Emulsion Terpolymerization of St/MMA/Bua: III. Modeling of Bua Backbiting, Diffusion of Monomers and Polymers in the Particle, and Bua Induced Branching

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8 Abstract

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In this work, the BuA backbiting and its kp-gel effect is included in a previous published 9 model for the simulation of the emulsion terpolymerization of St/MMA/BuA. It is then 10 possible to evaluate the branching of this terpolymer and the average diffusion of the 11 monomers, polymers and polymer radicals. The diffusion is evaluated through the propagation 12 and termination coefficients with a modification of the Schmoluchowski equation. On the 13 other hand, it is also found that the BuA propagation coefficient depends on the fraction of 14 BuA free volume XVf,BuA in the terpolymer and that the kind of model suitable for the 15 simulation of the kp-gel effect is determined by the rate of polymerization Rp, the number of 16 radicals in the particle per mol of monomers R/n and the total diffusion of the polymer 17 radicals in the particle nT DPR. 18

20 Index terms—

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21 **1** Introduction

he copolymers of butyl acrylate BuA synthesized by emulsion polymerization are important as resins for the paint industry ??1.2]. In particular, the increment of the branching of their chains promotes a lower swelling of the BuA copolymer by the solvent [3]. The branching also avoids the easier dispersion of carbon black [4]. Both effects modify the characteristics of the paint with technological and economical consequences. The branching is estimated through the branching density BD, to say, the fraction of branched BuA monomer units to the total number of monomer units polymerized [3].

The branching in a polymer with BuA is mostly caused by the backbiting reaction of BuA (intramolecular 28 polymer chain transfer). The backbiting reaction is substantially carried out through a ring of six carbon atoms 29 (abstraction 1:5), when the BuA ended secondary radical finds a BuA unit in the pen-penultimate position and 30 abstracts the hydrogen of the tertiary carbon near to the carbonyl group (See Supporting Information Section 31 S-1) [5,6]. This abstraction of hydrogen forms a lower reactive tertiary electrophylic radical [7]. We emphasize 32 the word electrophylic because the tertiary radical is joined to the carbonyl group of the butyl acrylate, which 33 34 attracts the charge of the tertiary radical and increases its electrophylicity. This tertiary radical propagates with 35 a branch of two inactive monomers. The penultimate effect is present in the backbiting reaction of the terpolymer 36 of styrene/methyl methacrylate/butyl acrylate St/MMA/BuA because the presence of penultimate monomers of St or MMA decreases the backbiting reaction as a consequence of steric effects [5]. At low temperatures T < T37 80 °C, as it happens in the emulsion polymerization of St/MMA/BuA, the -scission [3,8] and depropagation side 38 reactions are negligible and they are not taken into account in the modeling of its backbiting. 39 A lower concentration of monomer leads to a higher degree of branching due to a higher proportion of 40

⁴¹ intramolecular (backbiting) and intermolecular polymer chain transfer with respect to the propagation reaction ⁴² [3]. For this reason, it is expected a higher proportion of branching in the semicontinuous processes. Besides,

it has been found that a higher amount of chain transfer agent reduces the backbiting reaction in acrylics, and 43 correspondingly their branching. There are three explanations to this phenomenon: 1. Transfer of the proton (in 44 the case of thiols) or of the halogen (patching in the case of halogenides) to turn off the reactivity of the tertiary 45 electrophylic radicals; 2. The chain transfer agent decreases the chain length of the polymer chain and there are 46 lesser active sites for the radical intramolecular chain transfer to the polymer; 3. The decrement of the degree 47 of polymerization induced by the transfer agent provokes a diminution of the value of the kinetic coefficients of 48 BuA. This is the hypothesis of kinetic coefficients depending of the degree of polymerization. On this way, a 49 lower value of the kinetic coefficients of BuA induces a higher lessening of the BuA backbiting kinetic coefficients 50 and, in consequence, a decrement of the branch density BD. In the case of bulk polymerization, Agirre et al. 51 [3] discarded the patching of the tertiary electrophylic radicals because the signals in MALDI-TOF and NMR 52 spectra for the Emulsion Terpolymerization of St/MMA/Bua: III. 53

Modeling of Bua Backbiting, Diffusion of Monomers and Polymers in the Particle, and Bua Induced Branching. 54 patched carbon were not found. Nevertheless, Ballard reported that a more careful analysis of the spectra 55 indicates a signal related to the patching of these radicals. Ballard also found that the incertitude of the 56 temperature in bulk polymerization does not allow determining the precise magnitude of the patching by the 57 transfer agent [9]. In the case of solution polymerization, Ballard concluded through the fitting of computer 58 59 simulations to the experimental data that the 1 st hypothesis is discarded. This is due to a low value of the 60 kinetic rate of the chain transfer agent which is not enough to avoid the backbiting of BuA. By the contraire, chains with a lesser degree of polymerization decrease the branching of the polymer. These calculations validate 61 then the 2 nd hypothesis. On the other hand, Ballard also concluded that the 3 th hypothesis is not valid 62 because the kinetic rate in degrees of polymerization greater than 3 does not appreciably depend on the degree 63 of polymerization or the chain transfer agent CBr 4 [9]. On the other hand, there are additional kinetic rates in 64 the emulsion polymerization in comparison to the bulk and the solution polymerization: kinetic rate of radical 65 desorption from the particle to the aqueous phase R f and kinetic rate of capture of radicals from the water phase 66 into the particle R a . So, the concentration of BuA monomeric radicals in the particles is influenced by their 67 capture/desorption into/from the particles and then the backbiting and consequently the branching are influenced 68 by these phenomena. Besides, the influence of the surface on the kinetic rates and the concomitant hypothesis 69 of homogeneous reaction throughout the particle must be evaluated because the emulsion polymerization is 70 compartmentalized in particles emulsified in water. The correct assessment of surface dependence of the radicals 71 72 desorption from the particle, for example, helps to determine more accurately the branching of the St/MMA/BuA 73 terpolymer. The homogeneous reaction throughout the particle was first postulated by Harkins [10,11], but the presence of domains such as a core shell structure in the particle can influence the balance of polymer radicals. On 74 this way, it has been found that the reaction on the surface influences the desorption rate of monomeric radicals 75 R f. This is the case when the backbiting reaction of BuA is taken into account to simulate the molecular weight 76 of the terpolymer [12]. The influence of the surface on the balance of radicals has been found out in particles 77 of 250 nm for PMMA at high conversions, but not in particles of 25 nm [13]. For this reason, it is necessary to 78 determine if the other kinetic rates are surface dependent in the emulsion terpolymerization of St/MMA/BuA. 79 The verification must be done in processes in which the consideration of polymerization in all the volume or on 80 the surface modifies appreciably the outputs of conversion and/or molecular weight. In our experimental setup 81 the verification was done in batch B-3 in which the higher amount of water soluble monomers led to a high 82 desorption of the monomeric radicals from the surface: 83

