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# <sup>1</sup> Stress Increment Solution Charts for Soil Consolidation Analysis

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#### 6 Abstract

Current practice of estimating average stress increment required for consolidation settlement 7 computations employs mid-depth stress approach or multiple application of sublayer 8 technique, which are tedious and difficult methods to implement for hand calculations. This 9 paper presents simplified charts to estimate such a stress. The influence factor needed to 10 estimate the average stress increment is calculated based on the integration of Boussinesq?s 11 equations for common foundations and various soil configurations. The results are presented 12 in a series of normalized non-dimensional charts, which are independent of structural loads 13 and soil characteristics. The derived charts are useful especially when the compressible layer is 14 not directly located underneath the loaded foundation and they avoid the necessity of dividing 15 the soil into a series of sublayers to obtain a realistic value of average stress increment. They 16 can be readily implemented into design allowing accurate prediction of consolidation 17 settlement or can serve as a powerful tool for optimizing and proportioning the dimensions of 18 footings under certain allowable settlement where otherwise an iterative tedious solution is 19 required. Illustrative examples are presented to demonstrate the applicability and efficiency of 20 the suggested charts for consolidation settlement computations. 21

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Index terms— consolidation settlement, stress increment, influence factor, solution charts, shallow foundations.

# 25 1 Introduction

The variation of the stress produced below the foundation is non-linear in nature as schematically shown in 26 Figure ??. The intensity of the stress decreases from a maximum value just underneath the loaded area to about 27 zero at a very large distance from the Author : Department of Civil Engineering, University of Jordan, Amman 28 11942, Jordan. E-mail: ismeik@ju.edu.jo foundation. The calculation of the stress increment in a compressible 29 layer is commonly dealt with by the middepth stress approach as suggested in the literature (Terzaghi 1943;Dunn 30 et al. 1980 Das 2010). Usually, the average stress increment of the entire soil stratum is assumed to be the one 31 calculated at the middle of layer ignoring the non-linear variation of the stress, which may produce a substantial 32 error. 33

Calculations of average stress increment in soil mass are improved by subdividing the soil stratum into a number 34 35 of horizontal sublayers as illustrated in Figure ??. The technique involves replacing the smoothly varying stress 36 distribution within a soil by a staircase-like distribution. The technique assumes a constant stress over each 37 sublayer and the value at the mid-depth provides an approximation of the stress increment for every sublayer. The stress at the mid-depth of each sublayer is determined and the settlement within every sublayer is separately 38 calculated, and then summed to obtain the total settlement. Although this multiple application of the sublayer 39 technique is recommended in the literature, it is not widely used since it is impractical for manual computations, 40 and the calculations are time-intensive and tedious. 41

The error resulting between the application of mid-depth stress approach for a soil stratum and multiple application of sublayer technique, which might be misleading and unacceptable, depends largely on the size and shape of foundation, thickness of the compressible layer and its location relative to the applied load, and the number of sublayers as rimary consolidation is the time-dependent settlement of soil resulting from squeezing out of water from the voids, due to the dissipation of the excess pore water pressure, following the application of the load increment. The resulting settlement can be particularly large when the drainage is not impeded, but its magnitude is of engineering significance only when reference is made to a tolerable settlement for a given type of structure (Balasubramaniam and Brenner 1981). The magnitude of consolidation settlement depends largely on load and soil characteristics. Thus, a reliable settlement analysis requires accurate determination of the induced

51 stress in the soil layer in addition to reliable consolidation parameters. P II.

#### 52 2 Global

# 53 **3 STUDY MOTIVE**

54 Current practice of estimating average stress increment required for consolidation settlement computations usually 55 employs conventional methods such as mid-depth stress approach or multiple application of sublayer technique, 56 which are both tedious and difficult to implement for hand calculations. In addition, they do not consider the 57 case where the compressible soil layer is not directly located below the loaded foundation.

This paper enables the average stress increment beneath the center of a uniformly loaded foundation to be obtained as opposed to the stress increment at a specific depth. A series of normalized non-dimensional charts are developed to estimate the influence factor of a finite soil layer based on size and shape of foundation, thickness of compressible layer, and its location relative to the applied load. Numerical examples are included to illustrate the effectiveness and applicability of the derived charts for settlement computations. A comparison is made between

63 the results obtained by these charts and conventional methods.

#### 64 **4** III.

#### 65 5 DERIVATION

As proposed by Terzaghi (1943), the magnitude of consolidation settlement of a compressible layer is determined as:dz z z m dS v) () (?? = (1)

in which dS is the differential settlement due to compression of soil thickness dz, m v (z) is the soil coefficient of volume compressibility, and is the vertical stress increment produced below the loaded foundation at a particular depth z.

