

# Numerical Studies on Centrifugal Impeller Performance with Different Lean Combinations

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## Abstract

Centrifugal compressors are designed for a given operating pressure and mass flow rate. These machines are often run at off design operating conditions depending on the requirement from industrial to Aerospace applications. The need to maintain relatively high efficiency under off design conditions with adequate stall margin makes the compressor design more challenging. These necessities demand for improvement in the flow conditions through the impeller by optimizing the vane shape. Much of the research was carried out on impeller vane shape to minimize the wake regions at impeller exit and one such effort was to introduce a blade lean at impeller inlet and exit. Investigation from the experimental studies revealed the authors that the introduction of lean at exit suppressed the wake flow regions and henceforth improved the impeller performance either with improved pressure rise or with increased stall margin. Though many of the research studies have proven the influence of lean on the change in the Centrifugal impeller performance, the study was pertained to a lean with a combination of positive inlet and exit leans or negative inlet and exit leans that has shown no change in surge margin improvement. Moreover, the study was pertained to a transonic impeller and the flow investigations are confined to two operating conditions only. Considering the authors knowledge/experience on usage of lean, our current research is aimed to investigate the performance of a subsonic impeller that has a combination of positive inlet and negative exit lean. This impeller model is further compared for performance with the other two different impeller models viz., an impeller with negative exit lean and the impeller with zero lean. All these three different lean angle combinations are focused to understand the aerodynamic performance, stability margin for steady state operation and flow behavior throughout the operating range. The performance results revealed a noticeable improvement

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*Index terms*— lean angle, stall margin, centrifugal impeller

## 1 Introduction

Centrifugal compressors are widely used in various applications viz., aviation, oil & gas, refrigeration, etc. These type of roto dynamic machines are majorly used in turboprop, turbo-shafts and auxiliary power units for air compression due to their high pressure raising capability in a single stage and their robustness in case of foreign object damage. Centrifugal compressors are capable of producing pressure ratio up to 6:1 in a single stage made of high strength metal alloys. Multistage centrifugal compressors are not preferred in aviation industry because of the huge pressure losses accompanied when compared to multistage axial flow compressors. There have been continuous efforts to improve the performance of centrifugal compressors. To begin with, the impeller design is initially constrained by selection of specific speed that predetermines the impeller characteristics. With the available design concepts viz., blade backswept/radial, impeller shroud & inducer arrangements and the use of splitter blades resulted in the centrifugal impeller advancements to be exhausted. Despite this tremendous design

## 2 NUMERICAL ANALYSIS SETUP

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42 changes identified for the best performance, the flow distribution from the impeller has always become complex  
43 and inevitable.

44 Compressor performance improvements were reported by introducing splitter blades [1,2], tandem blades  
45 [3], three-dimensional impeller design [4, 5]. Elder and Gill [6] showed that the parameters viz., inducer  
46 incidence, impeller back-sweep angle, number of impeller and diffuser vanes have the significant effect on the  
47 compressor stability limit. Hildebrandt and Genrup [7] investigated the influence of different back sweep angles  
48 and exit widths on the impeller outlet flow pattern of a centrifugal compressor with vaneless diffuser through  
49 numerical simulations. It was revealed from their studies that the impeller with increased back sweep provides  
50 more uniform flow pattern at the outlet that would provide better diffusion process in the downstream.

51 Further, Moore et al. [8] [9] investigations realized that the impeller with  $0^\circ$  lean (also, defined as Skew in  
52 some literature) at outlet realized vast secondary flow losses near shroud region than in any other interior zone.  
53 To suppress these wakes, introduced a lean concept that allows redistribution of flow and moving the high loss  
54 fluid from shroud region to hub. By incorporating a lean at the exit indirectly affects the blade angle distribution  
55 as the tangency and profile smoothness are not to be disturbed as shown in Fig [1]. A patent by Harada and Shin  
56 [10] has disclosed the lean blade techniques. He claimed that the compressor performance, including efficiency,  
57 can be improved by imparting tangential lean to the impeller blades. Based on the above findings, it reveals that  
58 the overall performance and stability margin of centrifugal compressors can be improved by introducing negative  
59 lean at the impeller blade exit. Arunachalam and Nagpurwala [11] have given better approach in understanding  
60 the positive and negative lean affect on centrifugal impeller performance.