This verification was also done in the seeded semicontinuous BS-1 in which the particle volume was high, 84 see below. On the other hand, it has been found in the emulsion terpolymerization of St/MMA/BuA that the 85 transfer to monomer R m is not so important for the evaluation of the conversion and the molecular weight [12]. 86 We consider that the evaluation of the k p -gel effect in terpolymers in which the backbiting of BuA occurs is 87 more sensitive for testing the hypothesis of homogeneous particle-phase polymerization. This is due to the high 88 reactivity of BuA-ended secondary radicals (k p, BuA0 = 32390 dm 3 /mol/s at 55 °C) and the low reactivity of 89 the tertiary electrophylic radicals (k p, BuAbb = 34.45 dm 3 /mol/s at 55 °C) [5]. The gel effect in BuA causes a 90 high variation of these propagation coefficients [12] and then the simulation model must be more exact in order to 91 fit the outputs of conversion and molecular weight. On this way, the inclusion of the hypothesis of particle-phase 92 polymerization must give outputs in accordance to the experimental results. In this context, the values of the 93 diffusion of the monomers D M and polymers D P in the particle determined by the simulation model must also 94 correspond to the values found in the literature. The behavior of these diffusion coefficients in the reaction can 95 also help to understand the causes of the gel effect. It has been found that the diffusion of St in polystyrene PSt 96 [14] is of the order of 10 -6 cm 2 /s at W p = 0.5 and T = 50 °C. On the other hand, the diffusion of MMA in 97 polymethylmethacrylate PMMA is of the order of 10 -5 cm 2 /s [13] at W p = 0.5 and T = 50 °C. Furthermore, 98 the diffusion of the monomers of BuA or MMA in a copolymer of MMA/BuA (20-80 wt%) is of the order of 10 99 -7 cm 2 /s [15] at 50 °C and W p = 0.6. For this reason, it is expected a similar trend in the terpolymer of 100 St/MMA/BuA. In principle, the Rouse model can be applied to evaluate the diffusion of the polymers D P in 101 a concentration lower than the critical concentration for the overlap of the polymer chains c^{*} (concentration in 102 which the polymers interpenetrate in the dilution regime). On this way, the Rouse model predicts a dependence 103 of the polymer diffusion coefficient as D P ? (N P) -1 [16]. N P is the degree of polymerization of the polymer 104 and is obtained from the one and second moment of the molecular weight distribution of the dead polymer 1, 2 105

, respectively. On the other side, in accordance to the reptation model the diffusion of the polymer D P scales with N P as D M /(N P) n [17,18] with n = 2 after the critical concentration for the entanglements c^{**}. Griffiths et al. have pointed out that the exponent should increase progressively from n = 0.5 -0.6 at infinite dilution to n = 2 at a concentrated solution [19]. By their part, Tulig and Tirrell have emphasized, the dependence of the diffusion of the polymer D P on the concentration of the polymer solution "c" with a ? ? dependence of c 0.75 at c < c^{**}, and c 1.75 at c > c^{**} in accordance to the reptation model [20][21].

In our previous work [12], we only reported the results of the simulation of the backbiting of the BuAended 112 polymer radicals. The purpose of this work is to explain in more detail the previous results and correlate the 113 backbiting to the diffusion and the branching phenomena in the emulsion terpolymerization. First, we describe 114 the new equations added to the previous terpolymerization model as consequence of the BuAended secondary 115 polymer radicals backbiting. As a general overview, we make a comparison of the outputs of conversion and glass 116 transition temperature between the average k p -k t model for the terpolymerization developed in the previous 117 work and the model which includes the backbiting of BuA. After that, we correlate the gel effect to the diffusion 118 of monomers and polymer radicals in order to explain the causes of the gel effect. As a last part of this work, we 119 make an analysis of the dependence of the branching of the terpolymer to the kinetic conditions of the emulsion 120 terpolymerization. We considerer that the key contribution of our work is the evaluation by first time of the 121 122 diffusion of monomers in the particle. Also, our calculations differentiate the diffusion of the polymer radicals 123 from the polymer molecules.

124 **2** II.

¹²⁵ **3** Review of the Experimental Data

The composition and conditions of batches B-1 to B-4, semicontinuous SC-1 to SC-4 and seeded semicontinuous 126 BS-1 are given in our previous work. The batches B-1, B-2 and B-4 in addition to the semicontinuous SC-1, 127 SC-2 and SC-3 have the same feed composition of St/MMA/BuA (25/50/25 wt%) near to the azeotropic unitary 128 composition. The batch B-3 and the semicontinuous SC-4 have the feed same composition (17/33/50 wt%). The 129 seeded semicontinuous BS-1 was near to composition of B-1 (29/45/26 wt%). The addition rate of monomers 130 was: SC-1 (0.27 g/min), SC-2 (0.48 g/min), SC-3 (0.84 g/min), SC-4 (0.34 g/min), BS-1 (0.50 g/min). The 131 reaction temperature was 55°C, at exception in B-4 and BS-1 in which the reaction temperature was 70°C [12]. 132 The strategy of monomers addition and initial composition of the seed in seeded semicontinuous BS-1 tried to 133 134 keep the proportion of the monomers in the terpolymer almost constant throughout the polymerization reaction. For that reason, the reaction of the batch used as seed was near the unitary azeotropic composition and was 135 stopped at 77.5 % wt% of conversion in order to avoid a higher drift in the composition of the monomers in 136 the terpolymer. This batch was then distilled at low pressure in order to discard the residual monomers. The 137 conversion only increased to 79.2 wt% after the distillation. Most of the monomers in the emulsion were in the 138 particles and the higher boiling point of the acrylic monomers with respect to water produced their lower rate 139 of distillation. So, in accordance to the mass balance, the water was the most distilled liquid and the proportion 140 of monomers in the emulsion slightly increased from 3.2 to 4.1 wt%. On this way, from the 150 g of the distilled 141 emulsion that was used as seed, the mass of monomers was 6.2 g as reported in the previous work [12]. In 142 addition, the values of the final molecular weight for the processes are: B-1: M n = 45000, M w = 102000; B-2: 143 M n = 31000, M w = 57000, B-3: M n = 34000, M w = 52000: B-3: M n = 34000, M w = 52000; SC-1: M n 144 = 28000, M w = 47000; SC-2: M n = 34000, M w = 65000; SC-3: M n = 43000, M w = 72000; BS-1: M n = 43000, M w = 72000; BS-1: M n = 43000, M w = 72000; BS-1: M n = 43000, M w = 72000; BS-1: M n = 43000, M w = 72000; BS-1: M n = 43000, M w = 72000; BS-1: M n = 43000, M w = 72000; BS-1: M n = 43000, M w = 72000; BS-1: M n = 43000, M w = 72000; BS-1: M n = 43000, M w = 72000; BS-1: M n = 43000, M w = 72000; BS-1: M n = 43000, M w = 72000; BS-1: M n = 43000, M w = 72000; BS-1: M n = 43000, M w = 72000; BS-1: M n = 43000, M w = 72000; BS-1: M n = 43000, M w = 72000; BS-1: M n = 43000, M w = 72000; BS-1: M n = 10000; M w = 72000; BS-1: M n = 10000; M w = 72000; BS-1: M n = 10000; M w = 72000; BS-1: M n = 100000; M w = 72000; M w = 7200145 98000, M w = 299000 g/mol [22][23]. 146

We have made the simulation of the transition glass temperature T g and DSC thermograms. We have verified its results with the experimental DSC thermograms obtained in a Dupont 4210 DSC. The experimental DSC thermograms were run from -70 °C to 130 °C with a temperature rate of 10°C/min at open panel with a flux of N 2. The sample approximately weighted 10 mg. The simulation of the DSC was better for the batch processes and the variable that adjusted better the experimental range was T gi , as seen below (The equations for the simulation of Tgi and the DSC thermograms are given in Supporting Information Section S-6).

III. Backbiting Reaction Added to the Previous Terpolymer ization Model

The simulation model for the emulsion terpolymerization given in the previous article [12] is extended to include the backbiting side reaction of BuA.

a) BuA Backbiting model considerations scission [8] and depropagation reactions are not considered. ? The total number of j-ended radicals is obtained by the Nomura's semiempirical equation for the radicals in the particle [24]. The BuA-ended tertiary electrophylic radicals have the same kinetic processes as the secondary BuA-ended radicals: propagation, termination, transfer to monomer and transfer to chain transfer agent, with exception of the rate of capture of radicals into the particle and rate of desorption. The last rate is not considered because the tertiary radicals have a degree of polymerization greater than 2 and then they are not desorbed. ? The k p -gel effect of the BuA-ended radicals starts since the beginning of the reaction [12]. ? The constants of the Hamielec model of k p -gel effect are evaluated independently to the Ray and W p models. The constants of the two last models are interrelated through our previous procedure [12].

166 ? ?-

167 5 ?

