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1 2	Kinematics and Statics Including Cable Sag for Large CableSuspended Robots
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7 Abstract

⁸ Cable sag can have significant effects on the cable length computation in a cable suspended

⁹ robot and this is more pronounced in largescale outdoor systems. This requires modeling the

¹⁰ cable as a catenary instead of an approximated straigh-tline model. Furthermore, when there

¹¹ is actuation redundancy involved, the modeling and simulation of the system becomes much

¹² more complex, requiring optimizing routines to solve the problem. A cable-sag-compensated

13 (catenary) model was implemented in simulation for an example large outdoor

¹⁴ cable-suspended robot system to solve the coupled kinematics and statics problems. This

¹⁵ involved optimization of cable tensions and finding the errors involved in the cable length. A

¹⁶ comparative analysis between the straight-line and cable sag model is presented, the main

17 contribution of this paper. Based on the qualitative and quantitative results obtained,

¹⁸ recommendations were made on the choice of model and solution methodologies.

19

Index terms— cable ?suspended robot, cable sag, nonnegligible cable mass, catenary model, forward and inverse position kinematics, pseudostatics

²² 1 I. Introduction

distinct attribute of cable-suspended robots is the possibility of achieving very large workspaces which is difficult or impossible to achieve using rigid link manipulators. In the past two decades major progress has been made in the design and implementation of large scale robots throughout the world. The Five hundred meter Aperture Spherical radio Telescope (FAST) is large scale cable-suspended robot under development in China for astronomical study [1]. Another example is the Skycam [2], which is an aerial camera system that is widely used in sporting arenas. Other examples include CoGiRo (Control of Giant Robots) used for industrial purposes [3] and the Large Cable Mechanism (LCM) used for Radio Telescope Application [4].

Kozak et al. [5] addressed the issue of cable sag by studying the effects of considering mass in the statics and stiffness analysis of the FAST robot. This research used the "elastic catenary" discussed by Irvine [6], to model the cable lengths and subsequently address the inverse pose kinematics problem. Kozak et al. [5] also provided experimental validation and showed that the equations of the elastic catenary are in good agreement with experimental results. Additionally, Russell and Lardner [7] provided experimental validation of the elastic catenary model and quantified the difference between theoretical and experimental cable tensions.

An accuracy and error compensation study of the 6-dof FAST robot was presented by Yao et al. [8] and force distribution in the cables by Li et al. [9]. These results showed that cable sag has a considerable effect on the overall accuracy and control of the robot.

Research on the effects of sag on the workspace and cable characteristics was performed by Riehl et al. [10].

The findings, based on simulations for a 3-cable, 3-dof robot, showed that the workspace and the cable tension distribution for straight-line and elastic catenary (cable sag) models differ. Cable tension under cable sag, unlike

42 the cable tension for the straight-line model, is not constant throughout the cable.

Irvine [6] presented a simplified model for cable sag based on perturbation analysis. This was used by Gouttefarde et al. [11] to model and simulate a 6-cable, 6-dof robot. Although this model is still nonlinear and does not give an analytical solution, it is simpler compared to the elastic catenary. Also, the relationship
between the components of the cable tension is linear in this model. This model was further researched by Nguyen
et al. [12] to find the limitation of the simplified model, which is that the straight-line model is not necessarily
applicable throughout the workspace of the robot, unlike the catenary model. This model also lacks sufficient

experimental validation, whereas the catenary model has been experimentally verified.
Another noteworthy work was by Dallej et al. [13], which was vision-based control of a cablesuspended robot.
This method used cameras in 3D space to instantaneously compute inverse kinematics, thereby attempting to
compensate for cable sag. But this approach is expensive and requires further research to make it viable for field
operations and also to mitigate the iterative steps involved.

The mathematical modeling of kinematics and pseudostatics for small scale cable suspended robots generally 54 works well with the assumption of ideal massless cables (straight-line model). However, for large-scale cable-55 suspended robots, significant errors may arise when assuming the straight-line model for all cables. The main 56 purpose of this paper is to investigate the differences in cable length errors and computation, comparing the 57 straight-line cables assumption vs. a cable-sag model. dit Sandretto et al. [14] test the hypothesis that ignoring 58 cable mass and cable sag is sufficient, with regard to their CoGiRo project. This hypothesis was confirmed for 59 their current prototype hardware, but it was rejected for a planned larger robot. Riehl et al. [10] simply conclude 60 that the cable caternaries must be accounted for, in large workspace cable robots, "in order to achieve good 61 positioning and accuracy." Yaun et al. [15] develop static and dynamic stiffness models for large cable-suspended 62 robots; they conclude that the cable catenary is "important" for stiffness studies. 63

This paper first presents the methods, followed by results and discussion.

