

Identification of Dominant Shape Characteristic for Particle Packing Models using an Imaging Technique for Aggregates

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Abstract

Aggregates occupy most of the volume of concrete. A proper packing of aggregates with binding material ensures reduction in voids and thereby better performance of concrete. A good packing of the aggregates in a mix can be achieved by filling up the void space left by large or coarse aggregates by the finer aggregates, followed by standard process of compaction. Therefore, precise evaluation of characteristics of ingredients of concrete is highly essential. Various mathematical models for studying concrete mix proportions have been proposed in the literature. Most of these models have remained restricted to studying spherical or near-spherical particles. Therefore there is a need to understand whether there is a possibility of extending the existing theories to non-spherical particles also. The paper also presents the development of Digital Image Processing (DIP) based system for the measurement of volume, equivalent volume diameter, sphericity, roundness index of coarse aggregate particles.

Index terms— aggregate, shape characteristics, particle packing, DIP

1 Identification of Dominant Shape Characteristic

for Particle Packing Models using an Imaging Technique for Aggregates Madhuri N. Mangulkar ?, Suddhasheel Ghosh ? & Sanjay S. Jamkar ? Abstract-Aggregates occupy most of the volume of concrete.

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A good packing of the aggregates in a mix can be achieved by filling up the void space left by large or coarse aggregates by the finer aggregates, followed by standard process of compaction. Therefore, precise evaluation of characteristics of ingredients of concrete is highly essential. Various mathematical models for studying concrete mix proportions have been proposed in the literature. Most of these models have remained restricted to studying spherical or nearspherical particles. Therefore there is a need to understand whether there is a possibility of extending the existing theories to non-spherical particles also. The paper also presents the development of Digital Image Processing (DIP) based system for the measurement of volume, equivalent volume diameter, sphericity, roundness index of coarse aggregate particles. The system is calibrated using standard objects such as marbles, coins and then used for the measurement of coarse aggregate particles having varied characteristics. The dimensions of the aggregates i.e. the longest, the intermediate and the shortest dimensions and obtained using mathematical morphological operations. A detailed analysis of the various shape characteristics shows that sphericity is the most effective measure. The authors are currently working in the direction of extending the mathematical model using this shape characteristic.

2 Introduction

Aggregates occupy bulk of the volume of concrete. Their characteristics such as size, grading, shape and texture have significant effect on the properties of concrete in both fresh and hardened state. The effect is more significant in the case of high strength concrete. The properties of concrete such as strength, workability, cohesiveness and durability depend upon the properties of its constituents and their relative proportion in the mix.

43 Evolutions in concrete mix proportioning procedures are taking place since long. Particle packing theories
 44 have been under development to further refine the mix proportioning process. Particle packing models proposed
 45 by the researchers include (a) continuous, (b) analytical and (c) discrete element. Out of these, analytical particle
 46 packing models provide relatively better solution for concrete mix proportioning. The analytical model assumes
 47 that each class of particle will pack to its maximum density in the available volume. Theoretically, it gives
 48 the packing density of a mix based on particle size distribution and individual packing densities of various size
 49 fractions that are present in the distribution.

50 3 a) Research Significance

51 It is understood that the aggregate particles present in a concrete mix would interact based on their respective
 52 sizes and shapes. Our work is in the context of analytical modelling of this inter-particulate interaction. De
 53 Larrard [1] and Yu et al. [7] have attempted to model this interaction between the various aggregate particles in
 54 a mix, based on size fractions. Therefore, it is important to discuss the sizes and shapes of the aggregate particles
 55 and the consequent inter-particulate interactions. In this paper we describe a scanning system for aggregates,
 56 to identify the various shape descriptors, and choose the most effective one, and identify an effective modelling
 57 system based on the literature.

58 4 b) Estimation of packing density in a mix

59 De Larrard [2,3,4,5] has constrained his study on two types of aggregates namely rounded and crushed. In his
 60 study, the interaction between the coarse and fine particles in a concrete mix are modelled using the wall effect
 61 and loosening effect functions. These functions are finally used to determine the packing density in a concrete
 62 mix.

63 (1)

64 Where the function W_{eff} and L_{eff} represent the wall effect and the loosening effect respectively, and
 65 are given by the following equations.

66 (2)

67 (3) However, in reality, it is seen that aggregates are available in different shapes and sizes, see Figure 1. In
 68 their study, Yu et al. [7] had considered sphericity as an additional input to be given to the interaction function
 69 for the wall and loosening effects. The interaction functions proposed by Yu et al. [7,8] are given in the following
 70 equations.

