However, this technology is currently in beta. Therefore, kindly ignore odd layouts, missed formulae, text, tables, or figures.

On the Squeezing Flow of Nanofluid Through a Porous Medium With Slip Boundary and Magnetic Field: A Comparative Study of Three Approximate Analytical Methods M. G. Sobamowo¹ ¹ University of Lagos

Received: 7 December 2016 Accepted: 31 December 2016 Published: 15 January 2017

8 Abstract

6

This paper presents a comparative study of approximate analytical methods is carried out using differential transformation, homotopy perturbation and variation parameter methods for 10 the analysis of a steady two-dimensional axisymmetric flow of nanofluid under the influence of 11 a uniform transverse magnetic field with slip boundary condition. Also, parametric studies are 12 carried out to investigate the effects of fluid properties, magnetic field and slip parameters on 13 the squeezing flow. It is revealed from the results that the velocity of the fluid increases with 14 increase in the magnetic parameter under the influence of slip condition while an opposite 15 trend is recorded during no-slip condition. Also, the velocity of the fluid increases as the slip 16 parameter increases but it decreases with increase in the magnetic field parameter and 17 Reynold number under the no-slip condition. The approximate analytical solutions are 18 verified by comparing the results of the approximate analytical methods with the numerical 19 method using Runge-Kutta coupled with shooting method. Although, very good agreements 20 are established between the results, the results of variation parameter method provide 21

²² excellent agreement with the results of numerical method.

23

Index terms— nanofluid; squeezing flow; slip boundary; differential transformation method; homotopy perturbation method; variation parameter method.

26 1 Introduction

he flow of nanofluid in a channel, between two contracting or expanding plates and also, over a stretching sheet 27 have aroused research interests in recent times. Among the recent studies, the analysis of squeezing flow of 28 nanofluid or viscous fluid between two parallel plates have increased tremendously due to its various industrial 29 and biological applications. After the pioneer work on squeezing flow by Stefan [1], there have been improved 30 works on the flow phenomena. However, the earlier studies [1][2][3] on squeezing flow were based on Reynolds 31 equation. Jackson [4] and Usha and Sridhar an [5] pointed out the insufficiencies of the Reynolds equation for 32 33 some cases of flow situations. Consequently, there have been several attempts and renewed research interests 34 by different researchers to properly analyze and understand the squeezing flows using different analytical and 35 numerical methods. Also, effects of magnetic field, flow characteristics and fluid properties on the squeezing flow have been widely investigated under no slip conditions [27][28][29][30][31][32][33][34][35][36][37][38][39][40][41][42]. 36 However, in many cases of fluid and flow problems such as polymeric liquids, thin film problems, nanofluids, 37 rarefied fluid problems, fluids containing concentrated suspensions, and flow on multiple interfaces, slip condition 38 prevails at the boundary of the flow process. 39

Therefore, Navier [43] proposed the general boundary condition which demonstrates the fluid slip at the surface. Such consideration of slip condition in the flow analysis of fluids is of great importance especially when

3 III. APPROXIMATE ANALYTICAL METHODS OF SOLUTION: DIFFERENTIAL TRANSFORM METHOD

42 fluids with elastic character are under consideration [44]. In a past study on slip effects on flow conditions of fluids, Ebaid [45] investigated the effects of magnetic field and wall slip conditions on the peristaltic transport in 43 an asymmetric channel. The influence of slip on the peristaltic motion of third-order fluid in asymmetric channel 44 are analyzed by Harat et al. [46]. Also, Harat and Abelman [47] presented a study on the effects of align and division.

45 was analyzed by Hayat et al. [46]. Also, Hayat and Abelman [47] presented a study on the effects of slip condition 46 on the rotating flow of a third grade fluid in a nonporous medium. Abelman et al. [48] extended their work to a

on the rotating flow of a third grade fluid in a nonporous medium. Abelman et al. [48] extended their work to a
porous medium and obtained the numerical solutions for the steady magnetodrodynamics flow of a third grade
fluid in a rotating frame.