⁶⁵ 2 II. Methods

⁶⁶ The methods used by Kozak et al. [5] and subsequently used in [10][11][12] will be followed in this research.

⁶⁷ 3 a) Cable Sag Catenary

The equations of the cable catenary have been known for more than 80 years and they have been applied in various contexts of engineering. and their derivations are not presented (see [5,6]). Consider a cable suspended between two points A and B as in Figure ??.

⁷¹ 4 Figure 1: Cable suspended between two points

Where A is the cable drawing point, B is the end-effector attachment point, L e is the straight-line (Euclidean 72 73 norm) distance between A and B, L is the catenary (actual) length between A and B, g is the acceleration due to 74 gravity, T is the cable tension with X and Z components T x and T z at the end effector side, T dx and T dz are the X and Z components of the cable tension at the cable drawing point, and (x end , z end) are the coordinates 75 76 of the cable at the end-effect or attachment point. For this cable, the static catenary displacement equations for the inextensible case after simplification are (we ignore the axial elasticity since the cable mass dominates the 77 sag):(1) b) Cable-suspended Robot Model () Volume XVII Issue I Version I 2 Year 2017 H 1 1 sinh sinh x z z L 78 79 T T T T g L g ? ? ? ? ? ? ? ? ? ? ? (2) 80

81 Where p L is the linear density of the cable material.

kinematics and statics including cable sag for large cable-suspended robots

83 The kinematic diagram of the cable-suspended robot considered is shown in Figure 2. The base frame $\{A\}$ is fixed to the center of the robot footprint. The end-effector control point is point P, with hi being the height of 84 the towers. Points B i and Pi are the base and top points of the towers / poles respectively and points Ai are the 85 points where winches / motors are located on the ground. L i (or L ei according to the notation in Figure ?? and 86 used later in this paper) are the Euclidean norm (straight-line) cable lengths. In all cases i = 1, 2, 3, 4. The length 87 and width of the cable-suspended robot footprint are L and W, respectively. The IPK problem consists of finding 88 the active cable lengths for a given position. When considering the effects of cable sag (i.e., the mass of the 89 cables) in modeling, cable tension is involved in finding the cable length, unlike the traditional straight-line IPK 90 problem. Hence, the kinematics and pseudostatics problems are coupled and have to be solved simultaneously, 91 as evident from equations (??) and (2). This is a system of nonlinear implicit equations, hence there are no 92 93 analytical solutions, thus forcing the use of numerical methods.

As shown in [5] and [10], for a minimally or perfectly constrained case, the catenary equations (1)

(3) For a redundant or overconstrained case, an additional impediment is that the static problem does not have a unique solution. Since the number of variables outnumbers the equations available, there are infinite valid solutions. Consider a 4-cable 3-dof (XYZ translation) cable-suspended robot as shown in Figures 2 and 3. There are various methods available for mathematical optimization based on the nature of the problem. One popular approach used in field of robotics is that of the Moore-Penrose pseudoinverse of the statics Jacobian matrix, which minimizes the Euclidean norm of the cable tensions. Another useful technique is Linear Programming, which helps to find a solution to the above problem, provided the objective function and constraints are linear.

102 5 ? ?

As pointed out in [5], when using the catenary equations for finding the cable lengths of a redundant cablesuspended robot, one feasible approach is to solve it as constrained optimization problem or specify the (m-n) number of forces prior to solving.

The methodology adapted here to address the Inverse Position Kinematics and Statics problem is as described in [5,8,9,12]. The details of the method adapted and coded in MATLAB are shown in Figure 4 and described below. In this step, all the required inputs are entered for solving the IPK problem, along with necessary parameters such dimensional details of the robot footprint, robot variables, and properties of the cable. Then necessary coordinate transformations are made, which includes transforming global coordinates to local cable coordinates and vice versa. Subsequently, the Euclidean norm lengths of the cable and statics Jacobian matrix are calculated. Table **??** shows the input variables required.