? The model considers the initiation, termination and desorption of radicals in the aqueous phase in Equation (S-168 5) -(S-11) of Supplementary Information of the previous work [12]. The model does not consider the propagation 169 of radicals in the aqueous phase. Through the evaluation of the experimental value of particle diameter vs 170 conversion, the model includes the increment of the diameter by the homogeneous nucleation and the subsequent 171 adsorption in the particle. In the previous work, the simulation of the diameter of the particle through the 172 Langmuir adsorption curve includes the increment of the diameter by homogeneous nucleation through the 173 adjustment of the value of the exponent x of the micelar nucleation. The exponent x is given in Table ?? of the 174 previous work [12]. 175

¹⁷⁶ 6 b) Materials Balance

The mass balance was the same as the previous model [12] splitting the term of BuA radicals in terms of secondary and tertiary radicals.

$_{179}$ 7 c) Average total number of j-ended radicals in the particle n T

The total average number of j-ended radicals in the particle "n T " was calculated through the semiempirical 181 182 equation of Nomura [24]. The equations for finding n T only added the term of backbiting. In order to not be 183 redundant with the previous work, these equations are given in Supporting Information Section S-1. The kinetic rates are also given in that section. The number of BuA-ended tertiary radicals n cbb were calculated through 184 a mass balance of the kinetic rates (#rad/part/s) of backbiting R ncbb, propagation R p,ncbb, termination R 185 t,ncbb, transfer to monomer R m,ncbb and transfer to chain transfer agent R T,ncbb in accordance to Table ??. 186 The probability P ijk (i,j,k) of existence of the jended radical triad ijk at time t was calculated by the product of 187 the probabilities of the occurrence of the n i, n j, n k -ended radicals (without considering the tertiary radicals 188 of BuA) at times t-3 t, t -2 t and t t, respectively. t is the increment of time for the evaluation of the reaction 189 kinetics, in this case 0.001 s. This procedure is different to the one of Wang and Hutchinson [5]. 190

The total average number of j-ended radicals in the particle n T and the average number of other radicals that the BuA-tertiary radicals "n" are given by:cbb c b a T n n n n n + + + = (1a) cbb T n n n ? =(1b)

193 With:

194 If n < 0 then n T = n cbb and n = 10 -9 (1c)

The simulation was also performed considering a proportional amount of the radicals n and n cbb when n cbb > n T, but it did not give congruent results. The explanation of this behavior is that the formation of the tertiary BuA-ended radicals needs of the backbiting of polymer radical with a degree of polymerization at least of j = 3. For this reason, these radicals are not desorbed (R fncbb = 0) because the model considers desorption of monomeric radicals with j = 1.

As a chemical kinetic ground, the high reactivity of the BuA secondary radicals and the corresponding lower reactivity of the tertiary BuA-ended radicals produce a lower amount of the secondary radicals in the particle, as will be seen below.

²⁰³ 8 d) Reaction Kinetics

(The reason of defining the k p -gel effect in this article is given in Supporting Information Section S.1.3.) The evaluation of the kinetic rates R f , R p , R m and R T depends on the propagation coefficient k p,ij (See Supporting Information, Tables S-1 and S-2), which has a k p -gel effect. For this reason, we estimated first this variable and then we used it in the corresponding kinetic rates.

i. Propagation rate coefficient of radical "i" to monomer "j" k p, jj .

We have analyzed the k p-gel effect for this system in the previous article [12]. In this work the backbiting of 209 the BuA secondary-ended radicals was taken into account, in which the k p -gel effect starts since the beginning 210 of the reaction. The apparition of the k pgel effect in BuA is caused by the lower free volume V f of St and 211 212 MMA than of BuA in the terpolymer (V fPSt = 0.0025, Vf PMMA = 0.0032, Vf PBuA = 0.0605 at 55°C for the 213 homopolymers) [12]. In principle, we have kept the values and restrictions of the k p -gel constants for St and 214 MMA [12]. On the other hand, we have found the values of the constants for BuA for the V f Ray's k p -gel 215 model in the batch process B-1 iterating at the same time with the values of concentration of monomers in the particle [M] p and critical value of free volume for BuA V fcc as explained in the section Methodology below. 216 Then, we have matched the equations of the V f Ray's and W p k pgel models for BuA-ended radicals in order to 217 obtain the constants A j and V fcj for the W p k p -gel model [12]. The equating gave very different results in the 218 case of BuA in the equating of V f Ray's and the V f Hamielec's k p -gel models. Probably, the sensitivity of the 219 BuA backbiting reaction for the abrupt change of the value of k p,BuA set up this discordance of the Hamielec's 220

221 k p -gel model because this model predicts a lower k p -gel effect (Higher R p) in the batch processes than the

W p and V f Ray's models [12]. On this way, the constants of the Hamielec's k p -gel model were calculated of independently manner.

It has been realized by Sundberg et al. [25] that the constant A 1 of the exponential term for the ???? Hamielec's equation in the homopolymers for the propagation coefficient k p is the critical free volume V f M,*

for the beginning of a monomer to jump:)] 1 1 ($\exp[0.10 \text{ f f p p V V A k k }? = (2)$

V f0 is the critical free volume for the beginning of the k p -gel effect.

The values of the constants A 1j = V f j, * in the emulsion terpolymerization of St/MMA/BuA were near to the free volume of the homopolymers times 6 (we consider the value of A 1,BuA for backbiting, see Table ??): A $1,St = V f St,^* = 0.015$? 6 V f,PSt = 6 (0.0025), A 1,MMA = V f MMA,^* = 0.015? 6 V f,PMMA = 6 (0.0032) A 1,BuA = V f

BuA,* = 0.35 ? 6 V f,BuA =6 (0.0605). These constants were found by iteration to fit the conversion curve [12] and the similarity is worthy, because it shows that free volume of the homopolymers is related to the k p -gel effect. Consequently, a free volume V f near to the j-ended radical of the terpolymer higher than 6 of the free volume of the average homopolymer "j" is necessary to do not have k p -gel effect. We consider that the

constants A 3 for the W p model also have an equivalent meaning as in Equation (2).

237 It was observed a point of change of curvature of the rate of polymerization at X O = 0.78 (V fc2 = 0.05238 corresponding to W pc2 = 0.7945 in B-1), which was associated to an increment of the k p value for the radicals of BuA [12]. We have associated this critical value of V fc2 to a critical value of the proportion of BuA free 239 volume in the terpolymer X Vf (X Vfc2 = 0.84 in B-1) for the beginning of the increment of the BuA propagation 240 coefficient. Then, we have used the critical condition X Vf > X Vfc2 = 0.84 for all the emulsion polymerization 241 processes in the V f k p -gel models. In the W p k p -gel model, we used the condition W pc2 > 0.7945. We 242 consider that the increment of k p,BuA was due to a higher free volume of the last portion of the terpolymer 243 with a BuA-ended radical with a high proportion of BuA monomers in the terpolymer nearer to this radical 244 given by the condition X Vf > X Vfc2 = 0.84. We have associated the increment of the value of k p,BuA with 245 a change of the value of the constants in the k p -gel models, that is, from A 1k to A 2k (See Tables ?? and 3). 246 The change of the value of the constants produces a jump in the value of k p,BuA with its subsequent decrement 247 associated to the fall down of free volume V f. On this way, this jump is associated to a catastrophic behavior in 248 the value of k p,BuA. This catastrophic behavior is found when one monomer has an extremely higher reactivity 249 than the other monomers [26]. In this case, the segmental diffusion of the monomer ended radical of BuA is fast 250 at a higher proportion of BuA in the terpolymer and then it produces an abrupt increment of the reactivity. 251 This increment of the value of k p,BuA is produced by the higher free volume of BuA than that of St or MMA 252 in the terpolymer. With this argument we support the idea that the contribution of the segmental diffusion is 253 important to the evaluation of the k p-gel effect [27], which is included in the diffusion of the polymer radical 254 through its reptation. On this way, the diffusion of the monomers in the bulk of the solution is not as important 255 in the selection of the k p -gel model as their diffusion near to the polymer radical, because near to the polymer 256 the friction exponentially grows up [28], and their diffusion falls down in the same way. 257

