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# Low Probability of Intercept Frequency Hopping Signal Characterization Comparison using the Wigner Ville Distribution and the Choi Williams Distribution

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#### 8 Abstract

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9 Low probability of intercept radar signals, which are often challenging to detect and

<sup>10</sup> characterize, have as their objective ?to see and not be seen?. Digital intercept receivers are

<sup>11</sup> currently moving from Fourier-based techniques to classical time-frequency techniques for the

<sup>12</sup> analysis of low probability of intercept radar signals. This paper presents the novel approach

of characterizing low probability of intercept frequency hopping radar signals through

<sup>14</sup> utilization and direct comparison of the Wigner Ville Distribuion versus the Choi Williams

<sup>15</sup> Distribution. Two different frequency hopping low probability of intercept radar signals were

<sup>16</sup> analyzed (4-component and 8-component). The following metrics were used for evaluation:

17 percent error of: carrier frequency, modulation bandwidth, modulation period, and

18 time-frequency localization. Also used were: percent detection, lowest signalto- noise ratio for

<sup>19</sup> signal detection, and plot (processing) time. Experimental results demonstrate that overall,

 $_{20}$  the Wigner Ville Distribution produced more accurate characterization metrics than the Choi

21 Williams Distribution. An improvement in performance could potentially translate into saved 22 equipment and lives.

23

24 Index terms—

#### <sup>25</sup> 1 Introduction

low probability of intercept (LPI) radar that uses frequency hopping techniques changes the transmitting 26 frequency in time over a wide bandwidth in order to prevent an intercept receiver from intercepting the waveform. 27 The frequency slots used are chosen from a frequency hopping sequence, and this unknown sequence gives the 28 radar the advantage over the intercept receiver in terms of processing gain. The frequency sequence appears 29 random to the intercept receiver, therefore the possibility of it following the changes in frequency is remote 30 [PAC09]. This A prevents a jammer from jamming the transmitted frequency ??ADA04]. Frequency hopping 31 radar performance depends only slightly on the code used, given that certain properties are met. This allows for 32 33 a larger assortment of codes, making it more difficult to intercept.

34 Time-frequency signal analysis includes the analysis and processing of signals with time-varying frequency 35 content. These signals are best represented by a time-frequency distribution [PAP94], [HAN00], which displays how the energy of the signal is distributed over the two-dimensional time-frequency plane [WEI03], [LIX08], 36 ??OZD03]. Processing of the signal may then exploit the features produced by the concentration of signal energy 37 in two dimensions (time and frequency), vice one dimension (time or frequency) [BOA03], ??LIY03]. Since noise 38 has a tendency to spread out evenly over the time-frequency domain, while signals tend to concentrate their 39 energies within limited time intervals and frequency bands; the local SNR of a noisy signal can be improved 40 by using time-frequency analysis [XIA99]. In addition, the intercept receiver can increase its processing gain 41

42 by implementing timefrequency signal analysis [GUL08]. Time-frequency distributions can be beneficial for the

- visual interpretation of signal dynamics [RAN01]. An experienced operator may be better able to detect a signal
- and extract its parameters by examining the timefrequency distribution [ANJ09].

## <sup>45</sup> 2 a) Wigner Ville Distribution (WVD)

46 One of the most prominent members of the time-frequency analysis techniques family is the WVD. The WVD

- satisfies a large number of desirable mathematical properties. In particular, it is always realvalued, preserves
  time and frequency shifts, and satisfies marginal properties The WVD of a signal ??(??) is given in equation (1)

 50
 or equivalently in equation (2) as:?? ?? (??, δ ??"δ ??") = ? ??(δ ??"δ ??" + ?? 2 +? ?? )?? \* ?δ ??"δ ??" ?