113 6 Table 1: Input variables

114 The Euclidean norm length of the straight-line cable is calculated using:(4)

117 Step 2 -Cable Tensions Optimization

In this step, the cable tensions for a given position are calculated. As mentioned previously, this is a case with multiple valid solutions. To find a unique solution, this problem is solved as a constrained minimization problem. So, the statics problem is treated as a linear programming problem with an aim of minimizing the cable tensions. The problem is formulated as shown below:Objective function: Minimize (T 1 + T 2 + T 3 + T 4) Subject to Constraints: ? ? ? ? ? ? 0 A A A A T F m g ? ? ? ? ? min max i T T T ? ?

Where the cable tensions are is the external force, m A g is the end-effector weight (both expressed in {A} coordinates), and T min and T max are the minimum and maximum allowable cable tensions. winch / motor. This problem is solved using the linear programming solver linprog() in MATLAB. Additionally, the pseudoinverse method was also implemented using the pinv() command in MATLAB for comparison purposes.

127 Step 3 -Cable Lengths Computation

In this final step, cable lengths are computed using the catenary equations, by numerically solving a system of equations. This system of equations is shown below:

(6) (7) (8) where i = 1,2,3,4. For each cable this a system of three equations with three variables (T xi, T zi , and L i). To solve this system of equations the fsolve() command in MATLAB is used, which is an iterative solver used to solve a system of nonlinear equations with real variables. Also, the number of iterations is recorded. Finally, this solver returns the components of the cable tensions along with the cable lengths.

To summarize, the methodology consists of finding the initial variables and subsequent coordinate transformation. An optimization routine is then performed to get a valid set of cable tensions $\{T\}$, such that the sum of cable tensions is minimized.

Finally, these cable tensions are used in the catenary equations to obtain the cable lengths. The code combinesall the three steps to solve the Inverse Position Kinematics and Statics Problem

as the 3-sphere intersection algorithm presented in [14], which is valid only for the straight-line model. When cable sag is considered, FPK suffers the same hindrances that the IPK problem faces, i.e. the kinematics and statics problems are coupled, highly nonlinear, and have to be solved iteratively. The methodology here involves finding components of cable tensions using cable lengths and tensions and subsequently finding the position of the robot.

comprehensively, such that when the user enters a valid position, the program returns the cable tensions and lengths.

¹⁵³ 7 d) Forward Position Kinematics (FPK) And Statics

The FPK problem consists of finding the position of the robot when the cable lengths are given. There are analytical methods to solve this problem such . The five positions are graphically shown in Figure 6 and stated numerically in Table ??.

Step 1 -Computation of Initial Values Similar to the IPK problem, in this step all the necessary input values and coordinate transformations are entered. The active cable lengths and their respective tensions, dimensional details of the robot footprint, and the geometrical and material properties of the cables are entered.

Step 2 -Calculation of Position In this step, the static displacement equations of the catenary (6-8) along with the static equilibrium equations (3) are solved numerically along with necessary transformations of coordinate system. This system of equations is also solved using the fsolve() command in MATLAB and its solution yields the XYZ position of the robot. In summary, the method consists of finding the initial values and necessary transformations. This is followed by solving a system of nonlinear equations whose solution gives the position. A major difference in this FPK problem, when compared to the inverse position problem, is the absence of optimization step, thus making it considerably faster to solve. However, both problems must be solved numerically (i.e. iteratively), when the effect of cable sag has to be considered.

168 **8 III.**

¹⁶⁹ 9 Results and Discussion

Based on the methods described in the previous section, simulations were performed. This included simulating 170 snapshot examples, a trajectory, and parameter variations. The results obtained and their interpretations are 171 discussed in this section. The simulation results presented here use the values in Table 2. When the code for the 172 inverse problem is executed with these snapshot points as inputs, the program calculates the cable lengths and 173 tensions. Table ??: Cartesian coordinates of snapshot points First, the circular check is performed to verify and 174 partly validate the results obtained. To serve this purpose, both the inverse and forward problems were solved 175 for all the five snapshot points. The results are summarized in Table 4 and the circular check is verified (the 176 highlighted columns have equal corresponding values). The cable length difference between the cable sag and 177 straight model is calculated, followed by cable length error computation: (9) (10) The results of difference in 178 cable lengths and their percentage error are plotted in Figure 7 and 8. i e i D L L ?? 100% i e i i i L L ER L ? 179 ?? 180