In Table ?? are given the corresponding equations for the Hamielec (k = 1), Ray, (k = 2) and W p (k = 3)258 models before and after the critical point for BuA, X Vf > X Vfc2 = 0.84, and in Table ?? are given the values 259 of the corresponding constants. It is observed in the processes batch, semicontinuous and seeded processes a 260 critical value of V fc1 (W pc1) associated to the beginning of the reaction (V fc1 = 0.14 corresponding to W 261 pc1 = 0.1865 in B-1). This value of V fc1 is near to the value of V f for the monomer St. At exception of batch 262 B-3, the point of change of curvature at X Vfc2 > X Vfc2 = 0.84, only changed the value of the constant of the 263 k p -gel effect A 1k to A 2k, (k = 1,2,3 are the k p -gel models). However, the critical value of V fc1 of 0.14 264 (corresponding to W pc1 = 0.1865 in B-1) remained the same as observed in Table ??. We consider that the 265 original critical value of V f (Vf c1 = 0.14, W pc1 = 0.1865) had influence over the gel effect throughout the 266 reaction in almost all the processes. 267

In the case of the fitting of batch B-3 with a higher composition of BuA, it was necessary to put the value of V fc2 = 0.052 (W p = 0.7945) instead of the value used before of V fc1 = 0.14 (W pc1 = 0.1865;) in the expression (1/V f - 1/V fc1) at X Vf > 0.84. Then, we applied Benyahia's procedure for the termination k t -gel effect of BuA in order to write the expression of the k p gel effect as seen in Tables ?? and 3 [29]. On this way, an increment of the proportion of BuA in the batch B-3 caused that the value of V fc2 in the point of change of curvature (V fc2 = 0.052 see Table ??, near to the free volume of the homopolymer PBuA, V f, BuA = 0.05) had influence on the k p -gel effect in batch B-3.

²⁷⁵ 9 ii. Diffusion coefficients in the particle

We consider the model of wormlike chain (reptation of the polymeric radical chain with N monomers). The bond length is b and the bond angle is is the Boltzman constant (erg/K), T is the temperature (K), L pers is the persistence length (cm) which is higher for stiff polymers and the sequence is L pers,St (?9.0 X 10 -8 cm) > L pers,MMA (6.9 X 10 -8 cm) ? L pers,BuA (6.9 X 10 -8 cm) [30], SH is the hindrance factor which indicates the steric hindrance to rotate with the following sequence: SH,St (2.2)> SH,BuA . ? SH,MMA (1.9). There is not certitude in the value of the steric hindrance of BuA because this parameter increases with the size of the short branches (probably near to 1.9, which is the value of the polybutymethacrylate PBuMA). seg is the friction coefficient of the segment of the polymer, in this case the monomer in the terpolymer (g/s).

As also explained below, a higher proportion of BuA in the terpolymer allows a higher diffusion of the polymer 287 radicals and of the monomers. The lower value of the friction coefficient for the segment of BuA, seg, BuA, 288 is caused by the branches of butyl and the two monomer branches induced by the backbiting of the secondary 289 polymer radicals of BuA. On this way, Ferry pointed out that the branching decreases the friction coefficient ??31]. 290 In order to calculate the diffusion coefficients of the terpolymer, it was defined that the effective propagation 291 coefficient k p, Tot with gel effect, has an independent contribution [32] (similar to a parallel electric circuit) of 292 chemical reactivity and diffusion as expressed in Equation (??) [33][34]. Equation (??) is another way to express 293 the dependence of the propagation coefficient on the diffusion phenomena (parallel expression) to the W p and 294 V f Hamielec's and Ray's models given in Table ??. In the later models, the dependence is through the division 295 of the chemical propagation rate coefficient between the corresponding coefficient which considers the diffusion 296 (series expression).diff p Tot p diff p chem p Tot p k k k k k l 1 1 1 1 1 0, + + = + = (4)297

Where k p,Tot0, is the chemical propagation coefficient without gel effect (dm 3 /mol mon /s) and k p diff 298 299 (dm 3 /mol mon /s) is the propagation coefficient which depends on the diffusion of the monomer D M near 300 the polymer radical and the reactivity the polymer radical D PR. If we consider that the diffusion of a polymer 301 radical D PR (cm 2/s) is given by the diffusion of its center of mass (com) D com, PR [18] with a translation by reptation [17] and by the reaction diffusion induced by the propagation of the j-ended radicals D rd = D rd, PR302 (also named roving head diffusion or residual termination [35]. We could calculate the diffusion coefficients 303 through the sequence of the calculations given in Table ??. This sequence was established through a dimensional 304 analysis of the Schmoluchowski equation for reaction of two species in accordance to Mills et al. [13], Russell 305 et al. [35] and Stubbs et al. [18], which gives the equations given below (the corresponding deduction is given 306 in Supporting Information Section S-2). It is important to remark that from the Schmoluchowski equation we 307 obtained an expression specific for emulsion polymerization and, on this way, we could calculate de diffusion of 308 the monomers D M by using the propagation coefficients k p diff, k p, Tot, k p, Tot0, where k p diff is given 309 by:M p rd p diff p k k k + = (5a)) 2 2 (1000 # 4) 2 2 (] [4 M LJ R LJ rd M LJ R LJ rd p p T T rd p D n R 310 D v M n k ? ? ? ? ? ? + = + = (**5b**)) 2 2 (1000 # 4) 2 2 (] [4 R LJ M LJ M R LJ M LJ M p p T T M p D 311 n R D v M n k ? ? ? ? ? ?
 +=+= (5c) Where k p rd = k p rd, PR 312

is the propagation coefficient dependent on the reaction diffusion of the polymer radical and k p M is the propagation coefficient dependent on the diffusion of the monomer.

We have considered that the number of radicals R which reacts per mol of monomers #R/n (radicals/mol) is:p p T T w p p p T w p T v M n V N v M V N n n M n R] [1000] [1000 # # = = = (5d) ?, k B ? ? ? ? ? ? particle is n T, which reacts with the same number of monomers in reaction of first order per mol of monomers. Commonly n T < 0.5, and for example in the simulation of B-1, there were 6.9 X 10 6 molecules of monomer in the particle for one j-ended radical at X O = 99 wt%. In this context, Chern and Poehlein have shown that the monomers are distributed homogeneously throughout the particle and in consequence there is not a gradient of concentration of monomers in the particle [36].

The frequency of jumping of the reaction diffusion coefficient D rd is given by k p, Tot [M T] p . (1/s) [37]. The square of the average radius of gyration of the polymer radical divided by the number of monomers a 2 PR /6 (see Table ??) indicates how much the polymer has diffused from its center of gravity by each reaction of the polymer radical with the monomers.

Ferry [31] and Sundberg et al. [25] have analyzed the influence of the free volume in the diffusion of the polymers and monomers with the corresponding critical point in order to change the diffusion values of k p. These authors indicate that a higher free volume V f of the polymer solution allows a higher diffusion of the polymer radical and monomers. This is concluded in the following equation for the wormlike chain in the case of the diffusion of a polymer radical depending on the free volume V f [25,[30] ??31].) / * exp() 2 (, 2, 0 f Seg f pers seg PR V V b L b N D ? ? = ? (6)

From the equations in Table **??**, it can be observed that the diffusion of the monomer D M near the polymer radical depends directly on the volume of the particle v p, the concentration of monomers in the particle [M T] p and inversely on the number of radicals in the particle n T. The dependence of D M on the free volume is through the gel effect implicit in k p,Tot. On this way, using the Equation (**??**), (5a)-(5c)) with the Hamielec and W p formulas for the gel effect:rd R LJ M LJ T p p i diff p M D n v M k D ? + =) 2 2 (4] [??? (7a) Vg.: Hamielec's model???????????????????

