutions and far from the negative ideal solutions.  
29 Moreover, the paper offers a new method of identifying best SME using integrated  
30 fuzzy-TOPSIS and recommends optimum performance variables.

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32 **Index terms**— fuzzy, multi-criteria problem, TOPSIS.

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35 and supporting in local production. The job creation element of SMEs enables many poor people to feel more  
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## 1 D) CONTRIBUTION OF THIS PAPER

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47 the negative ideal solutions. Moreover, the paper offers a new method of identifying best SME using integrated  
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49 Keywords: fuzzy, multi-criteria problem, TOPSIS. a) Purposes of SMEs the small and medium manufacturing  
50 enterprises (SMEs) manufactures a great number of metal products every day. Manufacturing SME has a big  
51 contribution from repairing metal parts to manufacturing complex parts. There is wide range of activities behind  
52 the manufacturing system, from raw material to finished product until the product is used by customer or recycled.  
53 One of the most important roles of SMEs is poverty alleviation through job creation. The developed as well as  
54 developing countries are taking extreme benefits from SMEs and that are capable to accelerate the economy of  
55 any country. In developing countries, SMEs are major source of income. The following ??arkis (2006) found  
56 that early adoption and increased investment in environment risk management did not increase performance  
57 for small firms in the metal finishing industry. Paying particular attention to the needs of small and medium  
58 sized enterprises (SMEs), Project Acorn by Gascoigne j. provides a framework for the systematic management  
59 of environmental issues within individual organizations and the supply chains to which they belong ??1]. ??oyli  
60 et al. (2008) analyzed the relationship between logistics performance and financial performance in Finnish small  
61 and medium-sized enterprises (SMEs). Several studies in South Africa ??Mutezo, 2006; ??aas and Herrington,  
62 2006; ??ngela and Motsa, 2006; ??errington et al., 2008; ??usara and Fatoki, 2011) have alluded to lack of access  
63 to financing as one of the major challenges impeding the survival and growth in the SME sector. ??agner, B. A.  
64 et al. (2003) worked on E-business and Esupply chain strategy in small and medium sized businesses (SMEs).  
65 In a study in India's machine tools SMEs, Pillai (2010) found that proper inventory management practices  
66 results in lower inventory costs. In another study, ??ee (2006) revealed that many Chinese small manufacturing  
67 firms face size-related difficulties in implementing JIT. Lee suggested that Chinese small firms can achieve their  
68 goals by implementing only feasible elements of JIT without too much capital investment. ??ayraktar, E. et al.  
69 (2009) made a causal analysis of the impact of information systems and supply chain management practices on  
70 operational performance having evidence from manufacturing SMEs in Turkey. ??hagwat, R., & Sharma, M. K.  
71 (2006) worked on Management and practice of information system in Indian SMEs. While it is acknowledged  
72 that large firms have an advantage for adopting sustainable practices more than SMEs and that SMEs adoption is  
73 necessary in the long run, studies found that the rate of return on early adoption is not encouraging. Banomyong,  
74 R., & Supatn, N. (2011) developed supply chain performance tool for SMEs in Thailand. There is also a vast  
75 literature on business success of small and medium enterprises (SMEs). ??udretsch (2005) showed the relationship  
76 between ownership, decision making and employee deployment and the performances of the SMEs. In a research  
77 study on SME's in Indonesia ??Robert, 2007) founded that SMEs operate on traditional lines in marketing. Strict  
78 reaction on account of competition should be responded proactively by SMEs by doing business development and  
79 research Information access it stands for the availability of business information is also important to initiate new  
80 enterprises and to run the existing enterprise profitably. Technology also plays an important role in this respect.  
81 Technology has a close relationship with improvement of production process. Different studies have also revealed  
82 the similar results that lack of new technology and equipment are hindrances of SME development ??Swierczek  
83 & Ha, 2007). In Indonesian study it was revealed that business has no sufficient relation with the success of an  
84 SME ??Huggins, 2007).

### 1 d) Contribution of This Paper

85 Works on SME were seen frequent formerly. While it is acknowledge that large firms have an advantage for  
86 adopting change discussed above where SMEs have no option but SMEs adoption is necessary. More research is  
87 thus needed on how SMEs should approach to a standard performance. In this paper standard alternative has  
88 been selected incorporation with TOPSIS and fuzzy analysis.

89 It is a common problem found in many cases of quantitative decision making the human assessments is  
90 uncertain and it is often difficult for decision makers to supply exact numerical values for specific criteria. In  
91 this regard most of the selection parameters can't be given precisely and the evaluation data of alternatives'  
92 characteristics is expressed in linguistic term by the decision makers. Moreover human judgment on qualitative  
93 attributes is always subjective and thus imprecise. For the sake of modeling this type of characteristics in case  
94 of human approach, fuzzy logic could be the best means.

