

5 MATRIX TRANSFER FUNCTION

45 Accordingly, we have for Figure 2 the Laplace transforms the following system of the equations for k the piezo
46 layer in the form $() () () p Z Z Z p F Z Z p F k out k inp k 1 2 1 1 2 1 2 1 + ? ? ? ? ? ? ? ? + + ? ? ? ? ?$
47 $? ? ? + = ? (3) () () () p Z Z p F Z p k out k 1 2 1 1 1 1 + ? ? ? ? ? ? ? ? + + = ?$

48 the matrix equation for k the piezo layer $() () [] () () ? ? ? ? ? ? = ? ? ? ? ? ? ? ? + p p F M p [] ? ?$
49 $? ? ? ? ? ? ? ? + ? ? ? ? ? ? ? ? + + = ? ? ? ? ? ? = 2 1 2 1 1 1 2 1 2 2 2 1 1 2 1 1 2 1 Z Z Z Z Z Z$
50 $Z m m m M (5)$

51 Where $() ?? = + = = ch 1 2 1 2 2 1 1 Z Z m m , () ?? = ? ? ? ? ? ? ? ? + = sh 2 0 1 1 1 1 2 Z Z Z Z m ,$
52 $(0) 2 2 1 sh 1 Z Z m ?? = = , ? ? = ij s S Z 0 0$

53 For the multilayer piezo actuator the Laplace transforms the displacement The force on the output face for
54 the k the piezo layer equal in magnitude and opposite in direction to the force on the input face for k+1 the
55 piezo layer $() () p F p F inp k out k 1 + ? = (6)$

56 From equation (??) the matrix equation for n the piezo layers $() () [] () () ? ? ? ? ? ? = ? ? ? ? ? ? ?$
57 $? + p p F M p p F n out n n inp 1 1 1 (7)$

58 with the matrix of the multilayer piezo actuator Figure 1 a in the form $[] () () () () ? ? ? ? ? ? ? ? ? ?$
59 $? ? ? ? ? ? = n Z n n Z n M n ch sh sh ch 0 0$

60 Accordingly, in general, the matrix for the equivalent quadripole of the multilayer electro magneto elastic
61 actuator Figure 1 a-? has the following form $[] () () () () ? ? ? ? ? ? ? ? ? ? = 1 Z 1 1 Z 1 M n ch sh sh$
62 $ch 0 0$

63 Therefore, we have from the equation (??) the equivalent quadripole of the multilayer piezo actuator on Figure
64 1 a-? for the longitudinal piezo effect with length of the multilayer piezo actuator $? = n l$, for the transverse
65 piezo effect with $nh l =$, for the shift piezo effect with $nb l =$, where b , h , ? are the thickness, the height, the
66 width for k the piezo layer.

67 Equations of the forces acting on the faces of the multilayer piezo actuator at $0 = x , () () () p p M p F S$
68 $p , T j 1 2 1 1 0 0 ? + = (8) at l x = , () () () p p M p F S s , l T j d , d , d g , g , g d , d , d v mi , ? ? ? ? ?$
69 $= ? 1 3 1 3 1 3 H , H D , D E , E m , ? ? ? ? ? = ? H H H D D D E E E ij s , ? ? ? ? ? = ? H D E c c c c , ?$
70 $? ? ? ? ? ? = ? H D E , ? ? ? ? ? = nb nh n l . () () () () () () [] ? ? ? ? ? ? ? ? ? ? ? ? ? ? ? ? ?$
71 $? ? ? ? ? ? ? ? \times ? + ? ? ? ? ? ? ? = ? ? p p l l p p F p M p m mi ij$
72 $2 1 1 2 1 1 ch sh 1 1 (10) () () () () () () [] ? \times ? ? ? ? ?$
73 $? ? ? ? ? ? ? ? ? ? ? ? ? ? ? ? + ? ? ? ? ? ? ? = ? ? p p l l p p F p M p m mi ij 1 2$