61 Figure [1]: Blade angle distribution from hub to shroud  
62 [14]

63 Another study from, Howard et al.

64 [12] has also reported a study with the simple lean angle at impeller inlet and outlet as shown in Fig [2].  
65 The numerical results revealed a marginal improvement in impeller efficiency with reduced leakage flow at the  
66 shroud, while it lowered the impeller head rise. It was also noticed that lean angle can control the distribution  
67 of static pressure along the blade height, especially in the rear part of the cascade which not only reduces the  
68 energy losses in the impeller passage but also improves the downstream flow.

69 Based on the author's observations, impeller with negative lean identified a decent stall margin improvement  
70 compared to  $0^\circ$ . Investigations by analysts performed on a transonic impeller with positive inlet lean realized  
71 improved operating range with increased stability margin and acceptable pressure ratio while, negative inlet  
72 lean at the shroud provided the worst performance. [13] have already provided an understanding on change in  
73 the Centrifugal impeller performance, it was for a transonic inlet conditions. Moreover, the investigations so  
74 far contributed was on combination of positive lean at inlet and outlet or a negative lean at inlet and outlet  
75 with a transonic flow conditions. our current research is herewith intended to design a subsonic impeller that  
76 has combination of positive inlet lean and negative exit lean to provide enough surge margin for steady state  
77 operation throughout the operating range. Henceforth, it is proposed to develop an impeller model with the  
78 combination of  $10^\circ$  inlet positive lean and  $45^\circ$  negative lean at the blade exit. These magnitudes are based on  
79 the authors investigations performed in improving stability margin. Impeller performance with detailed flow  
80 passage investigation is carried out and compared with the other two models viz., an impeller with No lean and  
81 an impeller with exit lean.

82 An Eckardt-A type, 1976-80 [15] [16] impeller operating at a design speed 14000 rpm with a mass flow at  
83 4.52 kg/s and total pressure ratio of 1.92 is chosen as BASELINE for our current study. This impeller has  $30^\circ$   
84 backswept with  $0^\circ$  lean. To validate the tested impeller, basic sizing of an impeller is obtained by performing 2D  
85 analysis using well-known Jet-wake theory proposed by Japikse. With the basic geometry details obtained and  
86 with the available blade geometry information including blade profile and wrap angle distributions As the lean  
87 is obtained by moving the shroud section relative to the tangential direction, will not disturb the existing blade  
88 profiles and hence minor changes required to be imposed on deriving Models A and B. 13.0. It is a Commercial  
89 CFD code capable to solve 3D compressible Navier-Stokes equations using a finite volume discretization method.  
90 It uses a range of turbulent models with both logarithmic wall function and two-layer approaches to model the  
91 boundary layer. A 3D geometric model of the radial compressor stage has been developed using ANSYS Blade-  
92 Gen. Model created on Blade-Gen platform is imported into ANSYS Turbo Grid for grid generation. For the  
93 current study, a single passage impeller with 5% radial space is simulated with low solidity vaned diffuser (LSVD)  
94 configuration at the downstream. A 3Dmesh has been developed using the H-Grid and O-Grid topologies. The  
95 O-Grid provides a good mesh around the blades while rest of the passage used H-Grid. Adequate grid is developed  
96 with enough number of cells to capture the complex flow phenomena like boundary layers, flow separation, leakage  
97 flows and secondary vortices in the blade passage. Grid independence study was carried out to get the optimum  
98 grid for numerical solution to be independent of grid. Computational grid with 4, 43,000 elements were generated  
99 and the CFD simulations were performed.

## 100 2 Numerical Analysis Setup

101 After the successful grid complexion completion of every individual model, numerical analysis is planned to setup  
102 for all these configurations. The inlet of the computational domain is kept 200mm ahead of the eye of the impeller  
103 to ensure that the inlet boundary conditions are not affected by the back pressure of the impeller blade. Ambient

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104 states are defined at impeller inlet duct with zero Pascal as relative pressure and total temperature of 288 K.  
105 The fluid used for simulation here is air and assumed to be an ideal gas.