71 (4) (5) where, R is defined as the ratio of equivalent packing diameters, with the value of R ranging between
 72 0 and 1. The equivalent packing diameter D_{eq} , for a particular aggregate is given as: Therefore, it would be
 73 interesting to investigate whether the other measures can also contribute to improvising the modelling system
 74 for interaction. $W_{eff} = 1 - [1 - W_{eff} + W_{eff} R]^{-1}$ $L_{eff} = 1 - [1 - L_{eff} R]^{-1}$ $W_{eff} = 1 - [1 - W_{eff} R]^{-1}$
 75 $L_{eff} = 1 - [1 - L_{eff} R]^{-1}$ $W_{eff} = 1 - [1 - W_{eff} R]^{-1}$ $L_{eff} = 1 - [1 - L_{eff} R]^{-1}$ $W_{eff} = 1 - [1 - W_{eff} R]^{-1}$
 76 $L_{eff} = 1 - [1 - L_{eff} R]^{-1}$

77 5 c) Assessment of the shape and classification of aggregates

78 Several researchers have studied the shape and classified aggregates. These studies can be categorised into the
 79 following groups: (a) based on computer tomography, (b) based on laser scanning, and (c) based on camera based
 80 scanning. It is realised that computer tomography and laser scanning based techniques are difficult to be applied
 81 on the field, and are also expensive. Therefore, in this study camera based scanning techniques are discussed and
 82 implemented.

83 Most camera based study techniques developed till date use an arrangement that image the aggregate from
 84 two different sides to assess the longest, intermediate and the smallest sides of the minimal box containing the
 85 aggregate, represented as a triplet (l_1, l_2, l_3). However, a complete three dimensional picture of a complex
 86 shaped aggregate can be obtained only if it is imaged from multiple sides. Therefore, there is a need to develop
 87 a new system which can image an aggregate to obtain its precise dimensions.

88 6 d) Shape characteristics of an aggregate

89 The shape characteristics of an aggregate have been traditionally expressed in terms of sphericity, elongation,
 90 flatness and shape factor. The various formulae for determining these characteristics for a given triplet ($l_1, l_2,$
 91 l_3) are given in Table [1]. e) Research questions Based on the above discussions, we pose the following research
 92 questions for this paper: 1. Which is the most effective shape parameter for distinguishing various shapes of
 93 aggregates? 2. Can a system be designed which can image an aggregate from more than two sides? 3. Can the
 94 de Larrard's [4] CPM theory be extended to include more shapes of aggregates?

95 II.

96 7 Methodology

97 This section presents the design of a system for imaging various facets of aggregates, analysing the shapes of
 98 aggregates and the possible extension of de Larrard's [1] theory, in the light of the discussion and the questions

99 proposed in the previous section. In order to measure the various characteristics of an aggregate, it is placed
100 on the aggregate tray mounted on a conveyor. The conveyor arrangement moves the tray linearly to the first
101 position (in front of bottom camera) where the first LED lamp illuminates the aggregate. The bottom camera
102 captures the first image. The aggregate tray then moved to a second position on the turn table where a second
103 image is captured by the top camera. The third camera at the front also captures an image simultaneously. It
104 also captures images by turning the tray through 90, 180 and 270 degrees. The turntable rotates the tray by
105 270 degrees in opposite direction and conveyor brings it to the original position. The steps are repeated till the
106 image acquisition of all the aggregate particles in the sample is completed.

107 The system is calibrated using standard objects of known dimensions such as coins, rectangular prisms and
108 marbles. The dimensions of the objects are measured manually using standard vernier calliper. Digital images
109 of these objects are acquired by placing the objects one at a time, at a distance of 10cm from each camera. Six
110 images are taken at an interval of 5 seconds. Each camera in the system provided an image of dimensions 1600
111 pixels x 1200 pixels. The images are processed using MATLAB through the following steps: (a) conversion of
112 RGB images to gray scale, (b) noise filtering, (c) detection of boundary, and (d) computation of longest (dl),
113 intermediate (di), and shortest (ds) dimensions of the object. Based on the results, it is observed that 1600 pixels
114 correspond to 62.4 mm i.e. 0.039 mm/pixel.