338 model: () 1)] ($\exp[0\ 3\ 0$, ? ? = j p p j ji p diff p W W A k k (7c)

As it will be shown below, D rd was negligible. In Equation (7c) is shown the dependence of D M to W p . In an analogous way, the termination coefficient k t, Tot has an independent (parallel expression) contribution of chemical reactivity and diffusion [33][34].diff t Tot t diff t chem t Tot t k k k k l 1 1 1 1 1 0 , + = + = (8a)With the expression of the Schmoluchowski equation for k t diff [38]:) 2 2 (2 4 , R LJ R LJ t PR A diff t D N k ? ? ? + = (8b)

We have used the following conditions for the evaluation the diffusion of the polymer radical in the termination process D PR,t : Condition 0:rd n t PR M t PR D N D D + = 0) (,,

for $c < c^*$ and N P < N^{**} (9i) 346 Condition 1: Specifically D PR t is the diffusion coefficient (cm 2 /s) of the polymer radical associated to the 347 degree of polymerization of the radicals associated to termination N PR,t, "c" is the concentration of polymer 348 in the solution (g/cm 3). n 3 and n 4 are the exponents of the dependence of the diffusion coefficients D PR,t 349 on the concentration "c". The concentration at the beginning of the overlap of the polymers c*, in which the 350 polymers interpenetrate, was calculated in accordance to Brown and Zhou [39] and given in Table ??. In the 351 reptation model, n 3 = 0.75 and n 4 = 1.75 [17,20]. We consider that the diffusion of the monomers D M takes 352 into account the contribution of the critical concentration for the entanglements c^{**} and the critical value of 353 entanglement N** for this reason they are not present in Equation (9ii) -(9v). The critical concentration c** for 354 the apparition of entanglements was found by the relation $c^{**} = K c / N 0.65$. K c was given by data of Tulig 355 and Tirrell [20] The exponent 0.65 was calculated by the values of $c^{**} = 0.24$ g/cm 3 and Mn = 79,000 g/mol of 356 PMMA reported by the last authors. This correlation was also validated for the data of Callaghan and Pinder 357 [40] and Elias [30] for PSt. In fact, Tulig and Tirrell affirmed that the exponent is between 0.5 and 1 [20]. Then, 358 we have evaluated Equation (9i)-(9v) solving for N PR,t , Vg. For condition 2 in B-1:rd n n t PR M t PR D c N 359 360 361 362 The exponents n 0, n 1 and n 2, were varied in order to fit N PR,t the degree of polymerization of the polymer 363 radicals N PR deduced by the radical moments 0, 1 as seen in Fig. ??. In the semicontinuous processes SC-3 and SC-1, N PR was more higher than N PR,t. This is explained by the hypothesis that the short chains are 364 more important in the termination step as Russell has demonstrated by a balance of radicals [41]. We consider 365 that in the semicontinuous processes, the real distribution of N PR,t was between the distribution of N PR at 366 the end of the addition of the monomers, N PR max , and the distribution which considers n = 2 given by de 367 Gennes, N PR min . The exponents found by this method were congruent with the fact that for a higher value of 368 W p corresponds a higher value of the exponent n i. The sequence of exponents allowed explaining that a lower 369 addition rate of the monomers leads to a lesser diffusion of the polymer radicals, as observed in Table 5. On 370 this way, in the semicontinuous process SC-1 with lowest addition rate of monomers (more effect of diffusion of 371 polymer radicals in the particle), the exponent n 2, associated to the increment of concentration of the polymer, 372 is the highest (1.85) for the same feed composition. Besides, in the process semicontinuous SC-3 with the higher 373 addition rate of monomers, the exponent falls down to 1.70 (less effect of diffusion of polymer radicals in the 374 particle), and in the batch process B-1 n 2 decreases to 1.59 (least effect of diffusion of polymer radicals in the 375 particle). On the other hand, in the batch process B-3 with a higher proportion of BuA, the diffusion exponent 376 n 2 increases to 1.7. Because the simulated different degrees of polymerization in the last two processes (Vg., N 377 P = 242 for B-1 and N P = 169 for B-3 at X O = 50 wt%) and different composition of the terpolymer (Vg., 378 St/MMA/BuA = 35/51/14 mol% for B-1 and St/MMA/BuA = 29/39/32 mol% for B-3 at X O = 50 wt%), the 379 dependence of the exponent of B-3 to N P had a different trend. The final result was that the diffusion of the 380 monomers, terpolymer and terpolymer radicals was higher in batch process B-3 (not shown) as it was expected 381 by the low value of the PBuA's Tg, see below. On the other hand, it is worth to say that the value of the exponent 382 n 0, with a polymer concentration $c < c^*$, was selected as 1.4 in the batch process, value found for toluene or 383 benzene in PSt at W p = 0.5 [42]. The fitting to the experimental data was adequate with this value. 384 We have also performed the fitting with the addition of the critical value N**, as Russell has proposed [41,43] 385 and with or without the addition of the critical concentration c**. On this way; D PR,t ? (N PR,t) -n0 for N 386 $PR,t < N^{**} and c < c^{*} (Condition 0, see Equation (\ref{eq:see})); D PR,t? (N PR,t) -n1 c -n3 for N PR,t < N^{**} and c < c^{**} (N PR,t) -n1 c -n3 for N PR,t < N^{**} and c < c^{**} (N PR,t) -n1 c -n3 for N PR,t < N^{**} and c < c^{**} (N PR,t) -n1 c -n3 for N PR,t < N^{**} and c < c^{**} (N PR,t) -n1 c -n3 for N PR,t < N^{**} and c < c^{**} (N PR,t) -n1 c -n3 for N PR,t < N^{**} and c < c^{**} (N PR,t) -n1 c -n3 for N PR,t < N^{**} and c < c^{**} (N PR,t) -n1 c -n3 for N PR,t < N^{**} and c < c^{**} (N PR,t) -n1 c -n3 for N PR,t < N^{**} and c < c^{**} (N PR,t) -n1 c -n3 for N PR,t < N^{**} and c < c^{**} (N PR,t) -n1 c -n3 for N PR,t < N^{**} and c < c^{**} (N PR,t) -n1 c -n3 for N PR,t < N^{**} and c < c^{**} (N PR,t) -n1 c -n3 for N PR,t < N^{**} and c < c^{**} (N PR,t) -n1 c -n3 for N PR,t < N^{**} and c < c^{**} (N PR,t) -n1 c -n3 for N PR,t < N^{**} and c < c^{**} (N PR,t) -n1 c -n3 for N PR,t < N^{**} and c < c^{**} (N PR,t) -n1 c -n3 for N PR,t < N^{**} and c < c^{**} (N PR,t) -n1 c -n3 for N PR,t < N^{**} and c < c^{**} (N PR,t) -n1 c -n3 for N PR,t < N^{**} and c < c^{**} (N PR,t) -n1 c -n3 for N PR,t < N^{**} and c < c^{**} (N PR,t) -n1 c -n3 for N PR,t < N^{**} and c < c^{**} (N PR,t) -n1 c -n3 for N PR,t < N^{**} and c < c^{**} (N PR,t) -n1 c -n3 for N PR,t < N^{**} and c < c^{**} (N PR,t) -n1 c -n3 for N PR,t < N^{**} and c < c^{**} (N PR,t) -n1 c -n3 for N PR,t < N^{**} and c < c^{**} (N PR,t) -n1 c -n3 for N PR,t < N^{**} and c < c^{**} (N PR,t) -n1 c -n3 for N PR,t < N^{**} and c < c^{**} (N PR,t) -n1 c -n3 for N PR,t < N^{**} and c < c^{*} (N PR,t) -n1 c -n3 for N PR,t < N^{**} and c < c^{*} (N PR,t) -n1 c -n3 for N PR,t < N^{**} and c < c^{*} (N PR,t) -n1 c -n3 for N PR,t < N^{**} and c < c^{*} (N PR,t) -n1 c -n3 for N PR,t < N^{**} and c < c^{*} (N PR,t) -n1 c -n3 for N PR,t < N^{**} and c < c^{*} (N PR,t) -n1 c -n3 for N PR,t < N^{**} and c < c^{*} (N PR,t) -n1 c -n3 for N PR,t < N^{**} and c < c^{*} (N PR,t) -n1 c -n3 for N PR,t < N^{**} and c < c^{*} (N PR,t) -n1 c -n3 for N PR,t$ 387 (Condition 1); D PR,t? (N PR,t) -n2 c -n4 (c^{**}) -(n3-n4) for N PR,t <N^{**} and c>c^{**} (Condition 2), D PR,t? 388 (N PR,t) -n2 (N**) -(n1-n2) c -n3 N>N** and c<c** (Condition 3); and D PR,t? (N PR,t) -n2 (N**) -(n1-n2) 389 $c -n4 (c^{**}) - (n3-n4)$ for $c > c^{**}$ and $N > N^{**}$ (Condition 4). (When we use the methodology of Russell without the 390 normalized concentration c^{**} , it is written $c^{**} = 1$ in the later equations). We have found that the distribution 391 of N PR of the batch processes with Equation (9i)-(9v) was very similar to the distribution of N PR found by the 392 Russell's equations using c^{**} . The Russell's equations without c^{**} could not be evaluated in the batch processes, 393 because the conditions 0, 1, 2 were present in almost all the reaction. On the other hand, the semicontinuous 394