106 K-? turbulence model is preferred with "Stage" interface for rotor-stator interaction with 5% of turbulence  
107 intensity. Considering a single passage configuration, the computational domains are separated into inlet and  
108 impeller domains. The side walls of the impeller domain are specified with rotational periodicity. At the impeller  
109 solid walls, no-slip boundary condition is applied and all the solid walls are assumed to be adiabatic. The hub wall  
110 of the impeller is presumed to be moving with the rotor blade, while the upstream and downstream hub is made  
111 stationary. The impeller shroud is defined as counter-rotating that allows the relative motion between the rotating  
112 impeller. As mentioned earlier, Inlet boundary conditions with total pressure and static pressure distribution  
113 at the outlet are applied. The fluid time step is given as  $0.1/\omega$ , where  $\omega$  is the angular velocity in radian per  
114 second. Throughout the calculation the values of maximum residuals, a pressure at the outlet, eventually mass  
115 flow imbalances and efficiency were monitored. The convergence criterion is set for the maximum residuals below  
116  $10^{-4}$ . Applying the following boundary conditions, a Numerical analysis is performed by assuming the flow  
117 conditions as axisymmetric with periodic conditions imposed. Concrete solution is obtained by analyzing the  
118 flow through a single blade impeller passage for all these three models.

119 V. The other factor for the performance deviation can be due to the aerodynamic influence of Impellerdiffuser  
120 interaction. Concluding that the performance divergence between numerical model and experimental values  
121 are acceptable at the design point, the off-design performance trend was also satisfactory. After the successful  
122 validation of BASELINE MODEL, the improvement techniques revealed from authors knowledge [11] [12] are  
123 applied to investigate the aerodynamic behavior on MODEL A and MODEL B for comparing the performance  
124 results. Observations reveal that by imparting lean on the MODEL A, impeller exit has noticed a considerable  
125 reduction in total pressure losses with an improved stability, while with added inlet lean to the MODEL B  
126 impeller has shown the additional increase in stall margin with no significant loss in total pressure. Performance  
127 plots are generated for our discussion herewith. When inlet lean is provided to MODEL B in addition to the exit  
128 lean, the variation of area from Hub to shroud at inducer influence on the inlet blade angle variation and hence  
129 on the relative flow diffusion along the blade passage. The consequence of inlet lean feature resulted to further  
130 increase in relative velocity (reduction in tangential velocity) at outlet, which is observed on total pressure rise  
131 and appreciable increase in stall margin over MODEL A. Fig [12] and [13] substantiate the above discussions.  
132 Aerodynamic flow studies at impeller exit on all the three models are relatively compared at design and two off-  
133 design conditions. At design point, the highest relative Mach number is observed with MODEL B Impeller over  
134 Baseline and MODEL A impellers. This indicates the increase in relative Mach number reduces the tangential  
135 velocities (energy transfer) and hence decreases the static pressure rise as evident from the flow studies.

### 136 3 Numerical Model Validation

137 The calculated efficiencies obtained using numerical model shown in Fig [8] is always unpredictable and complex.  
138 However, when these magnitudes are compared looks to be acceptable as the pressure losses are function of  
139 impeller blade loading. Higher work-input coefficient with baseline impeller obviously envisages lower total  
140 pressure losses in relative to other two configurations. Following are the performance parameter observations  
141 tabulated below at design and Off-design conditions for three different impeller models. Readers are to be noted  
142 herewith, the performance values for Baseline Impeller at  $\phi = 0.95$  is not reported as the impeller underwent the  
143 surge occurrence near to design point condition.

## 144 4 VII. Flow Studies Through Centrifugal Impeller

145 From the numerical simulations, stall was detected in the diffuser ring as flow break down in between the passage  
146 with decrease in stage flow coefficient. Overload conditions are identified by flow break down in the diffuser as the  
147 flow coefficient is increased, while the impeller pressure ratio drops to exceedingly low values. No solutions were  
148 pursued beyond these limits and the below discussion is within these boundaries to examine the flow behavior.

### 149 5 a) Flow behavior through Meridional plane

150 The flow field of the impeller without inlet lean (MODEL A) and impeller with compounded effect of inlet and  
151 outlet lean (MODEL B), are examined through relative Mach number distribution in meridional planes at three  
152 different flow coefficients. The purpose is to find possible explanations for the effect of inducer leading edge on  
153 the performance of the compressor. It should be understood that the change in relative Mach number along the  
154 impeller meridional passage indicates the Global Journal of Researches in Engineering ( ) Volume XVII Issue II  
155 Version I growth in diffusion process. Higher the diffusion rate, higher will be the pressure rise.