#### <sup>71</sup> 6 If the coefficient of volume compressibility m v (z)

is taken as a constant, at least at certain depths, the total consolidation settlement S, over the entire thickness of soil stratum H, is the integration of Equation (1) as:? ? = H v dz z m S 0 ) (? (2)

Based on the theory of elasticity, Boussinesq (1885) provided the equations needed to calculate the stress increment in a soil mass. The equations consider a point load on the surface of a semi-infinite, homogeneous, isotropic, weightless and elastic halfspace. The integration of vertical stress at a depth below a uniformly loaded area was originally described by Newmark (1935). Then the solutions were later improved by Steinbrenner (1936) and graphically represented and summarized by Fadum (1948), and Poulus and Davis (1974). Despite of all the unrealistic assumptions used to develop such solutions, they are still traditionally being used in the literature to obtain the stress increment under foundation loads. Using Boussinesq (1885) solutions, the calculation of the

stress increment beneath the center of a uniformly loaded foundation is computed as:) ( ) ( z qI z = ?? (3)

where is the surface contact stress at the foundation level. is a non-dimensional influence factor defined as:? ? ? ? ? ? + + + + + + + + = ? 2 2 2 1 2 2 2 2 2 2 2 1 sin ) )( 1 ( 2 1 1 2 n n m m n m n m n m m m I ?(4) where m and n are dimensionless shape and depth factors, respectively, defined as a function of the rectangular foundation dimensions width B, and length L, as:B L m = and B z n 5 . 0 = (5)

where I are is the average influence factor of soil stratum defined as:? = H are dz z I H I 0 ) (1(8)

The integration of Equation (8) is commonly dealt with numerically since the influence factor I has a ??(z) ??(z) ??(z) q I ??(z), complex non-linear variation, which is a function of shape and size of the foundation, and depth of soil layer as given by Equations (4) and (6). Accuracy is improved when the integration is calculated over an infinite number of sublayers each of an infinitesimal uniform thickness dz. IV.

#### 97 7 RESULTS AND APPLICATION

98 Hand calculations of the average influence factor I ave of Equation (8), over a series of several sublayers, is 99 impractical and tedious even for a single soil layer. Alternatively, a computer code is developed to evaluate the integral numerically and the results are presented graphically. The solution charts, which are independent of structural loads and soil properties, consider a relative configuration of the compressible layer H 2 /H 1 ranging from 1 to 10, and common foundation types such as square (L/B = 1), rectangular (L/B = 2 and 3), strip (L/B > 10), and circular ones as presented in Figures ??, 3, 4, 5, and 6, respectively.

The presented charts are the exact solutions of average influence factor and they can be used confidently 104 in geotechnical design. They enable the average stress increment, beneath the center of a uniformly loaded 105 foundation, to be obtained directly as opposed to the stress value at a specific depth, as provided by Boussinesq's 106 (1885) solutions. The charts, which agree well with the results of Ismeik (2012), have two powerful and practical 107 advantages for preliminary foundation design when hand calculations are carried out, and especially if the 108 compressible layer is not directly located below the loaded foundation. Firstly, the estimation of the average 109 influence factor is far easier when obtained from the charts and thus avoids the use of mid-depth stress approach, 110 which may produce a large error. Secondly, the charts can be used efficiently to optimize the required dimensions 111 of a footing constrained by a tolerable settlement, as an alternative to classical mid-depth stress approach where 112 an iterative method is required to find minimum dimensions. V. 113

#### 114 8 EXAMPLES

The use of the charts in settlement computations is illustrated by considering the 2 m width square footing as shown in Figure 7. The soil profile is The error produced by the use of the proposed charts is about 1.99% of actual settlement, which is quite acceptable.

Had the mid-depth stress approach been used to calculate the influence factor I, for m = 1 and n = 3.5, the computations for settlement predication using Equations (4) and (??) would be: Such a settlement value yields a significant error of about 33.41%, which is definitely unsatisfactory in geotechnical design. Thus, the direct use of mid-depth stress approach may provide inaccurate results and can be misleading when compared with actual settlement values. As seen, the provided charts simplified the computations and can be used confidently to predict the average stress increment with acceptable accuracy.1371.05.315.311sin) 5.31)(5.31 (5.32115.3115.3122221222

Another powerful application of the proposed charts would be to determine the minimum dimensions of a footing required to satisfy an allowable settlement. If design code permits a tolerable settlement of 25.4 mm (1 inch) for the above footing, the average influence factor can be obtained directly from Figure ?? for several trials of width B. Then the corresponding settlement is calculated from Equation (7)

### **129 9 SUMMARY AND CONCLUSIONS**

Solution charts to predict the average vertical stress increment needed for consolidation settlement analysis are presented based on the numerical integration of Boussinesq's solutions. A software code is developed to provide relationships between the influence factor and shape and size of foundation, thickness of compressible layer, and its depth relative to the location of applied load.

The suggested charts provide a refined estimate of the stress increment, which could only be obtained with a large number of sublayers in the routinely used multiple application of the sublayer technique. In addition, if the soil is considered as one layer system, the mid-depth stress approach may provide inaccurate results.

The presented charts can be used as an alternative to current conventional methods. They represent an efficient and powerful solution to calculate the average stress increment especially when the compressible layer is not directly located below the loaded foundation, or can serve as a useful tool for optimizing and proportioning the dimensions of footings under an allowable settlement.

The most important advantages of these charts, when compared to conventional solutions, are their speed, ease of implementation, and versatility for routine hand settlement calculations required for geotechnical design of shallow foundations.



Figure 1: 11 Fig. 1 :

Figure 2:

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