The past efforts in analyzing the squeezing flow problems have been largely based on the applications of various 49 numerical and approximate analytical methods such as differential transformation method (DTM), Adomian 50 Decomposition Method (ADM), homotopy analysis method (HAM), optimal homotopy asymptotic method 51 (OHPM), variational iteration method (VIM). Moreover, most of the studies are based on viscous fluids. To the 52 best of the authors' knowledge, a Approximate Analytical Methods study on squeezing flow of nanofluid under 53 the influences of magnetic field and slip boundary conditions using variation parameter method (VPM) has not 54 been carried out in literature. Also, a comparative study of the three approximate analytical methods (differential 55 transformation, homotopy perturbation and variation parameter methods) has presented in this paper has not 56 57 been analyzed in past work. Therefore, in the paper, a comparative study of approximate analytical methods 58 is carried out using differential transformation, homotopy perturbation and variation parameter method for the 59 analysis of a steady twodimensional axisymmetric flow of nanofluid under the influence of a uniform transverse magnetic field with slip boundary condition. The analytical solutions are used to investigate the effects of fluid 60 properties, magnetic field and slip parameters on the squeezing flow. 61

62 II.

63 2 Problem Formulation

⁶⁴ Consider a squeezing flow of nanofluid squeezed between two parallel plates which are at distance 2h apart and ⁶⁵ they approach each other with slowly with a constant velocity under in the presence of a magnetic field as shown ⁶⁶ in Fig. 1. Assuming that the fluid is incompressible, the flow is laminar and isothermal, the governing equations ⁶⁷ of motion for the quasi steady flow of the nanofluid are given as: . 0v ? = ? (1) () () () 2 2 0 2.5 1 1 . 1 .

⁷² Introducing the stream function (), r z ? , vorticity function () , r z ?

And the slip boundary conditions as()()()()()", "00,00, 2 f f v f h f h f h? = = = =(10)

Using the following dimensionless parameters in Eq. (11)() 2 * * 2 0 B 1, , = / 2 f f nf Hv f z F z R G h a m v h k ? ? $\mu \mu$? ? = = + + ? ? ? ? ? ? . (11)

And the dimensionless boundary conditions in Eq. (10) as()()()()() 0 0, 0 0 1 1, 11F F F F ? ?? = ??? = (13)

where the asterisk, * has been omitted in Eqs. (12) and Eq. (??3) for the sake of conveniences.

⁹¹ 3 III. Approximate Analytical Methods Of Solution: Differen ⁹² tial Transform Method

The differential transform method has widely been used to solve both singular and non-singular perturbed boundary values problems. It gives analytical solution to differential or integral solutions in the form of a polynomial by transforming each term in the differential equation or integral into a recursive form or relation of the equation which follows an iterative procedure for obtaining analytical series solutions of differential equation. The basic definitions of the method is as follows:

98 If () u x is analytic in the domain T, then it will be differentiated continuously with respect to space x.

() (,) p p d u x x p dx ? = for all x T ? (17) () () (,) i p i p x x d u x U p x p dt ? = ? ? = = ? ? ? ? (18)
where p U is called the spectrum of () u() () () ! p i p x x u x U p p ? ? ? ? = ? ? ? ? ? ?(19)

where Eq. (19) is called the inverse of) (k U using the symbol 'D' denoting the differential transformation process and combining Eq. (18) and Eq. (19), it is obtained that ()10()()()! p i p x x u x U p D U p p? ? = ??? = = ????? (20)