156 The progressive diffusion along the passage for MODEL B impeller is slow when compared with the Baseline  
157 and MODEL A impellers as evident from Fig [9]. This indicates the MODEL B impeller has a lower decay  
158 rate of relative Mach number distribution along the meridional passage. Accordingly, this flow phenomenon is  
159 visualized with lower pressure rise with MODEL B impeller when compared to rest of the other impeller models  
160 as realized from Fig [10]. The static pressure rise at different flow coefficients envisaged the influence of relative  
161 Mach number distribution growth. The inlet relative Mach number distribution has no significant change between  
162 the three impeller models as evident from Fig [11]. With inlet lean on MODEL B impeller, the inducer inlet

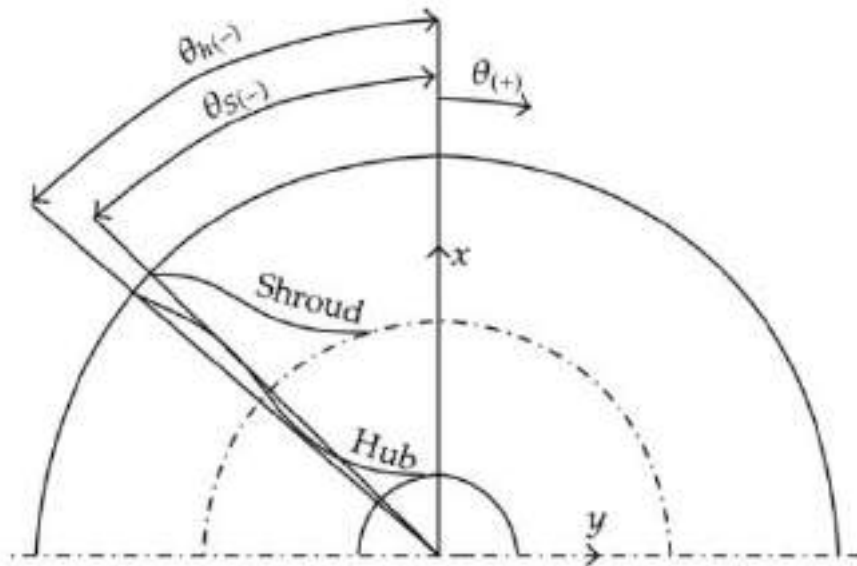
## 6 B) RELATIVE MACH NUMBER ENVELOPS AND STATIC PRESSURE DISTRIBUTION AT IMPELLER OUTLET

163 has variation of area from Hub to shroud that required the change in inlet blade angle variation. This feature is  
164 believed to influence the diffusion control along the impeller passage.

### 165 6 b) Relative Mach number envelops and Static pressure dis- 166 tribution at impeller outlet

167 The relative Mach number and static pressure distribution at impeller outlet is understood implicitly with the  
168 change in static pressure imposed at diffuser outlet. Flow phenomenon observed for the baseline impeller follow  
169 a similar trend as noticed by author Krain H. [1984]. Further, the provision of inlet lean at impeller inlet  
170 (MODEL B), the compound benefit is clearly verified from the flow dynamics showing higher relative Mach  
171 number at impeller exit for design and off-design conditions while, the Baseline impeller demonstrate the lowest  
172 relative Mach number. This phenomenon reflects on the pressure rise development for the respective impeller  
173 models as shown in Fig [13]. Similar interpretation can be made or judged based on realized relative Mach  
174 number at impeller exit. combinations on the impeller performance and stall margin. The results of the impeller  
175 are agreeable when looked onto the performance parameters like Work-input coefficient, Total pressure ratio  
176 and stall margin. The outcome of these parameters realized using MODEL B is comparable with BASELINE  
177 and MODEL A impeller except the computational values obtained for polytropic efficiencies. Although the  
178 commutated efficiencies are overestimated throughout the operating range by various factors, the conclusions  
179 drawn are as follows:

180 ? MODEL A impeller reveals an improved stall margin by 3.1% over baseline impeller, while MODEL B  
envisage further better stall margin by 7.4% compared with Baseline impeller. <sup>1 2</sup>