181 Along with computation of cable lengths, the cable tensions were also calculated using two methods; Linear Programming (LP) and Pseudoinverse Method (PI). These two methods give different values for cable tensions 182 as the objective functions in both cases are different. The resulting graph is shown in Figure 9. From the graphs, 183 it can be observed that the difference in cable lengths obtained from the straight-line model and cable sag model 184 ranges from 0-2600 mm, which appears to be significantly high. However, when the relative error is computed, 185 the range is 0-3 %. The current cable-suspended Robot System, unlike the FAST [1] or LCM [4], is not meant 186 for accurate positioning of the end-effector, hence from the snapshot examples the effects of cable sag appears 187 to be tolerable. But the five examples are a small sample size of random points; this necessitates running the 188 program to simulate a trajectory. 189

¹⁹⁰ 10 b) Trajectory Example

A pick-and-place robot trajectory was simulated with a step size of 0.5 m as shown in Figure ??0. The ideal 191 Cartesian coordinates and straight-line cable lengths for this trajectory are shown in Figures 11 and 12. Similar to 192 193 the snapshot example, the cable length differences between the cable sag and straight-line models are calculated, followed by cable length error computatio. This is shown in Figure 13 and 14. As observed from the graphs, 194 195 the difference in cable lengths obtained from the straight-line model and cable sag model ranges from 0-800 mm and the relative error ranges from 0-1.4%. These values further indicate that, although cable sag contributes to 196 erroneous cable length computation, the error is low enough for purposes where high accuracy is not a prime 197 requirement. The cable tensions were calculated for all the steps in the trajectory by both methods. This was 198 followed by finding the difference between the summation of cable tensions obtained from linear programming 199 (LP) and pseudoinverse (PI) methods From Figures 9, 15, and 16, a straightforward observation is that the two 200 methods (LP and PI) give different solutions for cable tensions except when the cable lengths are equal. Except 201 202 for this case, the linear programming method gives a solution such that the overall cable tensions are less, when compared to the corresponding pseudoinverse solution. 203

Another major advantage of using linear programming is that we can restrict the solution space by using the bounds (Tmin and Tmax). For example, in this simulation Tmin was set to be equal to the weight of end-effector, which can be increased if the cable tensions are found to be insufficient to keep it taut and decreased if feasible. A similar argument can be made for Tmax. In this simulation, Tmax was set to be +? to get an idea of the maximum tension that a particular configuration reaches.

The pseudoinverse method on the other hand does not give this flexibility. But a major merit of the pseudoinverse approach is that it has a closed-form analytical solution, unlike the iterative linear programming method.

212 There are a few issues associated with the use of the LP method that require attention. The LP approach 213 at times gives an abrupt increase or decrease in the tension solutions, thus not resulting in smooth curves for 214 trajectories (see Figure 15). Another issue is that the LP solution at times tends to give a solution that is the 215 lower bounds or upper bounds (T min or T max) for one of the cables. Regardless, a valid solution can be obtained by this method and research is being done in this field to get smoother results with less iterations. 216 Borgstrom et al. [15] show that linear programming can be suitably modified and, with the assistance of suitable 217 control systems, make it more efficient and computationally less expensive. Considering all of these factors, use 218 of linear programming for cable tension calculation is advisable. A summary of this discussion is provided in the 219 form of a comparison chart in Table ??. 220

221 11 Linear Programming (LP)

Moore Penrose Pseudoinverse (PI) Minimize the sum of the cable tensions; Min From the effects of cable sag, it is evident that if the cable weight increases, then cable sag increases, which in turn increases the error or cable length difference between the cable sag and straight-line models. Increasing cable diameter and / or cable material density increases cable weight. Based on the nature of the catenary equations, we expect a nonlinear increase in the difference in cable lengths when cable diameter and density is increased, as verified by the simulations

of Figures 17 and 18. The trends for increasing cable density are very similar to increasing cable diameter and hence are not shown [16].