95 There are many more operational tools for this type of analysis. Among those TOPSIS (Technique for Order  
96 Preference by Similarity to Ideal Solution) is applied to solve this type of multi-criteria problem. TOPSIS  
97 method is developed by ??wang and Yoon (1981) based on the concept that the chosen alternative should have  
98 the shortest distance from the positive ideal solution and the farthest from the negative ideal solution for solving  
99 a multi-criteria decision making problem. Briefly the positive ideal solution is made up of all the best values  
100 attainable of criteria, whereas the negative is composed of all worst values attainable of criteria.

102 The rest of the paper is organized as follows: Section 2 consists of briefly discussion on SME and G fuzzy-  
 103 TOPSIS. Methodology is discussed in section 3. Rest of the paper is comprised of calculation, result& discussion  
 104 and conclusion. There is also reference and appendix annexed at the last portion.

105 The fuzzy TOPSIS approach involves fuzzy assessments of criteria and alternatives in TOPSIS (Hwang and  
 106 Yoon, 1981) [2]. The TOPSIS approach chooses alternative that is closest to the positive ideal solution and  
 107 farthest from the negative ideal solution. A positive ideal solution is composed of the best performance values  
 108 for each criterion whereas the negative ideal solution consists of the worst performance values. The various steps  
 109 of fuzzy TOPSIS are presented as follows:

110 Step 1: Assignment of ratings to the criteria and the alternatives Let us assume there are J possible  
 111 candidates called  $A = \{A_1, A_2, \dots, A_j\}$  which are to evaluate against n criteria,  $C = \{C_1, C_2, \dots, C_m\}$ .  
 112 The criteria weights are denoted by  $w = (w_1, w_2, \dots, w_m)$ . The performance ratings of each decision maker  
 113  $D = (d_{ijk})$  for each alternative  $A_j$  ( $j=1,2,3,\dots,n$ ) with respect to criteria  $C_i$  ( $i=1,2,3,\dots,m$ ) are denoted  
 114 by  $R_k = (r_{ijk})$  ( $i=1,2,3,\dots,m; j=1,2,3,\dots,n; k=1,2,3,\dots,K$ ) with membership function  $\mu_{rk}(x)$ . Step 2 : Compute  
 115 aggregate fuzzy ratings for the criteria and the alternatives. If the fuzzy ratings of all decision makers is described  
 116 as triangular fuzzy number  $R_k = (a_k, b_k, c_k)$   $K=1,2,3,\dots,k$ ; then the aggregated fuzzy rating is given by  
 117  $R = (a, b, c)$ ,  $K=1,2,3,\dots,k$  where  $a = \min\{a_k\}$ ,  $b = \frac{1}{K} \sum_{k=1}^K b_k$ ,  $c = \max\{c_k\}$  (1)

118 If the fuzzy rating and importance weight of the k th decision maker are  $X_{ijk} = (a_{ijk}, b_{ijk}, c_{ijk})$  and  $W_{ij}$   
 119  $= (w_{j1}, w_{j2}, w_{j3})$ ;  $i=1,2,3,\dots,m$ ;  $j=1,2,3,\dots,n$ ; respectively, then the aggregated fuzzy ratings ( $X_{ij}$ ) of  
 120 alternatives with respect to each criteria are given by  $X_{ij} = (a_{ij}, b_{ij}, c_{ij})$  where  $a_{ij} = \min\{a_{ijk}\}$ ,  $b_{ij} = \frac{1}{K} \sum_{k=1}^K b_{ijk}$ ,  
 121  $c_{ij} = \max\{c_{ijk}\}$  (2)

122 The aggregated fuzzy weights ( $W_{ij}$ ) of each criterion are calculated as  $w_j = (w_{j1}, w_{j2}, w_{j3})$  where  $x_{11}$   
 123  $= \frac{1}{d} \sum_{i=1}^d w_{ij}$  ( $i=1,2,3,\dots,m$ ) (9)  $d = \sum_{i=1}^d w_{ij}$  ( $v = \sum_{j=1}^n w_{ij}$ ) ( $i=1,2,3,\dots,m$ ) (9)

## 125 2 G

126 In order to identify the causes behind the production quality three SMEs were observed. Then some fundamental  
 127 points were selected. The points were of two types: qualitative and quantitative. Even menial errors were tried  
 128 to be overcome, so before taking the data they were checked and rechecked. There were some categorizations set  
 129 for quantitative data analysis. Criteria weights are calculated as the triangular fuzzy numbers and then these  
 130 fuzzy criteria weights are inserted to the fuzzy TOPSIS methodology to rank the alternatives.