a) Operational properties of differential transformation method If () () u x and v x are two independent 104 functions with space (x) where () U p and () V p are the transformed function corresponding to () u x and () v 105 x , then it can be shown from the fundamental mathematics operations performed by differential transformation 106 that.i. If () () (), $z x u x v x = \pm$ then () () () p U p V p? = \pm ii. If () (), z x u x? = then () () Z p U107 p? = iii. If () (), n n d u x z x dx = then () (1) (2)(3)...() () p p p p p n U p n? = + + + + iv. If () 108 ()(), z x u x v x = then 0()()() p r p V r U p r = ? = ? ? v. If ()() m z x u x = , then 1 0()() p r p V r U p r = ? = ? ? v. If ()() m z x u x = , then 1 0() () () p r p V r U p r = ? = ? ? v. If ()() m z x u x = , then 1 0() () () p r p V r U p r = ? = ? ? v. If ()() m z x u x = , then 1 0() () () p r p V r U p r = ? = ? ? v. If ()() m z x u x = , then 1 0() () () p r p V r U p r = ? = ? ? v. If ()() m z x u x = , then 1 0() () () p r p V r U p r = ? = ? ? v. If ()() m z x u x = , then 1 0() () () p r p V r U p r = ? = ? ? v. If ()() m z x u x = , then 1 0() () () p r p V r U p r = ? = ? ? v. If ()() m z x u x = , then 1 0() () () p r p V r U p r = ? = ? ? v. If ()() m z x u x = , then 1 0() () () p r p V r U p r = ? = ? ? v. If ()() m z x u x = , then 1 0() () () p r p V r U p r = ? = ? ? v. If ()() m z x u x = , then 1 0() () () p r p V r U p r = ? = ? ? v. If ()() m z x u x = , then 1 0() () () p r p V r U p r = ? = ? ? v. If ()() m z x u x = , then 1 0() () () p r p V r U p r = ? = ? ? v. If ()() m z x u x = , then 1 0() () () p r p V r U p r = ? = ? ? v. If ()() m z x u x = , then 1 0() () () p r p V r U p r = ? = ? ? v. If ()() m z x u x = , then 1 0() () () p r p V r U p r = ? = ? ? v. If ()() m z x u x = , then 1 0() () () p r p V r U p r = ? = ? ? v. If ()() m z x u x = , then 1 0() () () p r p V r U p r = ? = ? ? v. If () () m z x u x = , then 1 0() () () p r p V r u p r = ? = ? ? v. If () () m z x u x = , then 1 0() () () () p r p V r u p r = ? = ? ? v. If () () m z x u x = , then 1 0() () () () p r p V r u p r = ? = ? v. If () () m z x u x = , then 1 0() () () () p r p V r u p r = ? = ? v. If () () m z x u x = , then 1 0() () () () p r p V r u p r = ? = ? v. If () () m z x u x = , then 1 0() () () () p r p V r u p r = ? e ? v. If () () m z x u x = , then 1 0() () () () p r p V r u p r = ? e ? v. If () () m z x u x = , then 1 0() () () () () p r p V r u p r = ? e ? v. If () () m z x u x = , then 1 0() () () () () p r p V r u p r = ? e ? v. If () () m z x u x = , then 1 0() () () () () p r p V r u p 109 m r p U r U p r ? = ? = ? ? vi. If () () (), z x u x v x = then 0 () (1) (1) () p r p r V r U p r = ? = + + 110 ? ? vii. If () () , n m n d u x z x x dx = then ()()() () () 0 () 1 1 2 3 ... p l p l m p l p l p l p l n U p l n 111 ? = ? = ? ? ? + ? + ? + ? + ? + ? + ? viii. If 3 3 () ()) () , d u x d u x z x dx dx = then ()()()() () 0 () 1 112 2 3 3 p l Z p U p l l l l U l = ? + + + ? ix. If 2 2 () ()) (), d u x d u x z x dx dx = then () ()()() ()113 0 () 1 1 1 2 2 p l Z p p l U p l l l U l = ? + ? + + + + ? x. If 2 () () du x z x dx ? ? = ? ? ? ? then () (114)()() 0() 1 1 1 1 p l Z p p l U p l l U l = ? + ? + + + ? xi. If ()(), du x z x u dx = then ()()()() 0() 115 1 1 p 1 Z p U p 1 1 U 1 = ? + + ? If 2 2 2 ()) (), d u x z x dx ? ? = ? ? ? ? then ()() () () () () 0 () 1 2116 117 2.5 1 2 3 4 4 3 2 1 3 2 2 0 1 1 1 k l s f k k k k F k R k l k l k l F l F k l G k k F k ? ? ? ? ? ? = + + + + ? ? 118 119

With differential transformed boundary conditions Where a and b are unknowns to be determined later using 120 the boundary conditions of Eq. (16b).[][][][]0 0, 1, 20, 3, FF a FF b = = = ???? (22) (1) [1] (121 1)(2)[2] k F k k k F k ? + + = + + + ? ? [] 0 4 F = ? [] () () 2.5 2 1 5 20 1 1 s f F bG abR ? ? ? ? ? ? ?? 122 123 124 125 126 127 128 129

Using Eqs. (21) and (??2), the value of (), 1, 2,3, 4,5,... 19, 20. i i F = ? are Application of the Differential Transform Method to the Present Problem

132 133 ? 134 ? + + + ? ? ? ? ? ? ? ? ? ? ? ? ? ? ? = ? ? () () () () () () **3**1 1 1 1 5 s f s s f f a b R a bG R a b R ? ? ? ? 135 ???????????????? ?? 136 137 138 139

a) The basic idea of homotopy perturbation method In order to establish the basic idea behind homotopy perturbation method, consider a system of nonlinear differential equations given as()()0, A U f r r? =??(24) with the boundary conditions, 0, u B u r???????????????(25)

where A is a general differential operator, B is a boundary operator,

144 **4** ()

f r a known analytical function and \hat{I} ?" is the boundary of the domain ? The operator A can be divided into two parts, which are L and N, where L is a linear operator, N is a non-linear operator. Eq.(24) can be therefore rewritten as follows()()() 0 L u N u f r + ? =(26)