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Figure 1: Figure [ 2 ]D

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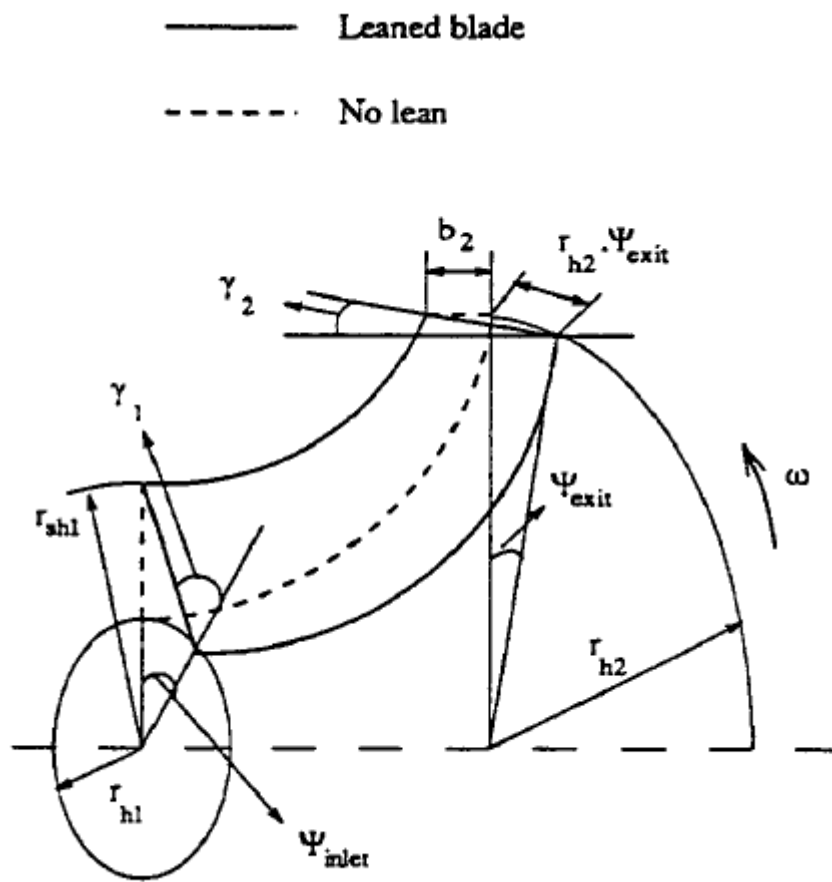


Figure 2:

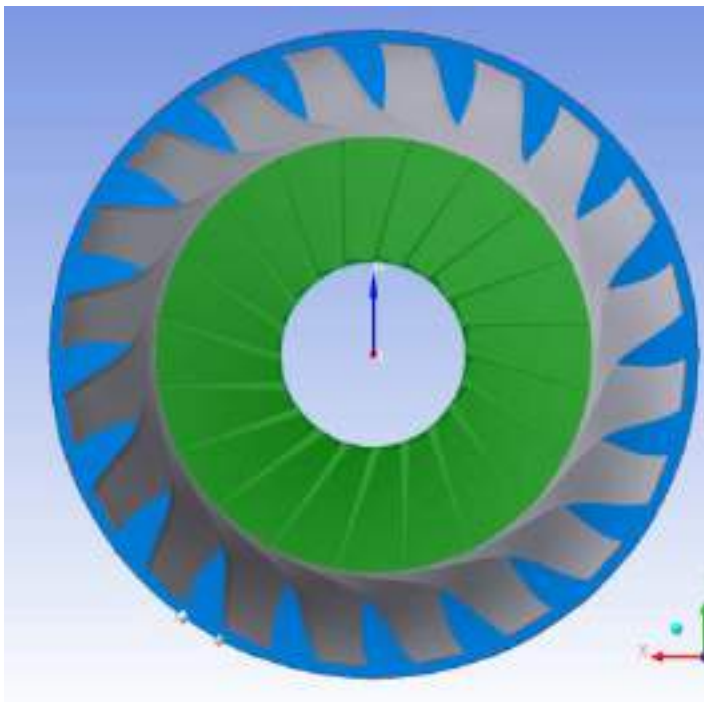
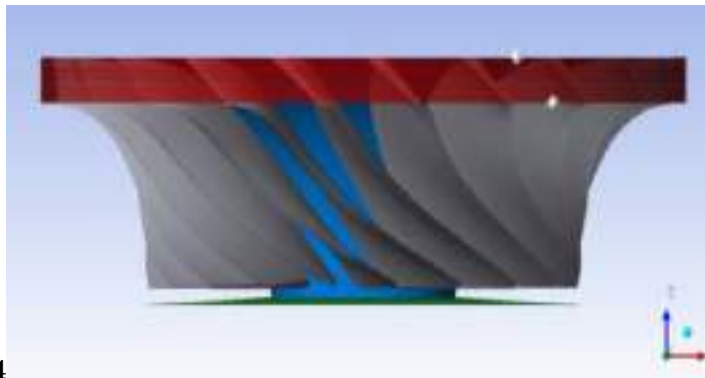