3 S s E E = ?

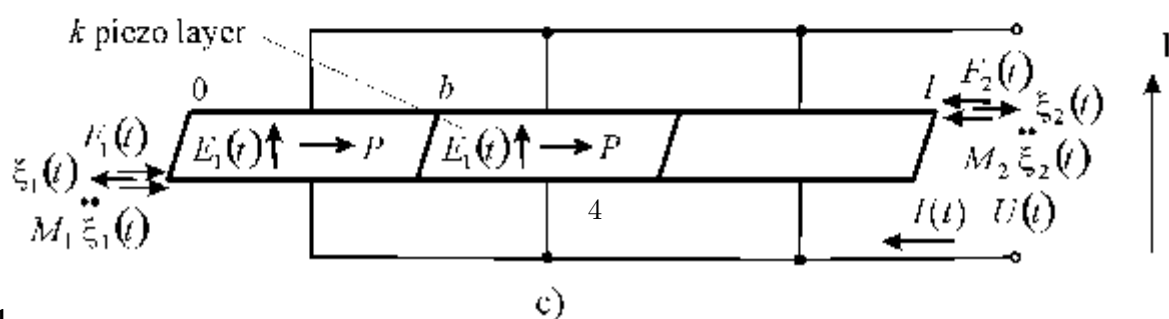
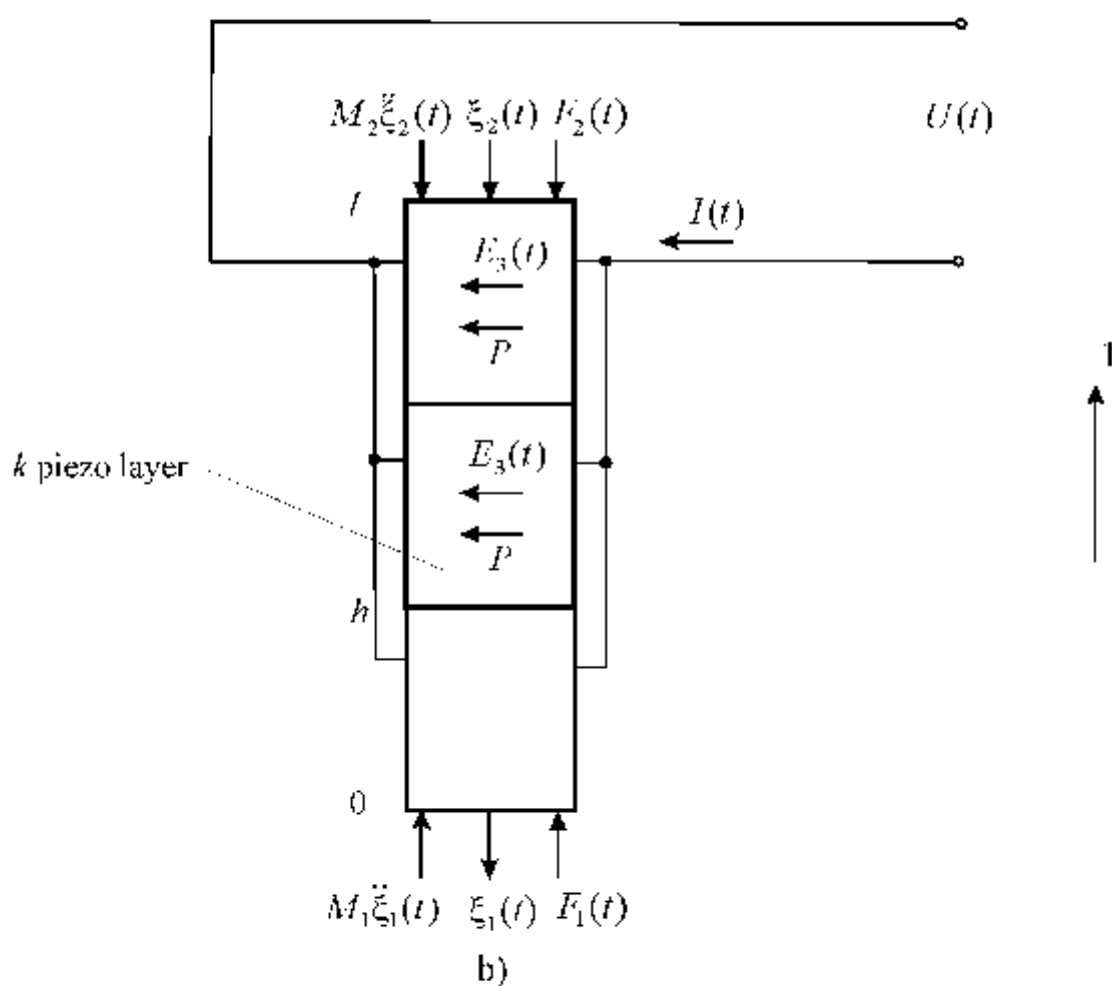
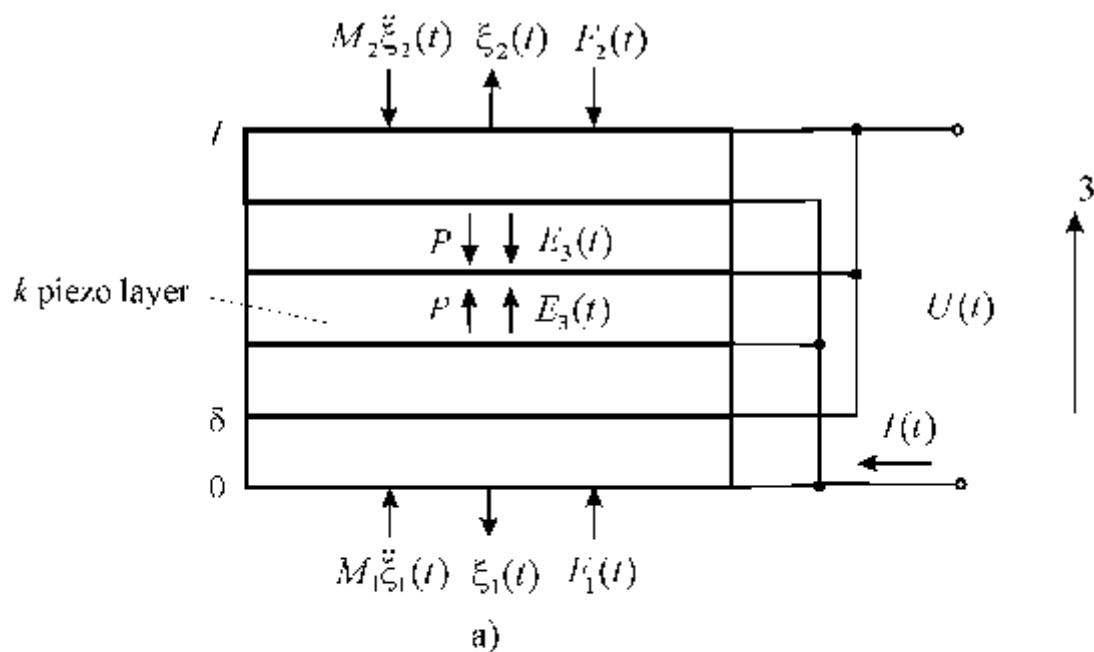
74 The structural-parametric model of the multilayer piezo actuator for the transverse piezo effect has the form
75 For the shift piezo effect the Laplace transform of the caused force The structural-parametric model of the
76 multilayer piezo actuator for the shift piezo effect has the form We drew the structural schematic diagram of the
77 actuator from the generalized structural-parametric model of the multilayer electro magneto elastic actuator for