By the homotopy technique, a homotopy() [], : 0,1 U r p R ? × ? can be constructed, which satisfies () () () () () () [], 1 0, 0,1 H U p p L U L U p A U f r p ? = ? ? + ? = ? ? ? ? ? ? ? ? (27)

In the above Eqs. (27) and (28),[] 0,1 p? is an embedding parameter, o

u is an initial approximation of equation of Eq.(24), which satisfies the boundary conditions. Also, from Eqs. (27) and (28), we will have()()(), 00 o H U L U L U = ? = (29)()()(), 00 H U A U f r = ? = (30)

The changing process of p from zero to unity is just that of (), U r p from () o u r to ()

¹⁵⁵ u r. This is referred to homotopy in topology. Using the embedding parameter p as a small parameter, the ¹⁵⁶ solution of Eqs. (27) and (28) can be assumed to be written as a power series in p as given in Eq. (28)2.1.2 ¹⁵⁷ ... o U U pU p U = + + +(31)

158 It should be pointed out that of all the values of p between 0 and 1, p=1 produces the best result.

Therefore, setting 1 p = , results in the approximation solution of Eq.(24)1 2 1 lim ... o p u U U U U ? = = + + + (32)

161 The basic idea expressed above is a combination of homotopy and perturbation method.

162 **5** A

Hence, the method is called homotopy perturbation method (HPM), which has eliminated the limitations of the traditional perturbation methods. On the other hand, this technique can have full advantages of the traditional perturbation techniques. The series Eq.(32) is convergent for most cases.

¹⁶⁶ b) Application of the homotopy perturbation method to the ¹⁶⁷ present problem

Using the embedding parameter p as a small parameter, the solution of Eqs. (??6) can be assumed to be written as a power series in p as given in Eq. (33)2 3 1 2 3 ... o p p p F F F F F = + + + + ? ? ? ? ? (34)

173 On substituting Eqs. (34) and into Eq.(33) and expanding the equation and collecting all terms with the same 174 order of p together, the resulting equation appears in form of polynomial in p. On equating each coefficient of the resulting polynomial in p to zero, we arrived at a set of differential equations and the corresponding boundary 175 conditions as 0 0, 0 0, 1 0, () 0 0 : 0, iv p F = ? () () () () () " ' " 0 0 0 0 0 0 0 0 0 0, 1 1, 1 1 F F F F F ? = 176 177 178 179 180 FF181 182 183 184 ? 185 186 187 ???()()()()()()()()()()()()()()2.5 2.5 5 2 """ 5 4 3 0 4 0 2.5 2.5 "" 3 1 2 2 2.5 1 3 : 1 1 1 1 1 1 188 189 190 191 ??????????(40)()()()()()()""5555500,00,10,11FFFFF?====?????? 192 193 On solving the above Eqs. (35)(36)(37)(38)(39)(40), we arrived at () () (30321231zzFz??) =194 ? ? (**41**)()()()()()()()() 2.5 2.5 2 5 7 1 2 2 2.5 2 5 2 2 2 9 1 1 2 1 3 1 1 3 3 1 2 3 1 2 3 1 90 1 1 2 1 63 1 1 195 196

197 2.5 2.5 2 2 2 2.5 2 2 3 6 1 1 2 1 9 1 1 12 3 1 3 1 3 1 90 1 1 2 1 63 1 60 3 1 3 1 1 3 2 1 s s f f s s f f z R R G R R 198 199 ? 200 201 202 203 204 205 206 207

c) The Procedure of Variation Parameter Method The basic concept of VPM for solving differential equations is as follows: The general nonlinear equation is in the operator form() () () Lf Rf Nf g?? + + = (44)

The linear terms are decomposed into L + R, with L taken as the highest order derivative which is easily invertible and R as the remainder of the linear operator of order less than L. where g is the system input or the source term and u is the system output, Nu represents the nonlinear terms.

m is the order of the given differential equation, k is are the unknown constants that can be determined by initial/boundary conditions and (,)??? is the multiplier that reduces the order of the integration and can be determined with the help of Wronskian technique.