131 The data were taken on the following points: Working space(in sq. ft.), light (in lumen), salary of workers, age  
 132 of machines, cutting tool quality, maintenance of machines, waste disposal system, basement space, floor quality,  
 133 welding rod, safety measures, handling equipment, working conditions, amount of work per hour, amount of scrap  
 134 material, quality of material used etc.

135 Then using fuzzy logic the qualitative and quantitative data analysis was performed.

136 The Process flow diagram is described below: (1, 3, 5, 1, 3, 5, 1, 3, 5)

## 137 3 =1

138 It is shown for the first element. Similarly others were calculated.

139 According to equation no. 4 normalized fuzzy was calculated represented in table 4. For the Alternative 1; a  
 140  $11 = 7/9 = 0.78$  For the Alternative 2;

141 (For Benefit Criteria)  $a_{21} = 3/9 = 0.33$  For the Alternative 3;  $a_{31} = 5/9 = 0.56$

142 It is shown for the first element. Similarly others were calculated. According to equation no. 5 For Alternative  
 143 1;  $a_{13} = 1/5 = 0.20$  For Alternative 2;

144 (For Cost criteria)  $a_{13} = 1/1 = 1$  For Alternative 3;  $a_{13} = 1/1 = 1$  It is shown for the first element.  
 145 Similarly others were calculated.

146 At the Table 5 the weighted normalized matrix was calculated from equation (5)

## 147 4 G

148 The fuzzy positive ideal solution (FPIS) was Calculated by using equation (6).

149  $\text{Max}(a_{11}) = \text{Max}(2.33, 5.00, 7.00, 1.00, 2.78, 5.44, 1.67, 3.89, 7.00) = 7.00$ ;

150 It is shown for the first element. Similarly others were calculated.

151 The distance of each alternative from FPIS and FNIS was calculated using equation following equation.d (a,  
 152  $b) = \frac{1}{3} [(d_{11})^2 + (d_{12})^2 + (d_{13})^2]$  (12)

153 For Alternative 1(D-), using equation 12.d  $(a_{11}) = \frac{1}{3} [(1 - 2.33)^2 + (1 - 5)^2 + (1 - 7)^2] = 17.93$   
 154  $= 4.23$

155 It is shown for the first element. Similarly others were calculated.

## 156 5 At table no.7

157 For Alternative 1(D+), using equation 12. For Alternative 1 calculation of (cc);  $cc = 63.25 / (63.25 + 78.57) =$   
 158  $0.446 = 44.60\%$ .

159 It is shown for the first element. Similarly others were calculated.

160 Table 8 shows the final result. There are three values for three alternatives. The alternative having highest  
161 value is the best, hereby standard among all. The analysis shows "alternative 1" as the standard manufacturing  
162 SME (small and medium enterprise). So the best possible alternative is "alternative 1. It is said in previous  
163 section that, on qualitative characteristics human assessment is uncertain and often subjective so the alternative  
164 characteristics are expressed in linguistic terms. There were some characteristics which were qualitative, but due  
165 to simplicity they were also transferred to quantitative. And for the purpose of confidentiality the real name of  
166 the manufacturing SMEs were not disclosed.

167 For the selection of the best alternative the proposed method is a unique one. As the best is selected by the  
168 analysis then it can be said as standard. So changing the others comparing to it can make them well efficient  
169 in production. So drastically change is not needed for SMEs. The proposed method will help the SMEs to cope  
170 with the competition in the era of industrialization. To our knowledge no previous work investigated such a  
171 solution with TOPSIS and fuzzy analysis. As the proposed method is novel, it might be applied to other MADM  
172 problem.

## 173 6 G

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182 R. A. Required brightness for working condition by electrical devices.

183 Level of material performance.

184 Material that are useless after working.

185 An action process of waste disposing.

186 Available voltage from the power supply.

187 Category of wire according to performance.

188 The process of maintaining of Machine.

## 189 7 Distinctive attribute of gas welding

190 Available space for the machine holding in basement

191 The standard of cutting fluid against similar kind Amount of production hourly(kg)

## 192 8 Quantity of worker appointed in working

193 The degree or intensity of heat present in working condition

## 194 9 Skill of worker

195 Conditions in which a worker operates machines Lower surface of the working room Distinctive attribute of  
196 welding rod Equipment that ensure safety like Goggles, apron, Hand gloves, cades.