process helped to determine that the Equation (9i)-(9v) applied better to all the processes because the Russell equations with/without c** gave higher value of N PR at the end of the addition of the monomers (N PR max) and higher values of N PR at intermediate conversion. Besides, the Russell expressions with c** did not give the sequence that a lower addition rate of monomers implies a higher Year 2017 C Emulsion Terpolymerization of St/MMA/BuA: III. Modeling of the BuA backbiting, diffusion of monomers and polymers in the particle, and BuA induced branching. µ µ exponent. For this reason, we did not use the Russell expressions.

Another method to evaluate the distribution of the number of polymer radicals was that proposed by Griffiths [19,44] in which the exponent of the polymer radicals is found by n = 0.664 + 2.02 W p. However, the values of the exponents in the cases of batch processes were near to the value of n = 2, and when these values were used in the calculation of N PR,t (see Tables 4,5 and Fig. ??) the distribution was quite different to N PR. For this reason, we did not use this approximation.

We have also considered the reptation model in which n 1 = n 2 = 2 [17]. We have found that k t diff calculated by Equation (8b) is much lower than the value given by the evaluation of Equation (??) with the values of k p,Tot and k p,Tot0 found in the batch and semicontinuous processes. This kind of discrepancy was also found

- by Faldi et al. for the diffusion coefficients of the polymer radicals D PR [45]. We consider that the exponents of the polymer radicals associated to the termination must be lower than 2 in order to have the same k t diff . The
- lower values are indicative that the polymeric solution is not so concentrated. On the other hand, we have found
- that in accordance to the sequence of Table ??, the value of the diffusion of the polymer radicals associated to
- termination D PR,t is independent of the selection of the exponents $n \ 0$, $n \ 1$ and $n \ 2$. This is not the case for the values of the diffusion of the polymer radicals (obtained by the method of moments of the MWD) and dead
- ⁴¹⁴ the values of the unusion of the polymer radie (obtained by the included information of the MWD) and deal ⁴¹⁵ polymers, D PR and D P, respectively. For the report of the values of D PR,t and D P, we have used the values
- 416 of the exponents n 0 , n 1 and n 2 of N PR,t max . It is possible to find a relation between the total propagation
- 417 coefficient k p,Tot and the total termination coefficient k t,Tot . As seen later in Fig. 11 for the batch process
- B-1, k M ? k p diff , k t, Tot ? k t diff ; and considering that D rd ? 0, N PR ? N PR,t (Fig. ??a) with D PR ?
- 419 D PR,t, LJ R ? LJ M and not effect of concentration "c" in the diffusion coefficient D PR (Equation (9i)):) 2 2 420 (8 1000 R LJ R LJ A diff t PR N k D ? ? ? + = (11) Tot t Tot p Tot p Tot t diff p diff t M p k k k k k k k , 0

- 423 Tot t Tot p k N n R N k k + ? ? ? ? ? ? (11c)
- Based on this last equation, we can explain the k p -gel (k p,Tot) effect through variables associated to propagation and termination phenomena.

426 10 IV. Branching

The evaluation of the instantaneous branch density BD i and the instantaneous branching fraction BF i [9], and the corresponding averages of branching density BD [3] and branching fraction BF were done through the following equations.p A p cbb p i R N N R BD, =(12a)? = niter i BD SBD 1 (12b) niter SBD BD = (12c)) (, , A p cbb p pc A p cbb p i N N R R N N R BF + = (12d) ? = niter i BF SBD 1 (13a) niter SBF BF = (13b) Where n iter is the iteration number of the program. SBD and SBF are the accumulated branching density at n iter iterations and the accumulated branching fraction at n iter iterations, respectively.

433 11 V. Methodology

Most of the values of the variables found for the k p -k t average set of models [12] were used as a reference for the set of models which includes the backbiting of BuA. On this way, the values of the diameter of droplet D d and correction factor F c were the Year 2017 C Emulsion Terpolymerization of St/MMA/BuA: III. Modeling of the BuA backbiting, diffusion of monomers and polymers in the particle, and BuA induced branching.

438 12 ? ?

439 same in order to compare the molecular weight results. Three Methods for evaluating the importance of the 440 viscosity in the increment of k p,BuA at the critical condition 2 (X Vfc2, W pc2) were tested: Method 1 (Lower viscosity in the particles). Critical point of X Vfc2 = 0.84 (W pc2 = 0.7945) in interval III of polymerization 441 (zero monomer droplets); Method 2 (Middle viscosity in the particle). Critical point at X Vfc2 = 0.84 (W pc2 442 = 0.7945) and Vf c² = 0.05. This critical point is present at a higher conversion than that at the beginning of 443 interval III, and Method 3 (Higher viscosity), without these critical points, therefore there is not increment of 444 k p,BuA. Thus, Method 2 is a bridge between Method 1 (earlier increment of BuA k p) and Method 3 (not 445 increment of BuA k p value). On this way, we have found that a lower viscosity in the particles produced an 446 earlier increment of BuA k p value (for whichever batch, Method 1) and that a higher viscosity in the particles 447 did not produce an increment of BuA k p value (SC-1, SC-3 and BS-1, Method 3). Methods 1 and 2 were 448 449 almost equivalent in the batch processes because the critical condition of Method 2 was obtained in interval III of polymerization as Method 1 (near X O = 80 wt%). 450

The values for almost all the parameters for this model of the terpolymerization of St/MMA/BuA were found in the literature. We consider that the selection of these parameters was adequate because the selection was based on similar conditions to the experimental ones. When there were several different values for a parameter one of them close to the average of them was taken for our simulations. On this way, they were selected not with the intention of obtaining the best fitting of the kinetic outputs, but by using a chemical and physical criterion of similar conditions to those of the experimental runs [12].

In order to fit the conversion, we have realized that there are four remaining unknown variables: The saturation 457 concentration of monomers in the particle [M i] p,sat , the ratio of the water mass transfer side resistance to 458 459 overall mass transfer for desorbed radical "j" j , the three k p -gel models and the three methods for evaluating 460 the effect of viscosity on the k p -gel effect. With this in mind, we have used the values of [M i] p,sat found in 461 the previous work: [M St] p,sat = 5.6, [M MMA] p,sat = 4.4, [M BuA] p,sat = 4.5 (mol/dm 3) for intervals 462 I and II with the hypothesis that a higher concentration of St in the particle decreases the solubility of MMA in the particle. We have used the Maxwell rule for calculate the instantaneous monomer concentration in the 463 particle [M i] p in intervals I and II [12]:? = sat p i ip p i M f M ,] [] [(14) 464