78 the nanomechanics. $() () E s p E S d p F 5 5 1 0 1 5 = (15) 0 5 5 5 S s E E = ? () () () () () () [] ? ? ?$
79 $? \times ? + ? ? ? ? ? ? ? = ? p p l l$
80 $p E d p F p M p E 2 1 3 3 3 3 1 2 1 1 ch sh 1 1 (12) () () () () () [] ? ? ? ? ? ? ? ? ? ? ? ? ? ? ? ? ?$
81 $? ? ? ? ? ? ? ? \times ? ? ? ? ? ? ? ? ? ? ? ? ? ? ? ? ? ? + ? ? ? ? ? ? ? = ? p p l l p E d p F p M p E 1 2 3$
82 $3 3 3 2 2 2 2 ch sh 1 1 () () () () () () [] ? \times ? ? ? ? ?$
83 $? ? ? ? ? ? ? ? ? ? ? ? + ? ? ? ? ? ? ? = ? p p l l p E d p F p M p E 2 1 3 3 1 1 1 2 1 1 ch sh 1 1 (14) ()$
84 $() () () () () [] ? \times ? ? ? ? ? ? ? ? ? ? ? ? ? ? ? ? ?$
85 $+ ? ? ? ? ? ? ? = ? p p l l p E d p F p M p E 1 2$
86