218 ()11111()(,)(1)!()!(1)!iimmmiimim???????????????????(47)

223 In the same manner, the expressions for () () () () () 2 3 45 6 , , , , ... z z z F F F F z z ? ? ? ? ?

were obtained. However, they are too large expressions to be included in this paper. Setting 1 p =, results in the approximation solution of Eq. (24)

229 The above equation can also be written as

230 7 Global

 $234 \quad ? ? ?? ?? ?? ? ? = = ? + ? + ? + ? ?? ?? ?$

- 235 Consequently, an exact solution can be obtained when n approaches infinity.
- Using the standard procedure of VPM as stated above, one can write the solution of Eq. (??5) as
- From the boundary conditions in Eq. (??6)
- 238 (0) 0, (0) 0F F?? = =

From the iterative scheme, it can easily be shown that the series solution is given as $3\ 2\ 0\ 1$ () $6\ k\ z\ F\ z\ k\ z =$

243 +(51)

Here, k 1, k 2, k 3, and k 4 are constants obtained by taking the highest order linear term of Eq. (??5) 244 and integrating it four times to get the final form of the scheme. sfsfkkRzkzGkzFzkzRkz????? 245 246 247 248 ? 249 250 251 252 ? 253 254 ? ? + Similarly, the other iterations F z F z F z F z F z F z are obtained. 255

Although, analytically, the VPM and DTM are somehow easier and straight-forward as compared to HPM, 256 there is no search for Wronskian multiplier (as carried out in VPM) or the rigour of developing recursive relations 257 or differential transforms coupled with the search for included unknown parameter that will satisfy second the 258 boundary condition lead to additional computational cost in the generation of the solution to the problem using 259 DTM. This drawback is not only peculiar to VPM and DTM, other approximate analytical methods such as 260 HAM, ADM, VIM, DJM, TAM also required additional computational cost and time for the determination 261 of included unknown parameter that will satisfy second the boundary condition. Also, the VPM and DTM 262 have their own operational restrictions that severely narrow there functioning domains as they are limited to 263 small domain. Using VPM or DTM for large or infinite domain is accompanied with either the application 264 of before-treatment techniques such as domain transformation techniques, domain truncation techniques and 265 conversion of the boundary value problems to initial value problems or the use of aftertreatment techniques 266 such as Pade-approximants, basis functions, cosine after-treatment technique, sine aftertreatment technique and 267 domain decomposition technique. This is because VPM and DTM were initially established for initial value 268 problems. Amending the methods to boundary value problems especially for large or infinite domains boundary 269 value problems leads to the inclusion of unknown parameters (that will satisfy second the boundary condition) 270 in the solution. This drawback in the other approximation analytical methods is not experienced in HPM as 271 such tasks of before-and after-treatment techniques might not necessarily be required in HPM. This is because 272 HPM is easily applied to the boundary value problems without any included unknown parameter in the solution 273 as found in VPM and DTM. In order to get an insight into the problem, the effects of pertinent flow, magnetic 274 field and slip parameters on the velocity profile of the fluid are investigated. Fig. 2 and 4 shows the effects of 275 magnetic field and porous parameter on the velocity of the fluid under the influence of slip condition, while Fig. 276 277 3 and 5 depicts the influence of the porous and magnetic on the velocity of the fluid under no-slip condition. It 278 could be inferred from the figures that the velocity of the fluid increases with increase in the porous-magnetic 279 parameter under slip condition while an opposite trend was recorded during no-slip condition as the velocity of 280 the fluid decreases with increase in the porous-magnetic parameter under the no slip condition. Fig. ?? shows the influence of the slip parameter ?? on the fluid velocity. By increasing ??, it is observed that the velocity of 281 the fluid increases. Fig. 7 presents the effects of Reynold's number on the velocity of the fluid. It is observed 282 from the figure that by increasing the value R, the velocity of the fluid decreases. 283

VI. 8 284

Conclusion 9 285

In this work, a comparative study of three approximate analytical methods have been carried out for the analysis 286 of two-dimensional axisymmetric flow of an incompressible viscous fluid through porous medium under the 287 influence of a uniform transverse magnetic field with slip boundary condition. From the analysis, it is established 288 that VPM give higher accurate results than DTM and HPM with faster rate of convergence. Also, from the 289 parametric study, it was established from the results that, the velocity of the fluid increases with increase in 290 the porous-magnetic parameter under slip condition while the velocity of the fluid decreases with increase in 291 the porous-magnetic parameter under no slip condition. By increasing the slip parameter, the velocity of the 292 fluid increases, and the fluid velocity decreases as the Reynolds number increases. The approximate analytical 293 solutions have been verified by comparing the results of the approximate analytical method with the numerical 294 method using Runge-Kutta coupled with shooting method ^{1 2 3 4}