Another important parameter is the end-effector mass. This is of special importance since it may vary during the operation of a cable-suspended robot. The variation of difference in cable length between the cable sag and straight-line models with an increase in end-effector mass is shown in Figures 19 and 20.

Figure 19: Difference in cable length vs. end-effector mass for nominal position For this case there is an inverse

relationship, i.e. the cable lengths differences decrease as the end-effector mass increases. This makes sense since,

for a given cable size, larger end-effector mass will dominate more and more relative to the cable mass, meaning the straight-line model becomes more and more accurate.

²³⁶ 12 d) Effects of Footprint Dimensions

As the size of the robot footprint increases, the cable length and its overall weight increases, thus increasing the 237 cable sag and increasing the difference in cable length. Keeping the ratio of footprint length to width constant 238 239 (L/W = constant), the area was increased in steps from 1 to 6 acres and the difference in cable lengths was 240 computed. As expected, the cable length difference increases with an increase in area as shown in Figure 21. Complimentary to the previous case, we next study the effects of variation of length to width (L/W) ratio, 241 keeping the area constant. For the nominal position, at a constant tower height, the variation of the Euclidean 242 norm length depends on the footprint length L and width W. By the Pythagorean Theorem, this is dependent 243 on the term . Also, the point where the length and width interchange their values, we expect the difference in 244 cable lengths to remain the same. All these facts are verified by simulation results as shown in Figure 22. The 245 straight-line model has been used in most cable-suspended robot systems when compared to the cable sag model. 246 One of the main reasons for this is its simplicity and an analytical model which is easy to use, manipulate, and 247 implement in control systems. 248

The cable sag model which uses the catenary equations describes the profile of the cable more accurately when compared to the straight-line model. However, the methods required to handle this are highly complicated. Ultimately, any model has to be implemented in a real-time control system to manipulate the cable-suspended robot system. Hence, understanding the computational complexities involved is important.

The catenary equations by themselves are highly nonlinear and are implicit. These equations have to be solved simultaneously with other equations by the accuracy of the solution, such approximations have to be made with more terms in a series expansion, hence requiring more data storage and ultimately increasing the computational cost.

To investigate this issue, during the computation of cable lengths the number of iterations for both snapshot points and trajectory was recorded for the cable sag model. This information is presented in Figures 23 and 24. For comparison, the straight-line model requires no iteration, so the number of iterations for that case is always 1.

261 13 LW?

L / W numerical methods iteratively, which is not only time consuming, but may also involve iteration errors. 262 263 This is a major drawback to the cable sag model. Another major impediment in using iterative methods is the truncation errors involved. These are especially dominant when exponential and hyperbolic terms are 264 approximated using truncated infinite series, thus reducing the accuracy of the solution. To improve There 265 is no definitive prediction that can be made on the number of iterations for a different trajectory or snapshot 266 example, but the examples shown above are representative. They show that even for the simplest trajectories or 267 snapshot points, each cable length computation requires a considerable number of iterations, ranging from 10-40. 268 Thus, the cable sag model, despite being an accurate model, suffers from increased computational requirement. 269

A relative comparison between the straight-line model and cable sag model is shown in Table 6.

²⁷¹ 14 Iterative errors, truncation errors

Solving the cable tension and length problems independently in separate steps (i.e. using the straight-line model) offers significant practical benefits. Firstly, it offers easy control system implementation, since ensuring positive cable tension is a necessary condition and cable sag computation can be circumvented if the corresponding error is within limits. Secondly, solving the steps separately greatly reduces the computational time. Additionally, if the steps are combined (i.e. using the cable-sag model) the problem becomes a constrained non-linear optimization problem (instead of a robust linear programming problem) which needs more sophisticated optimization routines

and is not practical to implement in simple, cost-effective, real-time control system architectures.

²⁷⁹ 15 IV. Conclusion and Recommendations

The current research was conducted primarily with an intention of studying and understanding the qualitative and quantitative effects of cable sag on the calculation of cable lengths in cable-suspended robots. The research also involved studying the effects of cable density, cable diameter, robot footprint size, and computational requirements.