Where f ip is the fraction mol of monomer i in the particle in relation to all monomers. We have found that for B-1, the monomer MMA was more solubilized in the particle than the other monomers, that is, [MMA] p was higher [12]. On this way, the saturation lower concentration of MMA, [M MMA] p,sat = 4.5 mol/dm 3, did

not avoid of having a higher solubilization of MMA in the particle than the other monomers, but the maximal 468 solubilization decreased but the presence of the other monomers. In the case of interval III, we have used the 469 saturation values reported in the literature: [M St] p,sat =5.6, [M MMA] p,sat =6.9, [M BuA] p,sat =5.2 470 471 (mol/dm 3) and the prediction was accurate, as for example observed in the semicontinuous processes [12]. On the other hand, we have varied the other three parameters: j in the range [0.02, 0.16], the k p -gel models (Ray, 472 Wp, Hamielec) and the tree methods for taking into account the viscosity on the k p -gel effect. The range of j 473 between [0.02, 0.16] was used by Ginsburger [46], and also by Nomura and Fujita [24] for St, MMA or BuA [12]. 474 For simplicity, we have given the same value of j for all the monomer radicals, so = j as Nomura and Fujita have 475 found for St and MMA [24]. The values of the constants of the k pgel effect for all the processes were found by 476 adjusting the conversion of batch B-1, taken as a reference, as explained above and in the previous work [12]. 477 From these k p -gel models and the three methods which take into account the effect of the viscosity, the most 478 adequate model was selected by considering the lowest error in the fitting to the experimental data. After that, 479 we have verified the that the [M i] p,sat the constants of the k p,gel effect for the Hamielec's model and the 480 critical free volume V fcc were optimal through the optimization of the values by the algorithm evolutive reported 481 by Kukkonen [47,48] with the aid of a previously found optimum by trial and error. In fact, the optimal k p,gel 482 effect constants for the Hamielec's model have a physical meaning as explained above. It is important to mention 483 484 that the sensitivity of the models to the above mentioned parameters was very low ant then a change of the mean 485 square error MSE of 0.1 wt% for X O [12] can be considered important. In the selection of the best models for 486 the semicontinuous processes, we also considered an MSE of the accumulated conversion X ac < 0.5 wt% and the best fitting to the conversion at the end of the addition of the monomers, as occurred with semicontinuous 487 SC-3. Two examples of the manner for selecting the best k p -gel models are given in Supporting Information 488 Section S-3. On the other hand, the condition of k p -gel effect in the radical desorption rate R f was critical 489 in batch B-3 in order to adjust the molecular weights. This condition was used for the other processes in which 490 the k p -gel effect in R f was not critical for the evaluation of the molecular weights, as explained in Supporting 491 Information Section S-1.1. All the processes were simulated with k p -gel effect in the kinetic rate of polymer 492 radical transfer to monomer, condition which was critical for the seeded BS-1. Besides, as a chemical congruence 493 the k p -gel effect was present in ????????? the propagation rate of the tertiary radicals and transfer to chain 494 transfer agent for all the radicals. 495

In the literature there are reported works in which the outputs conversion, molecular weight, diameter of particle [46] are considered simultaneously in the parameter estimation algorithm in order to find their optimum values that give the best fitting of the experimental data with the simulation results. In the present work we have chosen a different approach, a sequential one, in which the conversion is fitted first [12] because a valid value of molecular weight needs a correct value of conversion and there is more accuracy in the determination of conversion output than in the other two outputs.

502 **13** VI.

503 14 Results

All emulsion terpolymerization processes were simulated taking into account: 1. The decrement of the value of k 504 p by the k p -gel effect, 2. The possibility of increment of the k p value of BuA by the higher proportion of BuA 505 in the terpolymer, as above has been explained. All the better k p -gel models gave acceptable approximations 506 to the experimental conversion curves, however, always was one that gave a slightly better fitting and then it 507 was chosen as the best k p -gel model as shown in Fig. ??. The best fitting to the experimental data by the 508 simulation curves obtained with the Hamielec's, Ray's and W p models were the following (here we are reporting 509 510 all the cases which satisfied the MSE uncertainty): B-1 (Method 1, best: W p, second best: Ray, = 0.02), B-2 (Method 1, Hamielec, = 0.02), B-3 (Method 1, best: Ray, second best: W p , = 0.02), B-4 (Method 1, Hamielec, 511 = 0.02), SC-1 (Method 3, best: Ray, second best: W p , = best: 0.04, second best: 0.05), SC-2 (best: Method best: Method best: 0.05), SC-2 (best: 0.05) 512 2, second best: Method 1, W p , = 0.02), SC-3 (Method 1, best: Hamielec, best: = 0.04; second best: Ray, 513 second best: = 0.02), SC-4 (Method 3, Hamielec, = 0.02), BS-1 (Method 3, W p , = 0.16). We must emphasize 514 that the selection of the method (1, 2 or 3) was dependent on the value of the polymeric solution viscosity inside 515 the particles at the critical point when the proportion of BuA is higher than X Vfc,BuA : for processes with a 516 low viscosity then Method 1 should be employed, for high viscosity then Method 3, for a middle viscosity then 517 Method 2. All the batch processes were simulated by Method 1 because their low viscosity at the critical point. 518 Besides, the most similar semicontinuous process to the batch B-1, to say, SC-3, was also simulated by Method 519 1. The semicontinuous SC-3 had the higher addition rate of monomers and then a lower viscosity in the particles 520 521 than the other semicontinuous. On this way, it was expected that the polymer particles formed in SC-3 were 522 more similar to the batch process B-1. On the opposite the semicontinuous processes with lower addition rate of 523 monomers, SC-1 and SC-4, had more constraints to the diffusion. This was consequence of the higher proportion of the polymer. The higher proportion of polymer produced a higher viscosity in the particles and then Method 524 3 (the higher viscosity in the particle does not allow the increment of k p,BuA) was more suitable for fitting 525 the conversion. Then, these processes did not have a critical point for an increment of the BuA propagation 526 coefficient. In the same trend, the seeded semicontinuous process BS-1 was simulated by Method 3 due to have 527 the highest proportion of the polymer and then a higher viscosity. 528

As observed in the previous work [12]; A). The k p -gel effect in the batch processes is stronger in the W p 529 and Ray's models and lesser in the Hamielec's model (See Fig. ??2, Supporting Information). On this way, the 530 simulation of the semicontinuous process BS-1 by the W p k p -gel model indicates the k p -gel effect is stronger in 531 this process, B). The increment of the addition of monomers decreases the effect of the k p -gel effect (SC-1 with 532 the lowest addition rate simulated by Ray's and W p models and SC-3 with the highest addition rate simulated 533 by Hamielec's model), C). A higher rate of polymerization R p (due to a higher temperature in B-4) produces 534 that the k p -gel effect is lower in this batch process and then the process is simulated by the Hamielec's k p 535 -gel model. The same increment of R p was found by the higher amount of emulsificant in batch B-2 and then 536 the Hamielec's k p -gel model best fitted this process. On this way, we can say that an increment in the rate of 537 polymerization R p with respect to B-1 make the batch more prone to be simulated by Hamielec's k pgel model. 538 On the other hand, at exception of BS-1 with = 0.16, all the batch and semicontinuous processes have a near 539 to 0.02, indicating that the radical desorption was not appreciable. All the batches have the minimum desorption 540 with a value of = 0.02 and the highest desorption of the semicontinuous was in SC-1 and SC-3 with = 0.04. The 541 value of for the semicontinuous process SC-2 and the batch process B-1 was 0.02, SC-3 as intermediate process 542 between SC-2 and the batch process B-1 should also have a value of = 0.02, but it has a value of 0.04. This higher 543 value of in SC-3 probably indicates that the higher addition rate of monomers produced a lower proportionality 544 545 between the polymerization and desorption rates R p / R f because the desorption of the monomeric radicals was 546 higher. On the other hand, it was observed that in all the processes the coefficient of desorption K f,BuA was the 547

highest one, Vg., K f,St = 0.0384 1/s, K f,MMA = 0.544 1/s, K f,BuA = 0.792 1/s in B-3; K f,St = 0.164 1/s, 548 K f,MMA = 2.24 1/s , K f,BuA = 3.37 1/s in SC-4 (see equations in Table S1, Supporting Information as a 549 reference). Then, the value of = 0.02 in SC-4, where the amount of BuA was higher in the feed, indicates that 550 the resistance to similar to the batch processes. It was also found that the radical desorption was the highest (= 551 0.16) in the seeded semicontinuous process with higher diameter of particle, BS-1, indicating that the resistance 552 to water diffusion outside the particles fell down dramatically in relation to the batch processes. In Fig. ?? 553 are given the fittings of the set of models which includes the backbiting for the BuA-ended radicals and for 554 comparison are shown the fittings by the average k p -k t set of models of the previous work [12]. As observed, 555 the batches B-1 and B-3 were best simulated by models which include the backbiting of BuA than the models 556 which used the average values of k p -k t . 557

The batch process B-4 had a higher polymerization rate caused by a higher temperature of reaction than B-1. The best fitting was achieved by the average Hamielec k p -k t model than by the Hamielec's model which includes the backbiting of BuA. Indeed, the last model predicts a visible point of change of curvature of the rate of polymerization. We consider that, as a consequence of the high experimental polymerization rate R p , the point of change of curvature is not appreciable in the data of B-4. Another possible explanation to this fact is that the dependence of the critical values XV fc and/or V fc on the molecular weight of the terpolymers could soften this change of curvature.