Figure 1:

On the Squeezing Flow of Nanofluid Through Porous Medium With Slip Boundary and Magneti Field: A Comparative Study of Three Approximate Analytical Methods Year 2017 For belongs to the set of non-negative integers, denoted as i x = xGlobal , then (,)(,) ix p x p?? = , where p the p-domain. Therefore Journal Eq. (17) can be rewritten as Engineering

 $i \ge x = i$ If () u x can be expressed by Taylor's series, the () u x can be represented as

) Volume XVII Issue VI Version I A of Researches in

Figure 2:

() Volume XVII Issue VI Version I A Researches in Engineering

Figure 3:



Year 2017 68 I Journal of Researches in Engineering () Volume XVII Issue VI Version A Global



9 CONCLUSION

 $^{^{1}}T \otimes 2017$ Global Journals Inc. (US)

 $^{^{2}(6)}$ where © 2017 Global Journals Inc. (US)

 $^{^3 \}odot$ 2017 Global Journals Inc. (US)

⁴On the Squeezing Flow of Nanofluid Through Porous Medium With Slip Boundary and Magneti Field: A Comparative Study of Three Approximate Analytical Methods

```
... 396249600
```

()

- where the constants k 1 and k 2 are determined using the boundary conditions in Eq. (??6) i.e.
- 297
- The equations are solved for the corresponding values of k 1 and k 2 for the different values of ?.
- 299 V.

300 .1 Results and Discussion

The above analyses show the applications of three approximate analytical methods of differential transformation, 301 homotopy perturbation and variation of parameters methods for the analysis of a steady two dimensional 302 axisymmetric flow of an incompressible viscous fluid under the influence of a uniform transverse magnetic field 303 with slip boundary condition. Using VPM and DTM, closed form series solutions are obtained as they provide 304 excellent approximations to the solution of the non-linear equation with higher accuracy than HPM. Also, the 305 VPM and DTM shows to more convenient for engineering calculations compared to HPM as they appear more 306 appealing than the HPM. However, higher accuracy and high rate of convergence was recorded in VPM than 307 DTM as shown the table, the solution of VPM is used to carry out the parametric study shown in Figs. ??-7. 308

- [Hayat and Abelman ()] 'A numerical study of the influence of slip boundary condition on rotating flow'. T Hayat , S Abelman . International Journal of Computational Fluid Dynamics 2007. 21 (1) p. .
- 311 [Jackson ()] 'A study of squeezing flow'. J D Jackson . Appl. Sci. Res. A 1962. 11 p. .
- [Rhooades et al. ()] 'Abrasive flow machining of cylinder heads and its positive effects on performance and cost
 characteristics'. L J Rhooades , R Resnic , T O' Bradovich , S Stegman . *Tech. Rep* 1996.
- [Hamdam and Baron ()] 'Analysis of squeezing flow of dusty fluids'. M Hamdam , R M Baron . Applied Science
 Research 1992. (49) p. .
- [Hamdan and Baron ()] 'Analysis of the squeezing flow of dusty fluids'. M H Hamdan , R M Baron . Appl. Sci.
 Res 1992. 49 p. .
- [Rashidi et al. ()] 'Analytic approximate solutions for unsteady two dimensional and axisymmetric squeezing
 flows between parallel plates'. M M Rashidi , H Shahmohamadi , S Dinarv . Mathematical Problems in
 Engineering 2008. 2008. p. .
- [Ullah et al. ()] 'Analytical Analysis of Squeezing Flow in Porous Medium with MHD Effect'. A Ullah , M T
 Rahim , H Khan , M Qayyum . U.P.B. Sci. Bull., Series A 2016. 78 (2) .
- IIslam et al. ()] 'Anaxisymmetric squeezing fluid flow between the two infinite parallel plates in a porous medium
 channel'. S Islam , H Khan , I A Shah , G Zaman . ID 349803. Mathematical Problems in Engineer-ing, 2011.
 2011 p. 10.
- [Domairry and Aziz ()] 'Approximate analysis of MHD squeeze flow between two parallel disk with suction or
 injection by homotopy perturbation method'. G Domairry , A Aziz . Mathematical Problem in Engineering
 2009. 2009. p. .
- [Usha and Sridharan ()] 'Arbitrary squeezing of a viscous fluid between elliptic plates'. R Usha , R Sridharan ,
 R . Fluid Dyn. Res 1996. 18 p. .
- [Birkh ()] G Birkh . Hydrodynamics, a Study in Logic, Fact and Similitude, 1960. Princeton University Press.
 137. (Revised ed)
- [Hatami and Jing] 'Differential Transformation Method for Newtonian and non-Newtonian nanofluids flow
 analysis: Compared to numerical solution'. M Hatami , D Jing . Alexandria Engineering Journal (55) p.
 .
- [Ebaid ()] 'Effects of magnetic field and wall slip conditions on the peristaltic transport of a Newtonian fluid in
 an asymmetric channel'. A Ebaid . Physics Letters A 2008. 372 (24) p. .
- [Le Roux ()] 'Existence and uniqueness of the flow of second grade fluids with slip boundary conditions'. C Le
 Roux . Archive for Rational Mechanics and Analysis, 1999. 148 p. .
- 340 [Kuzma ()] 'Fluid inertia effects in squeeze films'. D C Kuzma . Appl. Sci. Res 1968. 18 p. .
- [Kamiyama ()] 'Inertia Effects in MHD hydrostatic thrust bearing'. S Kamiyama . Transacti ons ASME, 1969.
 91 p. .
- [Tichy and Winer ()] 'Inertial considerations in parallel circular squeeze film bearings'. J A Tichy , W O Winer
 J. Lubr. Technol 1970. 92 p. .
- [Archibald ()] 'Load capacity and time relations for squeeze films'. F R Archibald , FR . J. Lubr. Technol 1956.
 78 p. .
- ³⁴⁷ [Hughes and Elco ()] 'Magneto hydrodynamic lubrication flow between parallel rotating disks'. W F Hughes , R
 ³⁴⁸ A Elco . Journal of Fluid Mechanics 1962. 13 p. .
- [Hamza ()] 'Magneto hydrodynamic squeeze film'. E A Hamza . Journal of Tribol ogy 1988. 110 (2) p. .