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 ?? 2 ? ?? ??????? ???? b) Choi Williams Distribution (CWD)

The CWD is a member of the Cohen's class of time-frequency distributions which use smoothing kernels [GUL07] to help reduce cross-term interference so prevalent in the WVD [BOA03], [PAC09], [UPP08]. The reduction in cross-term interference can make the time-frequency representation more readable and can make signal detection and parameter extraction more accurate. The down-side is that the CWD, like all members of Cohen's class, is faced with an inevitable trade-off between cross-term reduction and timefrequency localization. Because of this, the signal detection and parameter extraction benefits gained by the cross-term reduction may

- <sup>58</sup> be offset by the decrease in time-frequency localization (smearing or widening of the signal).
- The CWD of a signal ??(??) is given in equation (3) as:

Low Probability of Intercept Frequency Hopping Signal Characterization Comparison Using the Wigner Ville Distribution and the Choi Williams Distribution???? ?? (??, ð ??"ð ??") = ? 2 ?? ? ?? |??| +? ?? ?? ???? 2 (?????) 2 /?? 2 ?? ??? + ?? 2 ??? \* ??? ? ?? 2 ? ?? ??? 2??ð ??"? ????? ?????

As can be seen from equation (3), the CWD uses an exponential kernel in the generalized class of bilinear time-frequency distributions. Choi and Williams introduced one of the earliest 'new' distributions [CHO89], which they called the Exponential Distribution or ED.

This new distribution overcomes several drawbacks of the Spectrogram and the WVD, providing decent localization with suppressed interferences [WIL92], [GUL07], [UPP08]. Interference terms tend to lie away from the axes in the ambiguity plane, while auto terms (signals) tend to lie on the axes. The Spectrogram kernel

attenuates everything away from the (0,0) point, the WVD kernel passes everything, and the CWD kernel passes

 $_{\rm 70}$   $\,$  everything on the axes and attenuates away from the axes.

# <sup>71</sup> 3 Thus, the CWD generally attenuates interference terms <sup>72</sup> [PAC09], [HLA92].

73 This provides its reduced interference characteristic. The Spectrogram reduces interference also, but at a cost to 74 the signal concentration.

### 75 **4** II.

#### $_{76}$ 5 Methodology

The methodologies detailed in this section describe the processes involved in obtaining and comparing metrics 77 between the classical time-frequency analysis techniques of the Wigner Ville Distribution and the Choi Williams 78 79 Distribution for the detection and characterization of low probability of intercept frequency hopping radar signals. 80 The tools used for this testing were: MATLAB (version 7.12), Signal Processing Toolbox (version 6.15), Wavelet Toolbox (version 4.7), Image Processing Toolbox (version 7.2), Time -Frequency Toolbox (version 1.0). 81 Testing (which was accomplished on a desktop computer) was performed for 2 different waveforms (4 82 component frequency hopping, 8 component frequency hopping). For each waveform, parameters were chosen for 83 academic validation of signal processing techniques. Due to computer processing resources they were not meant 84 to represent real-world values. The number of computer. Testing was performed at three different SNR levels: 85 10dB, 0dB, and the lowest SNR at which the signal could be detected. The noise added was white Gaussian noise, 86 which best reflects the thermal noise present in the IF section of an intercept receiver [PAC09]. Kaiser windowing 87 was used, when windowing was applicable. 50 runs were performed for each test, for statistical purposes. The 88 plots included in this paper samples for each test was chosen to be 512, which seemed to be the optimum size for 89 90 the desktop were done at a threshold of 5% of the maximum intensity and were linear scale (not dB) of analytic 91 Task 1 consisted of analyzing a frequency hopping (prevalent in the LPI arena [AMS09]) 4component signal 92 whose parameters were: sampling frequency=5KHz; carrier frequencies=1KHz, 1.75KHz, 0.75KHz, 1.25KHz; 93 modulation bandwidth=1KHz; modulation period=.025sec.

Task 2 was similar to Task 1, but for a frequency hopping 8-component signal, whose parameters were: sampling frequency=5KHz; carrier frequencies= 1.5KHz, 1KHz, 1.25KHz, 1.5KHz, 1.75KHz, 1.25KHz, 0.75KHz, 1KHz; modulation bandwidth=1KHz; modulation period=.0125sec.