115 **8 b) Analysis of shape characteristics**

116 In this study, four different categories of aggregates are tested, viz. Elongated, rounded, angular and cylindrical.
117 30 aggregate pieces of each of the types are passed through the imaging arrangement (DIPAM), and the
118 measurements of their longest, intermediate and shortest dimensions were obtained. In addition, the volumes of
119 the respective aggregates were also found out using a measuring cylinder. To identify the shape characteristic
120 that distinguishes the aggregates the most, a linear separability analysis is conducted.

121 **9 c) Extension of the CPM theory**

122 It was pointed out earlier that the CPM theory proposed by de Larrard [1,4] was limited to rounded and crushed
123 aggregates. His theory proposes two activation functions, which have already been denoted by equations (1,2) and
124 (3). The activation functions proposed by Yu et al. [6,7] consider the sphericity of the aggregates as an additional
125 parameter. The activation functions proposed by de Larrard intersect with each other, see Figure 2. In his work,
126 Fennis [8,9] points out that this intersection of the two function may cause problems in "scaling". Further, in the
127 works proposed by de Larrard [1][2][3][4][5], Yu et al. [6,7] and Fennis [7,8], the curves for interaction function
128 are convex. Thus, in this context, it might be said that (a) the interaction functions must not intersect with each
129 other, (b) must be convex, and (c) must be inclusive of the shape parameters.

130 **10 III.**

131 **11 Results and Discussion**

132 **12 a) Calculation of the shape parameters**

133 Aggregates of different shapes and sizes were passed through the imaging system. The dimensions of each of
134 the aggregates were obtained. Further, the volumes of each of the aggregates was also calculated. The shape
135 parameters calculated for each of the types of aggregates are given in (as shown in Table 1).

136 **13 b) Choosing the most distinguishing factor**

137 It is seen from a separability analysis and also (as shown in Table ??), that sphericity is the most discriminating
138 factor amongst all types of aggregates. Hence, in this study, sphericity is chosen. c) Choice of the interaction
139 functions Both de Larrard and Yu et al. [6,7] have proposed interaction functions for modelling the interparticle
140 interactions in the CPM theory. Furthermore, both the theories use particle size ratio r . In contrast to de
141 Larrard's approach where r is taken as a ratio of particle diameters, Yu et al [6,7] have represented r as a ratio
142 of equivalent packing diameters, where they have considered sphericity as a shape factor. It was argued earlier,
143 in this paper, that Fennis [8,9] objected to the interaction functions intersecting between the values or $r = 0$
144 and $r = 1$, where r denotes the particle size ratio.

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147 It is seen that the model of the interaction functions proposed by Yu et al [6,7] are mathematically simpler, and
148 than the changes in the different coefficients and the exponents can change the shape of the function. Further,
149 based on the respective choices, these functions may or may not intersect with each other. It remains to be
150 investigated as to what could be these choices for coefficients and exponents.