197 The equipment used for lifting, holding.

198 Distinguishing performance level of lubricant used.

## 199 10 Payment of worker

200 Length of time machine has been worked

Categorization of belt basis of performance 1 2 3 4



Figure 1:

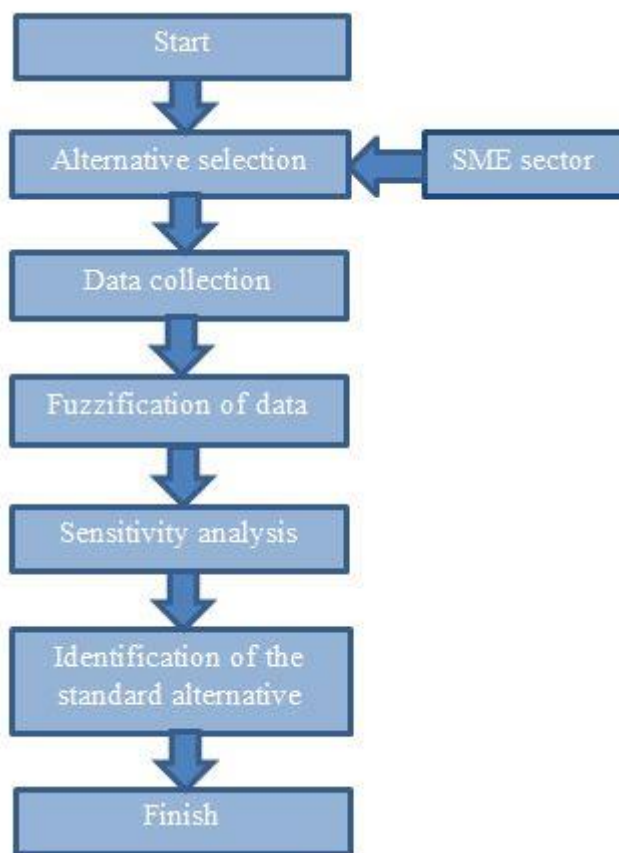


Figure 2: ?

important and necessary research, how the SMEs can be made enable without changing infrastructure, equipment, environment, budget, capacity and environment.

c) Previous Work

SMEs have received noticeable attention in the literature.

Importance of SMEs on Economy of Asian Countries country SMEs as %

		all enter- prises	employees as  % of total employees population
T	Japan	98.9	69.2
	Singapore	99.7	57.0
	Hong- Kong		60.0
	Thailand	98.0	58.0
	Philippines	99.7	68.8
	Taiwan		70.0
	Malaysia	97.7	45.0
		99.6	
		96.1	

Figure 3:

3

	Weightage			Alternative 1		
	3	5	7	7	9	
	7	9	9	3	5	
	5	7	9	7	9	
	5	7	9	7	9	
	3	5	7	5	7	
	5	7	9	5	7	
Year	3 3 5 5	5 5 7	7 7 9 9	1	3 3 3 5	
2013	7	7 9	9	1	1	
				1		
				3		
				1		
	3	5	7	3	5	
	5	7	9	1	3	
XIII	3 3 5 3	5 5 7	7 7 9 7	1	3 3 5 7	
Is-	3 7 5 3	5 5 9	7 9 9 7	1	5 1 1 7	
sue	7	7 5 9	9	3	1	
v v				5		
V				3		
Ver-				1		
sion				1		
I				5		
				1		
Volume	5 3	7 5	9 7	3	5 5	
				3		

Table 4 : Fuzzy normalized matrix for alternatives

	Global Max	Alternative 1	1.00	0.56	1.00	1.00	0.78	0.78	0.60	0.33	0.33	0.56	0.14	0.71	
Jour-	9	0.33													1.00
nal	9	0.78													0.78
of	9	0.78													1.00
Re-	9	0.56													1.00
searches	9	0.56													1.00
in	9	0.20													1.00
En-	5	0.11													0.56
gi-	9	0.11													0.56
neer-	9	0.33													0.78
ing	9	0.14													0.43
	7	0.43													1.00
	7														
	1	1.00								0.33					0.20
	1	1.00								0.33					0.20
	1	1.00								0.33					0.20
	3	1.00								0.60					0.43
	3	0.60								0.43					0.33
	3	1.00								0.60					0.43
	1	1.00								1.00					0.33
	1	1.00								1.00					0.33

[Note: G]

Figure 4: Table 3 :



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<sup>1</sup>© 2013 Global Journals Inc. (US)  
<sup>2</sup>Fuzzy-TOPSIS Analysis for Standard Alternative Selection: A Multiple Attribute Decision-Making Method and Application for Small and Medium Manufacturing Enterprises (SMEs)  
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