[Ahmed et al. ()] 'MHD Flow of a Dusty Incompressible Fluid between Dilating and Squeezing Porous Walls'. N

Ahmed , U Khan , Z A Zaidi , S U Jan , A Waheed , S T Mohyud-Din . Journal of Porous Media 2014. 17
 (10) p. .

- [Hayat et al. ()] 'MHD squeezing flow of second grade fluid between parallel disks'. T Hayat , A Yousaf , M
 Mustafa , S Obadiat . International Journal of Numerical Methods 2011. (69) p. .
- [Qayyum et al. ()] 'Modeling and Analysis of Unsteady Axisymmetric Squeezing Fluid Flow through Porous
 Medium Channel with Slip Boundary'. M Qayyum , H Khan , M T Rahim , I Ullah , ; H Khan . Behavioral
 Study of Unsteady Squeezing Flow through Porous Medium, 2015 25. 2016. 10 p. . (PLoS ONE)
- 358 [Ahmed et al. ()] 'Mohyud-Din. Magneto hydrodynamic (MHD) squeezing flow of a Casson fluid between parallel
- disks'. N Ahmed, U Khan, X J Yang, S I U Khan, Z A Zaidi, ST. Int. J. Phys. Sci 2013. 8 (36) p. .
- [Khan et al. ()] 'Mohyud-Din. MHD squeezing flow between two infinite plates'. U Khan , N Ahmed , Z A Zaidi
 M Asadullah , ST . Ain Shams Eng. J 2014b. 5 p. .
- [Khan et al. ()] 'Mohyud-Din. On unsteady twodimensional and axisymmetric squeezing flow between parallel
 plates'. U Khan , N Ahmed , S I U Khan , Z A Zaidi , X J Yang , ST . Alexandria Eng. J 2014 a. 53 p. .
- [Mohyud-Din and Khan ()] 'Nonlinear radiation effects on squeezing flow of a Cass on fluid between parallel
 disks'. S T Mohyud-Din , S I Khan . Aerospace Science & Technology 2016. Elsevier. 48 p. .
- [Mohyud-Din et al. ()] 'On heat and mass transfer analysis for the flow of a nanofluid between rotating parallel plates'. S T Mohyud-Din , Z A Zaidi , U Khan , N Ahmed . Aerospace Science and Technology 2014. 46 p. .
- ³⁶⁸ [Mustafa et al. ()] 'On heat and mass transfer in the unsteady squeezing flow between parallel plates'. M Mustafa
- 369 , S Hayat , Obaidat . *Mechanica* 2012. (47) p. .
- [Duwairi et al. ()] 'On heat transfer effects of a viscous fluid squeezed and extruded between parallel plates'. H
 M Duwairi , B Tashtoush , R A Domesh . *Heat Mass Transfer* 2004. (14) p. .
- [Reynolds ()] 'On the theory of lubrication and its application to Mr Beauchamp Tower's experiments, including an experimental determination of the viscosity of olive oil'. O Reynolds . *Philos. Trans. Royal Soc. London*
- an experimental determination of the viscosity of olive oil'. O Reynolds . *Philos. Trans. Royal Soc. London* 1886. 177 p. .
- [Nhan ()] 'Squeeze flow of a viscoelastic solid'. P T Nhan . J. Non-Newtonian Fluid Mech 2000. 95 p. .
- [Mahmood et al.] 'Squeezed flow and heat transfer over a porous surface for viscous fluid'. M Mahmood , S