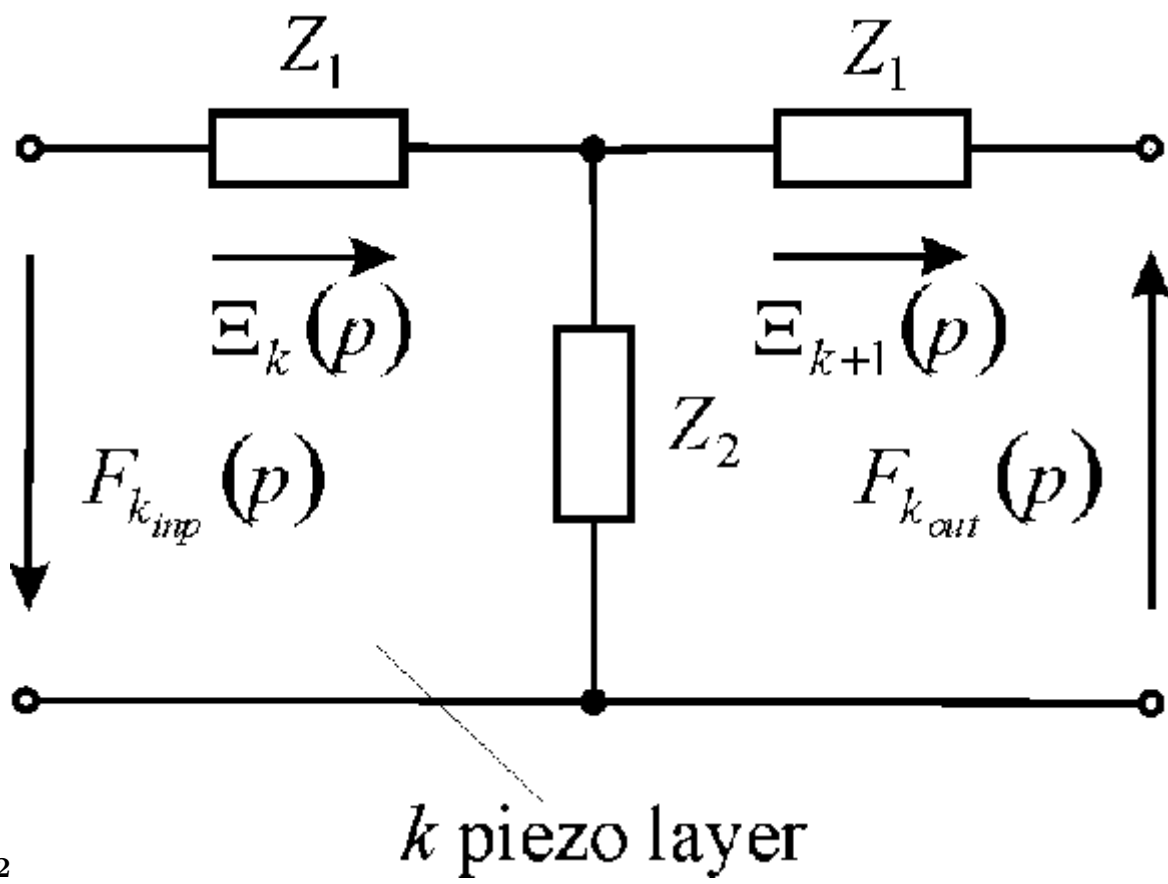
4 III.