284 16 H

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²⁸⁶ 17 Control system application Straight-forward Difficult

Based on the results of the snapshot and trajectory examples (for a 1-acre footprint robot), the relative error in cable lengths does not exceed 3%. The cable sag model suffers from computational complexities. On the other hand, the straight-line model is simple to manipulate, control, and implement practically. Considering all these factors and quantitative comparison results presented earlier, the straight-line model is preferred over the cable sag model at this particular scale (1-acre footprint, 4047 m2). In cases where the cable sag and errors are greater, the use of a Cartesian servo controller based on GPS sensing of the end-effector location is recommended.

Cable tension distribution is an important aspect of cable-suspended robots and, based on the results of this research, linear programming serves as an efficient tool for computing and ensuring appropriate cable tensions in

cables (the pseudoinverse-based method is much more common). An additional benefit of the LP method is to

help in finding if a given cable tension range is acceptable for motion control of a cable-suspended robot system

and is within the torque limitations of a winch / motor. Conversely, the simulation results could be used for appropriate choices in winch / motor design. $1 \ 2 \ 3 \ 4 \ 5 \ 6$



Figure 1: Figure 2 :

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Figure 6: 1 ?Figure 5 :











Figure 9: Figure 8 :







Figure 11: Figure 9 :







Figure 13: Figure 13 : Figure 14 :







Figure 15: Table 5 :







Figure 17: H



Figure 18: Figure 18 :



Figure 19: Figure 20 :



Figure 21: Figure 22 :



Figure 22: Figure 23 :



Figure 23: Figure 24 :



Figure 24:



Figure 25:



Figure 26:



Figure 27:

$\mathbf{2}$

Variable	Value	Notes
Length (L)	$50 \mathrm{m}$	1 acre footprint
Width (W)	$80.9 \mathrm{m}$	
Pole Height (h)	$7.6 \mathrm{~m}$	All poles are same height
End-effector mass (m)	$258.6 \mathrm{~kg}$	-
Cable Diameter (d)	$20 \mathrm{mm}$	-
Density of the Cable (?)	7860 kg/m 3	Density of a steel cable
External Force (AF)	{0}	0 xyz vector
Tension Lower Limit (T min)	2537 N	-
Tension Higher Limit (T max)	+?	To find the maximum
		force

? 0 0 0 ?

Figure 28: Table 2 :

 $\mathbf{4}$

		Point No.		Х	End-ef	fector	position (m) Y	Ζ		
		1		0		0	0				
		2		-29.4		10.2	1.5				
		3		-33.0		-	2.0				
						18.8					
		4		28.5		-	3.1				
						18.0					
		5		35.0		22.0	5.0				
		Inverse Position Solution					Forward I	Position	Sc	olut	ion
No	.Input		Ou	tput			Input				Out
	Point	L 1	L	Ĺ 3	L 4	L 1	L^{2}		\mathbf{L}	L	Poir
			2						3	4	
	0,										0,
1	0,	56.70 56.70 56.70 56.70 56.70 56.70 56.70 5	6.70)							0,
	0										0
	-29.4,										-29.
2	10.2,	45.25 27.72 81.38 87.87 45.25 27.72 81.38 87.87							10.2		
	1.5	1.								1.5	
	-33,										-33,
3	-18.8,	19.14 52.46 96.41 83.22 19.14 52.46 96.41 8	33.22	2							-18.
	2										2
	28.5,										28.5
4	-18,	77.75 90.26 53.11 22.75 77.75 90.26 53.11 2	22.75	5							-18,
	3.1										3.1
	35,										35,
5	22,	97.64 84.7 14.93 54.92 97.64 84.7 14.93 54.	92								22,
	5										5

[Note: Global Journal of Researches in Engineering () Volume XVII Issue I Version I]

Figure 29: Table 4 :

Criteria	Straight-line model	Cable sag model
Governing	Euclidean norm between	Catenary equations
equations		
	two points	
Type of model	Approximate model	Accurate model
Kinematics and	Analytical solution for	Both problems are coupled
Statics		
	both; problems solved	and there is no analytical
	independently.	solution.
Nature of solutions	Analytical	Numerical
Mass of the cable	Neglected	Included
Areas of applica-	Small scale robots and	Any cable-suspended
tion		
	where accuracy is not a	robot system, especially
	prime concern.	large outdoor systems.
Errors involved	Cable length computation	
	errors	

Figure 30: Table 6 :

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