97 After each particular run of each test, metrics were extracted from the time-frequency representation. The

98 different metrics extracted were as follows: 1) Plot (processing) time: Time required for plot to be displayed.

Threshold percentages were determined based on visual detections of low SNR signals (lowest SNR at which 99 the signal could be visually detected in the timefrequency representation) (see Figure ??). Year 2018 F Figure ??: 100 Threshold percentage determination. This plot is an amplitude vs. time (x-z view) of the CWD of a 4component 101 frequency hopping signal (512 samples, SNR= -2dB). For visually detected low SNR plots (like this one), the 102 percent of max intensity for the peak z-value of each of the signal components was noted (here 98%, 78%, 81%, 103 70%), and the lowest of these 4 values was recorded (70%). Ten test runs were performed for this timefrequency 104 analysis tool (CWD) for this waveform. The average of these recorded low values was determined and then 105 assigned as the threshold for that particular time-frequency analysis tool. Note -the threshold for the CWD is 106 70%. 107

Thresholds were assigned as follows: CWD (70%); WVD (4 component FSK) (50%); WVD -(8-component FSK) (20%) .

For percent detection determination, these threshold values were included in the time-frequency plot algorithms so that the thresholds could be applied automatically during the plotting process. From the threshold plot, the signal was declared a detection if any portion of each of the signal components was visible (see Figure 2). max intensity values for these test runs was 20%. This was adopted as the threshold value, and is representative of what is obtained when performing manual measurements. This 20% threshold was also adapted for determining the modulation period and the time-frequency localization (both are described below).

116 For modulation bandwidth determination, the 20% threshold value was included in the time-frequency plot 117 algorithms so that the threshold could be applied automatically during the plotting process. From the threshold plot, the modulation bandwidth was manually measured (see Figure 4). For lowest detectable SNR determination, 118 these threshold values were included in the time-frequency plot algorithms so that the thresholds could be applied 119 automatically during the plotting process. From the threshold plot, the signal was declared a detection if any 120 portion of each of the signal components was visible. The lowest SNR level for which the signal was declared a 121 detection is the lowest detectable SNR (see Figure 7). ) with threshold value automatically set to 70%. From this 122 threshold plot, the signal was declared a (visual) detection because at least a portion of each of the 4 frequency 123 hopping signal components was visible. Note that the signal portion for the 73% max intensity and the 72% max 124 intensity (just below the 'n' in 'intensity' for each case) is barely visible because the threshold for the CWD is 125 70%. For this case, just a slightly lower SNR would have been a non-detect. Compare to Figure 2, which is the 126 same plot, except that it has an SNR level equal to 10dB. 127

The data from all 50 runs for each test was used to produce the actual, error, and percent error for each of these metrics listed above.

The metrics from the WVD were then compared to the metrics from the CWD. By and large, the WVD outperformed the CWD, as will be shown in the results section.

#### <sup>132</sup> 6 III.

#### 133 7 Results

Table 1 presents the overall test metrics for the two classical time-frequency analysis techniques used in this testing (WVD versus CWD).

From Table 1, the WVD outperformed the CWD in average percent error: carrier frequency (0.19% vs. 0.62%), modulation bandwidth (5.97% vs. 17.92%), modulation period (17.01% vs. 17.05%), and timefrequency localization (y-direction) (2.04% vs.