151 IV.

15 Conclusion

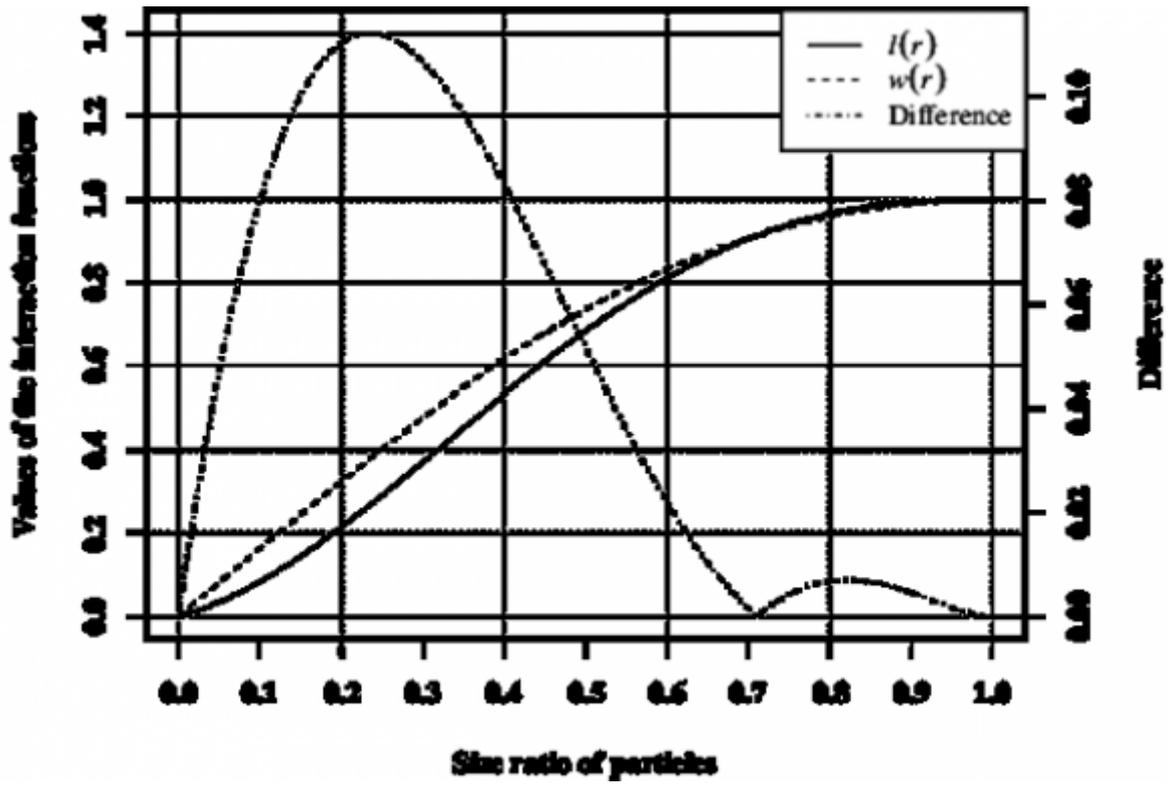
152

153 In this work, we have presented the design of an imaging system, which improves on the past imaging systems to
154 give a more complete picture of the dimensions of an aggregate. The dimensions captured by the imaging system
155 are analysed for shape characteristics of the aggregates. It was found that sphericity is the most prominent
156 measure of shape amongst the four considered in this study. It was also seen that the model of interaction
157 functions proposed by Yu et al [6,7] are more appropriate to extend the study of the CPM theory proposed by de
158 Larrard [1][2][3][4][5]. The tuning of the coefficients and the exponents in the model of the Yu et al [6,7] remains
to be seen and will be conducted by the authors in the future research work. ¹



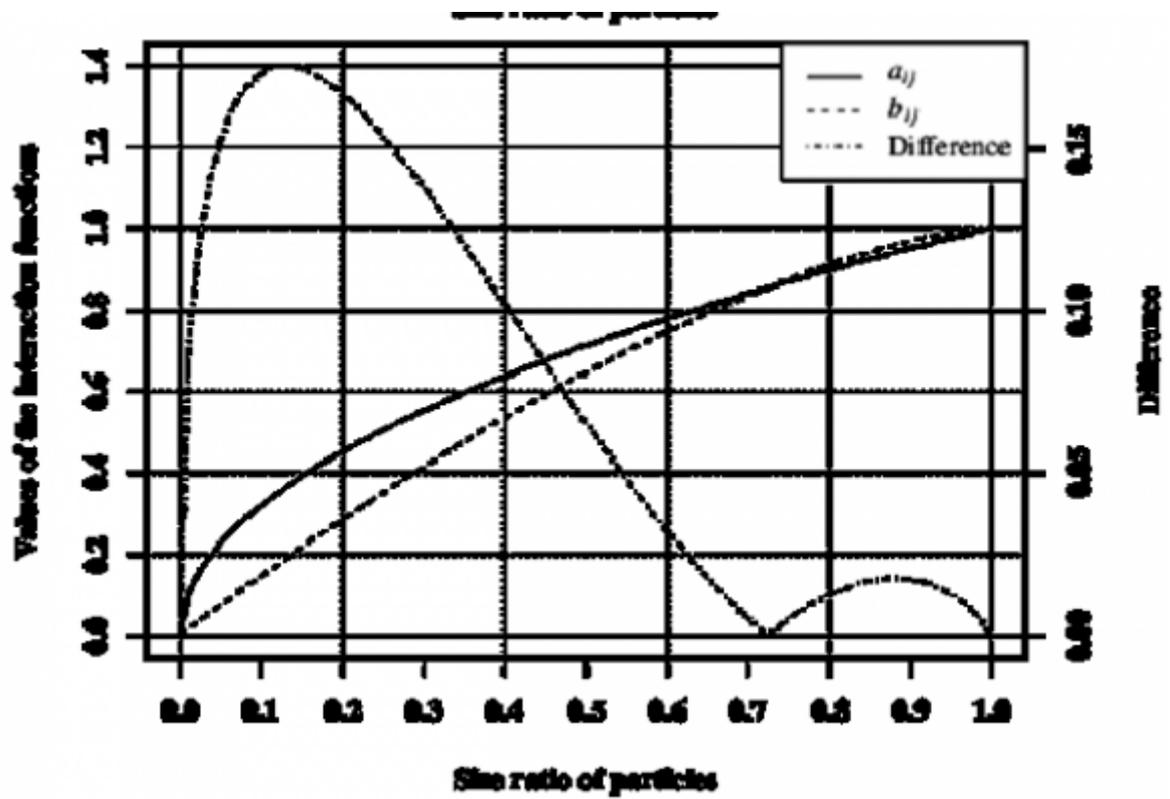
Figure 1: Figure 1 :