Figure 3: Fig

## 6 B) RELATIVE MACH NUMBER ENVELOPS AND STATIC PRESSURE DISTRIBUTION AT IMPELLER OUTLET

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Figure 4: Fig. [ 4

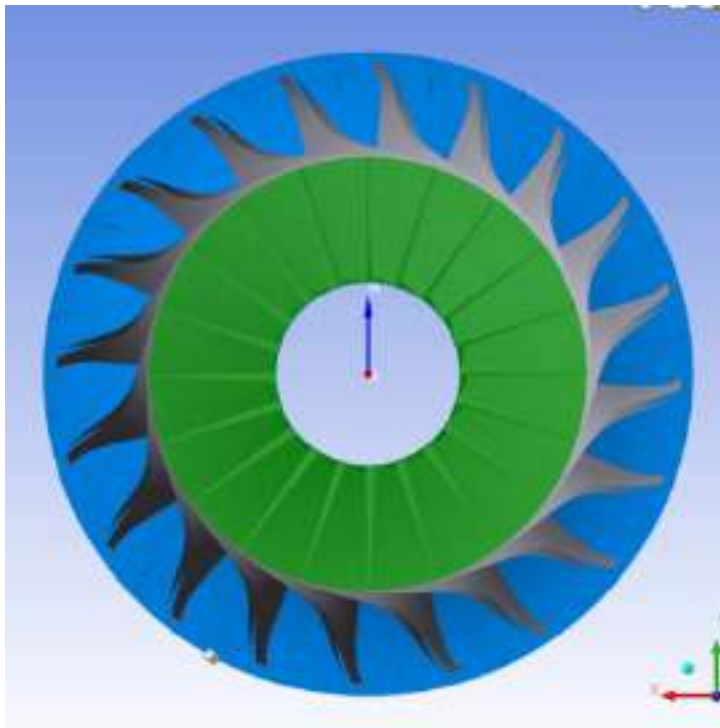


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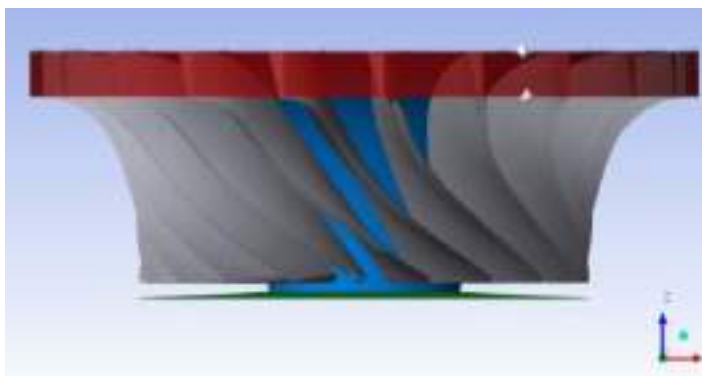
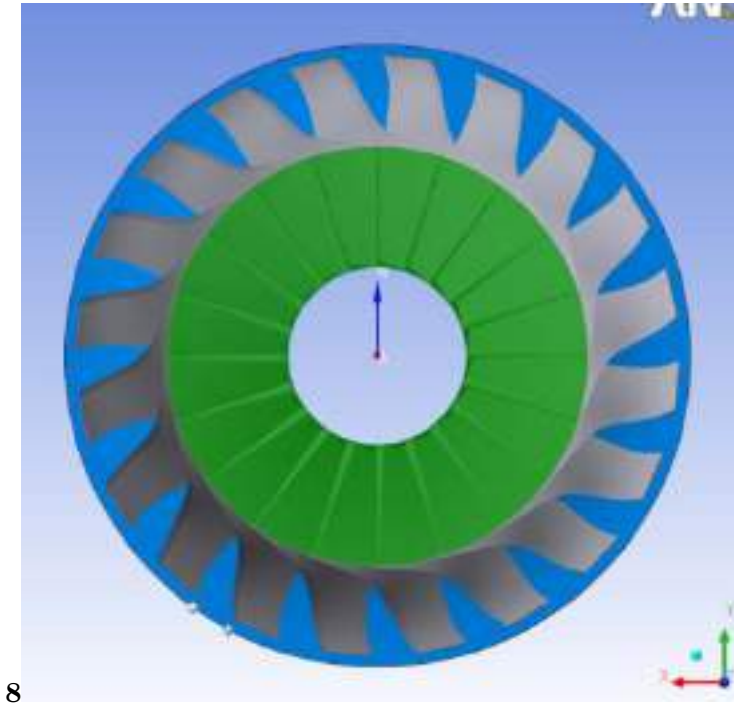


