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¹ Supplier Selection using Integer Linear Programming Model

2	Md. Sazol Ahmmed ¹ , Sourav Kumar Ghosh ² , Naurin Zoha ³ , Tanzima Zoha
3	Chowdhury and Md. Sazor Annihed
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7 Abstract

Contemporary business organizations highly depend on outsourcing for success in today?s 8 competitive marketplace, and selecting a suitable supplier is an important process as 9 developing new products. Supplier selection is one of the most important decisions of supply 10 chain management which is upstream management. As organizations become more dependent 11 on vendors, the direct and the indirect consequences of poor decision- making become more 12 severe. There are a lot of methods to determine the best matched supplier for a particular 13 product. In this study, at first, we have calculated the weighted values (Using AHP) for 14 different product for different vendors. Then we have proposed a vendor selection model using 15 Integer Linear Programming (ILP) Model for multi-product, multi-vendor environment. The 16 contribution this research lies in the implementation of this model as a customized decision 17 support system according to the expectation of any company. The model is validated with a 18 case study by implementing the model for managing the best suppliers for knit fabrics of a 19 renowned textile industry of Bangladesh. 20

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22 Index terms— Keywords: vendor selection, upstream management, ILP, AHP M. MCDM.

²³ 1 I. Introduction

he supplier selection is a very crucial problem in today's highly dynamic business scenario involving many 24 25 qualitative and quantitative criteria. Suppliers are considered as a key to a firm's ability to provide quality 26 products in shorter time at lower costs and with greater flexibility and reduced risk [1]. The rise in outsourcing and off shoring practices due to globalization has also added to complexity of supplier selection problem. Moreover, 27 the need to develop sustainable supply chain practices in organizations [2] [3] have made supplier selection problem 28 even more challenging. Hence, in order to choose best suppliers, it is important to achieve a tradeoff between 29 these criteria which may be conflicting in nature. Hence supplier selection is a multi-criteria decision making 30 (MCDM) problem. We develop an integer linear programming (ILP) model for this purpose. Linear Programming 31 (LP) is one the most widely used techniques in the world of optimization, where a particular objective function is 32 developed for some unknown variables to be either maximized or minimized considering limitations or constraints. 33 ILP is one of the LP techniques where the unknown variables are all bound to be integer numbers. There is 34 another type of LP called the Binary Integer Programming (BIP), where the unknown variables can only be 0 or 35 36 1. This is, in fact, a special case of ILP. This special form gives the model a little more dimension in the process 37 of decision making. The numbers in this case represent the selection choices instead of their arbitrary values. For 38 instance, in our vendor selection method, the value for the corresponding unknown variable of a vendor signifies if the vendor is selected or not for supplying that particular product. The value 1 represents the selection of that 39 vendor and the value 0 represents that the vendor is not selected. The model is developed to fit the preference of 40 the company depending on their requirements and preference. In different circumstances, different vendors may 41 be selected. There are multiple criteria that determine the optimized selection of the vendor. We develop this 42 model keeping in consideration the weights of all the criteria and selecting the most optimal vendor to maximize 43 profits and reduce risk in the overall purchasing process. 44

There are a number of MCDM techniques applied in supplier selection process such as analytic hierarchy 45 process (AHP) [4], analytic network process (ANP) [5], technique for order preference by similarity to ideal 46 solution (TOPSIS) [6], Fuzzy set theory, elimination and choice expressing reality (ELECTRE), Preference 47 ranking organization method for enrichment evaluation (PROMETHEE), data envelopment analysis (DEA), 48 mathematical programming and their hybrids to supplier selection. There are plenty of supplier selection methods 49 available in the literature. Linear Programming (LP) formulates the supplier selection problem in terms of a 50 mathematical objective function which is a linear function that needs to be maximized (e.g., maximize profit, 51 Productivity) or minimized (e.g., minimize costs, lead time). LP has some resource constraints which need to 52 be satisfied. Some of the mathematical programming models [7] focus on the modeling of specific discounting 53 environments. Akinc function is to minimize the total cost of the wholesaling service by optimizing the selection 54 of the manufacturer. Weber et al. [10] combine MP and the DEA method to negotiate with the vendors that 55 are rejected to ensure the number of vendors to use. [11] Karpak et al. [12] use goal programming to minimize 56 costs and maximize quality and delivery reliability when selecting vendors and allocating orders between them. 57 Manoj Kumar et al. 58 [13] develop a decision tool using multi-objective integer linear progr III. Methodology a) Assumptions i. 59

We didn't consider peak and off seasons for the process. ii. We didn't account resource constraints or other constraints. iii. We neglected some criteria for simplification of the case.

62 We considered only one decision maker.

⁶³ 2 b) General Model Formulation

64 Objective Function: The objective function represents the maximization of the preference weight.

⁶⁵ 3 c) Case study for supplier selection for four different products

⁶⁶ There are four suppliers and four products to be selected. For each product, we applied AHP to rank the ⁶⁷ suppliers. We use All these weighted values are in the objective function. The problem formulated in case study

 $_{68}$ $\,$ has been solved using excel solver. The solutions

⁶⁹ 4 IV. Conclusion

Vendor selection model using ILP is developed to select the vendors for a business environment having two-70 stage supply chain. The model is tested in knit fabrics wholesaler and is effectively working out. We can 71 also use this model in real-life cases of other domains like automobile, textiles, electronic equipment and food 72 industries. The model can be further improved by splitting the allocation of each product among vendors and 73 by considering the limited capacity vendors. For more accuracy, periodic review of the key criteria should be 74 conducted. The mathematical model used in this study work can be further extended towards multiobjective 75 optimization to minimize overall procurement cost. Companies should choose the appropriate method for their 76 problem according to the situation and the structure of the problem they have. 77

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Figure 2:

[Note: 44 = 0 ????? 1 d) Solution and Result]

Figure 3:

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Figure 4: Table 1 :

- So, the company wants to select nine products from four suppliers. The result shows that product one and two are selected from vendor one, product three (two items each) is selected from two vendors (vendor two and vendor four) and product four (two items) is selected from vendor three.
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