5 Matrix Transfer Function

87 From equation (10) we receive the matrix transfer function of the multilayer electro magneto elastic actuator with
88 n the layers in the following form Therefore, in general, we have the matrix transfer function of the multilayer
89 electro magneto elastic actuator in the form $() () () () () () () () () ? ? ? ? ? ? ? ? ? ? ? ? ? ? ? ? ?$
90 $? = ? ? ? ? ? ? ? ? p F p F p p W p W p W p W p W p () [] () [] () [] p P p W p = ? (18) () [] () () ?$
91 $? ? ? ? ? ? ? = ? p p p 2 1 () [] () () () () () ? ? ? ? ? ? = p W p W p W p W p W p W () () ($
92 $) () [] ij ij mi m A l p M p p p W 2 th 2 2 1 1 1 ? ? + ? ? = ? ? = ? 0 S s ij ij ? ? = ? () () () [] { } () ($
93 $) [] 2 2 2 2 1 3 2 1 4 2 2 1 2 1 th ? + ? + ? ? + ? ? + ? ? = ? ? ? ? ? ? c p p c l M M p l c M M$
94 $p M M A ij ij ij () () () [] ij ij ij m A l p M p p p W 2 th 2 1 2 2 1 ? ? + ? ? = ? ? = ? () () () () []$
95 $ij ij A l p M p F p p W ? ? + ? ? ? = ? = ? ? th 2 2 1 1 1 2 () () () () () () [] ij ij A l p F p p W p F$
96 $p p W ? ? ? = ? = ? = ? sh 1 2 2 2 1 1 3 () () () [] ij ij A l p M p F p p W ? ? + ? ? ? = ? = ? ?$
97 $th 2 1 2 2 2 3$

100 We receive the generalized parametric structural schematic diagram and the generalized matrix transfer
101 function from the generalized structural-parametric model of the multilayer electro magneto elastic actuator
102 to calculate its static and dynamic characteristics for the nanomechanics. Let us consider, for example, the
103 voltage-controlled multilayer piezo actuator for the longitudinal piezo effect with the inertial load $1 M m \ll , 2 M$
104 $m \ll$ and $() () 0 2 1 = = t F t F$





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Figure 2: Figure 2 :