#### 139 8 Discussion

140 This section will elaborate on the results from the previous section.

From Table 1, the WVD outperformed the CWD in average percent error: carrier frequency (0.19% vs. 0.62%), modulation bandwidth (5.97% vs. 17.92%), and modulation period (17.01% vs. 17.05%) -and in average: timefrequency localization-y (as a percent of y-axis) (2.04% vs. 6.78%) and percent detection (90.7% vs. 88.7%). These results are by and large a result of the Year 2018 F WVD signal being much more localized signal than the CWD signal. The CWD's 'thicker' signal is a result of its cross-term reduction -at the expense of signal

localization.
The CWD outperformed the WVD in average: plot time (10.16s vs. 6382s) and lowest detectable SNR (-2.2db
vs. -2.0db). The combination of the CWD's reduction of cross-term interference along with the WVD being very
computationally complex [MIL02] are the grounds for the CWD's better plot time. In addition, lowest detectable
SNR is based on visual detection in the Time-Frequency representation. Figures 8 and 9 show that, for the WVD
plots, as the SNR gets lower, it gets more difficult to distinguish between the actual signals and the cross-term

interference. However, for the CWD plots there is no cross-term interference to confuse with the actual signals, making the CWD signals, though not as localized, easier to detect than the WVD signals-at these lower SNRs.

- The WVD might be used in a scenario where you need good signal localization in a fairly low SNR environment, without tight time constraints. The CWD might be used in a scenario where a short plot time is necessary, and where signal localization is not an issue. Such a scenario might be a 'quick and dirty' check to see if a signal is
- 157 present, without precise extraction of its parameters.

158

V.

### 159 9 Conclusions

Digital intercept receivers, whose main job is to detect and extract parameters from low probability of intercept 160 radar signals, are currently moving away from Fourier-based analysis and towards classical timefrequency analysis 161 techniques, such as the WVD and the CWD, for the purpose of analyzing low probability of intercept radar signals. 162 Based on the research performed for this paper (the novel direct comparison of the WVD versus the CWD for 163 the signal analysis of low probability of intercept frequency hopping radar signals) it was shown that the WVD 164 by and large outperformed the CWD for analyzing these low probability of intercept radar signals -for reasons 165 brought out in the discussion section above. More accurate characterization metrics could well translate into 166 saved equipment and lives. 167

<sup>168</sup> Future plans include analysis of an additional low probability of intercept radar waveform (triangular modulated FMCW), again using the WVD and the CWD as time-frequency analysis techniques.



Figure 1:



Figure 2: 2)

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Figure 3: Figure 2 :

 $\mathbf{2}$ 



Figure 4: Figure 3 :



20% threshold of max intensity CWD FSK 4-component fs=5KHz fc=1KHz, 1.75Khz, 75Khz, 1.25KHz modBW=1KHz modper=.025sec #samples=512 SNR=10dB

Figure 5: F



Figure 6: Figure 4 :



Figure 7: Figure 5 :F



Figure 8: Figure 6 :



Figure 9: Figure 7 :



Figure 10: Figure 8



CWD FSK 4-component fs=5KHz fc=1KHz, 1.75KHz, 75KHz, 1.25KHz modBW=1KHz modper=.025sec #samples=512 SNR=0dB

Figure 11: Figure 8 :

correlating the signal with a time and frequency translated version of itself, making it bilinear. The WVD exhibits the highest signal energy concentration in the time-frequency plane [WIL06]. By using the WVD, an intercept receiver can come close to having a processing gain near the LPI radar's matched filter processing gain [PAC09]. The WVD also contains cross term interference between every pair of signal components, which may limit its applications [GUL07], [STE96], and which can make the WVD time-frequency representation hard to read, especially if the components are numerous or close to each other, and the more so in the presence of noise [BOA03]. This lack of readability can in turn translate into decreased signal detection and parameter extraction metrics, potentially placing the intercept receiver signal analyst in harm's way. Experimental results demonstrate that overall, the Wigner Ville

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Distribution produced more accurate characterization metrics than the Choi Williams Distribution. An improvement in performance could potentially translate into saved equipment and lives.

Figure 12:

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[Note: 6.78%); and in average: percent detection (90.7% vs. 88.7%), while the CWD outperformed the WVD in lowest detectable SNR (-2.2db vs. -2.0db) and average plot time (10.16s vs. 6382s).]

Figure 13: Table 1 :

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