Figure 6: (



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Figure 7: Fig. [ 8

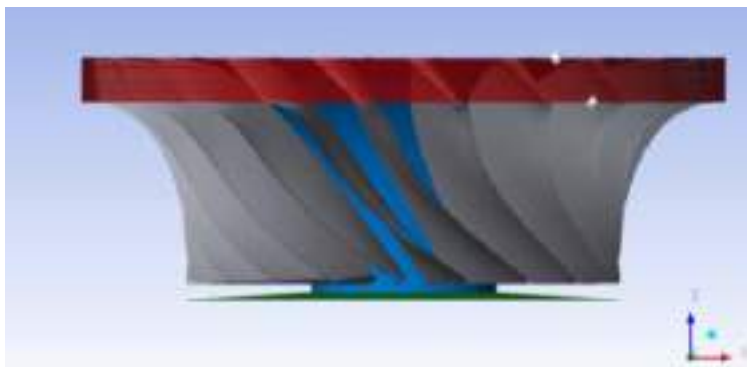


Figure 8:

**6 B) RELATIVE MACH NUMBER ENVELOPS AND STATIC PRESSURE DISTRIBUTION AT IMPELLER OUTLET**

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<b>Impeller Type</b>	<b>Parameter</b>	<b><math>\Phi = 0.95</math></b>	<b><math>\Phi = 1.00</math></b>	<b><math>\Phi = 1.10</math></b>
<b>Baseline</b>	Mass flow (kg/s)		4.48	4.89
	Pressure Ratio		1.92	1.91
	Head Coeff.		0.65	0.64
	Impeller Efficiency		93.00	93.15
<b>Model A</b>	Mass flow (kg/s)	4.34	4.56	4.85
	Pressure Ratio	1.88	1.87	1.85
	Head Coeff.	0.63	0.63	0.61
	Impeller Efficiency	93.5	93.5	92.3
<b>Model B</b>	Mass flow (kg/s)	4.15	4.54	4.90
	Pressure Ratio	1.87	1.85	1.82
	Head Coeff.	0.63	0.62	0.59
	Impeller Efficiency	92.70	92.30	92.00

91011112

Figure 9: Fig. 9 :Fig. 10 : 1 Fig. 11 :Fig. 12 :

? Numerical model realizes narrow operating range than Eckardt impeller. It is fairly expected as the Test impeller has VLD configuration in the downstream that has no influence on incidence effect in off-design condition, since the fluid follows a logarithmic spiral path.

? Eckardt impeller reported 88.6% gain in isentropic efficiency and total pressure ratio of 1.90 with design mass flow of 4.54 kg/s at design speed. The test data obtained with vaneless diffuser configuration for Eckardt makes sense when compared with the numerical model, as the VLD encounters higher pressure losses over LSVD configuration.

Figure 10:

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Centrifugal Compressor Impeller Using Evolutionary Algorithms” Hindawi Publishing Corporation  
Mathematical Problems in Engineering Volume  
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doi:10.1155/2012/752931

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Figure 11:

**6 B) RELATIVE MACH NUMBER ENVELOPS AND STATIC PRESSURE DISTRIBUTION AT IMPELLER OUTLET**

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182 .1 Conclusions

183 Numerical investigations have been performed to determine the effect of the inlet and exit lean

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