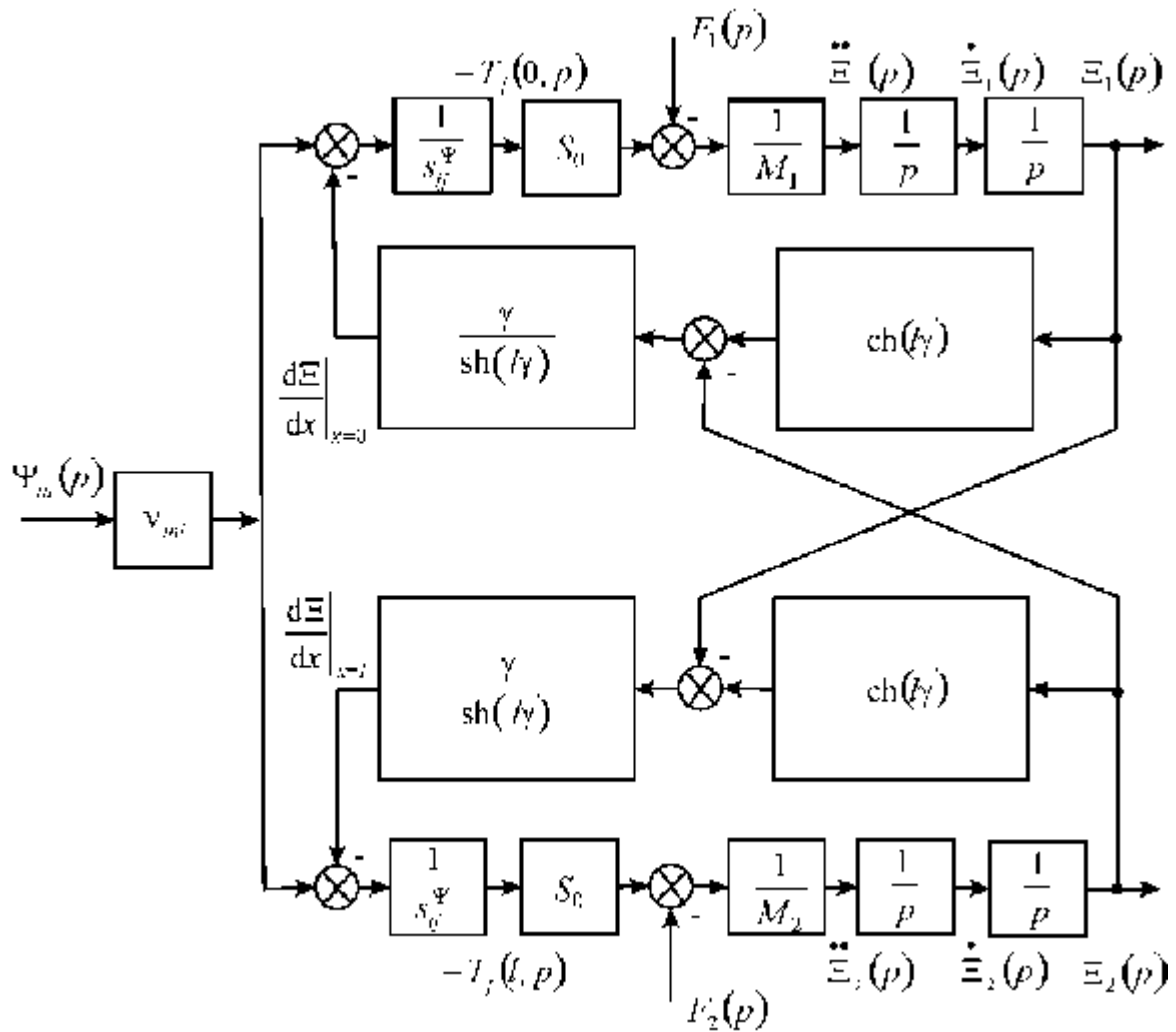


Figure 3:

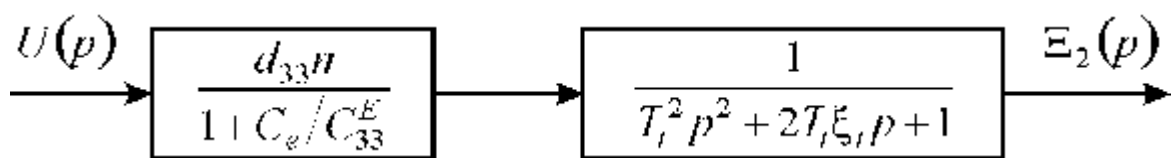


Figure 4:

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7 V. ONCLUSION

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