 Assghar , M A Hossain . *Heat and mass Transfer* (44) p. .
- [Qayyum et al. ()] 'Squeezing flow of non-Newtonian second grade fluids and micro polar models'. A Qayyum ,
 M Awais , A Alsaedi , T Hayat . *Chinese Physics Letters* 2012. (29) p. 34701.
- [Grimm ()] 'Squeezing flows of Newtonian liquid films an analysis including fluid inertia'. R J Grimm . Applied
 Scientific Research 1976. 32 (2) p. .
- [Grimm ()] 'Squeezing flows of Newtonian liquid films: an analysis include the fluid inertia'. R J Grimm . Appl.
 Sci. Res 1976. 32 (2) p. .
- [Wang and Watson ()] 'Squeezing of a viscous fluid between elliptic plates'. C Y Wang , L T Watson . Appl. Sci.
 Res 1979. 35 p. .
- [Abelman et al. ()] 'Steady MHD flow of a third grade fluid in a rotating frame and porous space'. S Abelman ,
 E Momoniat , T Hayat . Nonlinear Analysis: Real World Applications 2009. 10 (6) p. .
- [Navier ()] Sur les lois de l' equilibre et du movement des corps solides elastiques, C.-L.-M.-H Navier . 1823. p. .
 (Bulletin des Sciences par la Societe Philomatique de Paris)
- [Hayat et al. ()] 'The influence of slip on the peristaltic motion of third order fluid in an asymmetric channel'. T
 Hayat , M U Qureshi , N Ali . *Physics Letters A* 2008. 372 p. .
- [Acharya et al.] 'The squeezing flow of Cu-water and Cu-kerosene nanofluid between two parallel plates'. N
 Acharya , K Das , P K Kundu . Alexandria Engineering Journal (55) p. .
- [Wang ()] 'The squeezing of fluid between two plates'. C Y Wang . J. Appl. Mech 1976. 43 (4) p. .
- ³⁹⁵ [Wolfe and Yang ()] 'Unsteady laminar boundary layers in an incom-pressible stagnation flow'. W A Wolfe , K
 ³⁹⁶ T Yang . J. Appl. Math. Trans. ASM E 1965. 1958. 14 p. . (Appl. Sci. Res.)
- ³⁹⁷ [Bhattacharyya ()] 'Unsteady MHD squeezing flow between two parallel rotating discs'. S Bhattacharyya , A .
 ³⁹⁸ Mechanics Research Communications 1997. 24 (6) p. .
- [Khan et al. ()] 'Unsteady Squeezing flow of Casson fluid between parallel plates'. U Khan , N Ahmed , S I U
 Khan , B Saima , ST . World J. Model. Simul 2014. 10 (4) p. . (Mohyud-din)
- [Khan et al. ()] 'Unsteady Squeezing Flow of Casson Fluid with Magneto hydrodynamic Effect and Passing
 through Porous Medium'. H Khan , M Qayyum , O Khan , M Ali . ID 4293721. Mathematical Problems in
 Engineering 2016. 2016 p. 14.
- 404 [Siddiqui et al. ()] 'Unsteady squeezing flow of viscous MHD fluid between parallel plates'. A M Siddiqui , S Irum
 405 , A R Ansari . Mathematical Modeling Analysis 2008. 2008. p. .
- 406 [Stefan ()] 'Versuch Über die scheinbare adhesion", Sitzungsberichte der Akademie der Wissenschaften in Wien'.
- 407 M J Stefan . *Mathematik-Naturwissen* 1874. 69 p. .