159



2

Figure 2: 3EFigure 2 :



3

Figure 3: Figure 3 :

1

FACTOR	FORM	REFERENCE
Shape factor		Barksdale et al.[10]
Flatness		Barksdale et al.[10]
Elongation		Kuo et al.[11]
Sphericity		Kuo et al.[11]

Figure 4: Table 1 :

2a

AGGREGATE AVERAGE DIMENSIONS IN MM AS PER DIP LONGEST (DL) INTER-MEDIA TYPE
 - SIZE
 GATE FRACTIO
 TYPE IN MM

1	2	3	4	5
	4.75-6.3	16.10	5.40	4.30
	6.3-10	16.69	10.75	6.31
Type-10-12.5	20.57	10.75		8.71
A- Elongat ed	12.5-16	27.40	12.75	10.88
	16-20	43.70	23.00	12.50
	20-25	30.10	23.30	14.00

Figure 5: Table 2a :

2b

AGGREGATE AVERAGE DIMENSIONS IN MM AS PER DIP LONGEST (DL) INTER-MEDIA TEST
 - SIZE
 GATE RATIO
 TYPE IN MM

1	2	3	4	5
	4.75-6.3	9.20	5.43	5.28
	6.3-10	12.15	6.08	5.90
Type	10-12.5	16.65	9.68	9.48
B	Angular	15-16	20.40	11.83
	16-20	27.80	16.30	11.50
	20-25	31.25	19.65	1350.00
				2774.15
				1387.07
				15.70
				3000.00
				7114.30
				3557.15
				18.85
				5000.00
				11575.08
				5787.54

Figure 6: Table 2b :

2c

	AVERAGE DIMENSIONS IN MM AS PER DIP										VOLUME IN M ³						
	AGGRGATE TYPE	SIEVE SIZE IN MM	LONGEST (DL)	INTER-MEDIA (DI)	SHORTEST (DS)	ARCHI-MEDESAL PRINCIPLE		EQUISAL PRINCIPLE		EQUISAL PRINCIPLE							
	1	2	3	4	5	6	7	8	9	10	11	12					
Year 2021	Type- C	6.3-10	10-12.5	15.15	9.68	10.75	6.33	12.5-16	22.90	14.48	6.08	9.53	14.10	3500.00	4673.83	36	
Volume Xx XI Issue I V		16-20	20-25	26.30	14.48	30.10	18.28	14.10	6000.00	5367.76	4215.83	55.3	17.80	8000.00	9791.38	7690.13	-85.

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Figure 7: Table 2c :

2d

AGGREGATE TYPE	SIEVE SIZE	FRACTION IN MM	AVERAGE DIMENSIONS IN MM AS PER DIP			VOLUME IN MM ³ AS PER		
			LONG-INTENT (DL)	SHORT- MENDS TE (DS)	(DI)	ARCHIM-EQUIVA- EDES LENT PRIN- CYLINDE CIPL R E		
1	2		3	4	5	6	7	
	4.75-6.3	7.82 5.83			4.75	100.00	379.38	151.752
	6.3-10		8.40	9.30	6.18	300.00	1312.14	524.856
Type	10-12.5	13.45 12.60	9.13			750.00	2120.68	848.24
D								
Rounde								
d	12.5-16	15.83 15.75	10.83	1450.00	4157.68	1663.73		
	16-20	20.95 19.90	12.65	2000.00	5775.17	2310.69		
	20-25	21.50 21.00	15.03	5200.00	13229.38	5291.50		

Figure 8: Table 2d :

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