The fitting of the conversion curve for the semicontinuous processes was similar in the selected best models for 565 both the k p -k t average and the BuA backbiting set of models, as seen in Fig. ??. The maximum difference was 566 in the semicontinuous SC-1 and it was necessary to adjust the value of to 0.04 instead of 0.02 in the backbiting 567 models for obtaining a best fit. The k p -k t average gel model for fitting SC-1 was the Benyahia's model which 568 used = 0.16 with MSE XO = 1.25 wt% and MSE Xac = 5.06 wt%. A higher value of could improve the accuracy 569 of the fitting, but it is outside our valid range of [0.02, 0.16]. It was found that the fitting of the Benyahias' k p -k 570 t average gel model with a fixed value of = 0.02 which used Method 3 was poorer than the Ray's k p backbiting 571 gel model with = 0.04 which used Method 3 with MSE XO = 1.09 wt% and MSE Xac = 3.35 wt% in the last 572 model. This indicates that fitting of the k p -k t average Benyahia's kp-gel model is less probable. On this way, 573 the backbiting procedure gives more insights on the value of in emulsion terpolymerization. 574

In the semicontinuous processes it was found a similar trend in the selection of the k p -gel model as in the batch processes: a higher polymerization rate R p makes more suitable the process to be simulated by a free volume Hamielec's V f k p -gel model. On this way, the process SC-3, with the highest R p , was simulated by the Hamielec's V f k p -gel model. On the other hand, the process SC-1, with the lowest polymerization rate R p in semicontinuous, was simulated by Ray's and W p k p -gel models.

We have found that the semicontinuous process SC-4 with a higher proportion of BuA than SC-1, had a lower k p -gel effect and then it was simulated by the Hamielec's V f k p -gel model. We conjecture that in this semicontinuous process the higher free volume in the particle (caused by the higher proportion of BuA in the terpolymer and in the monomers) led to a lower k pgel effect. On the other hand, the process semicontinuous BS-1 was better simulated by W p with Method 3, which indicates a higher influence of the viscosity on the increment of the k p -gel effect. We hypothesize that the higher proportion of polymer in the particle caused this behavior.

We consider that the internal structure of the particle near its surface is different in the batch and semicontinuous processes. Under this hypothesis, the viscosity of the particles and consequently the importance of diffusion of the polymer radicals in the batch processes are lower than in the semicontinuous processes, as it is detailed below. Okubo et al. [49] also found a lower viscosity in a seeded PSt emulsion polymerization with a previously absorbed monomer of MMA (batch process) than in a semicontinuous process in which MMA was

added. They also encountered that the surface morphology of the particles was similar at the end of the reaction 592 for both methods. In the emulsion terpolymerization of St/MMA/BuA, the higher viscosity in the particles of 593 the semicontinuous processes was corroborated by the experimental lower conversion after the end of the addition 594 of the monomers. This fact was also encountered in the work of Urretabizkaia et al. [50]. The lower conversion at 595 the end of addition of the monomers was more visible in the semicontinuous SC-1 and in the seeded process BS-1 596 as seen in Fig. ??. The higher viscosity at the end of the reaction also indicates that the internal structure of 597 the particles in the batch processes is different to that in the semicontinuous processes. The difference of internal 598 structure is at least in the number and size of the domains of the sequences riches of monomers of St and MMA 599 in the terpolymer St/MMA/BuA. Okubo et al. [49] have pointed out this difference of internal structure for the 600 case of PMMA or PSt domains in the mentioned emulsion homopolymerization of MMA in seeds of PSt. 601

In the same context, Sundberg et al. have demonstrated that acrylic polymers with a lower T g allows a higher 602 diffusion of the polymer radicals. On this way, it has been found a difference of three orders of magnitude in 603 the diffusion coefficients in the case of styrene polymeric radicals in a seed of PMMA with a T g of 387 K in 604 comparison with a seed of polymethylacrylate PMA with a T g of 289 K [18]. Consequently, it is expected that 605 the friction seg in a terpolymer with a high proportion of BuA (T g, PBuA = 229 K, [22] See Table ??-3 lower 606 than in the terpolymers with a higher proportion of St or MMA near the surface. For this reason, the diffusion 607 608 of j-ended radicals is higher in BuA richer domains in the particle. On this way, it was expected a more uniform 609 distribution of St and MMA in the particle in the semicontinuous processes SC-1, with no appreciable islands of 610 BuA. SC-1 had the lowest addition rate of monomers, and consequently, the reaction took place near the surface which was enclosed by subsequent reaction steps. Due to the uniform distribution of MMA and St in SC-1, the 611 viscosity was higher than in batch B-1, in which the distribution of MMA and St was more at random. This 612 randomness was produced by the polymerization in the interior of the particles as a consequence of a higher 613 concentration of monomers and higher diffusion of j-ended radicals inside the particle in B-1 than in SC-1. The 614 higher viscosity was more perceptible after the end of addition of the monomers in SC-1. Consequently, the more 615 uniform distribution of domains of St and MMA in the interior of the particle in this process decreased strongly 616 the polymerization rate at the end of the addition of the monomers as also observed in BS-1 (Fig. ??). Indeed, 617 this change of kinetic behavior at the end of the addition of monomers points out that the consumption of the 618 monomers, after the end of their monomers addition, was from outside to inside the particle. It can be argued 619 the for validating this hypothesis, the diameter of the batch and semicontinuous processes must be similar, but 620 the problem is that the diameter of particles in semicontinuous are commonly lower as seen in Fig. ?? of the 621 previous work for batch B-1 and SC-1 [12]. Nevertheless, we have found that a lower experimental conversion at 622 the end of the reaction was found also in the seeded semicontinuous BS-1 with a higher particle diameter than 623 the batch process B-1 as seen also in Fig. ?? of the previous work. This means that at the end of the addition of 624 the monomers in the semicontinuous processes (with whichever particle diameter), at least the particle surface 625 is different to that of the batch processes. This is reinforced when we analyze that the semicontinuous processes 626 SC-2 with a higher addition rate of the monomers than SC-1 presented a higher experimental polymerization 627 rate in relation to the simulation after the end of the addition of the monomers as seen in Fig. ??. For this 628 reason, we have concluded that SC-2 had particles more similar in structure to the particles of the batch process 629 B-1. 630

In relation to the outputs of conversion, composition of monomers in the terpolymer, molecular weight and DSC thermograms, they are very similar for both the k p -k t average set models and BuA backbiting set models. The conversion curves have already been analyzed, the similarity in the composition is analyzed in Supporting Information Section S-4. On the other hand, the desorption rate of monomeric radicals R f in the backbiting set of models is more important than in the k p -k t average set of models. This concept and the analysis of the molecular weight are given in Supporting Information Section S-5.

In relation to the DSC thermograms, in Table ?? are reported the experimental and simulated range of 637 variation of T g, T g,DSC, of the batch and semicontinuous processes (See Supporting Information Section S-6. 638 for the procedure and respective equations to simulate the DSC Thermograms). The value of the experimental 639 T g is given by the intersection of the upper and lower extrapolations of the baseline at the onset of the inflexion 640 [51]. In the case of the simulation, in order to define with more precision the onset for the beginning of T g, we 641 adjusted the initial baseline to be horizontal. Besides, in Table ?? is given the range of variation of the simulated 642 instantaneous glass transition temperature T gi . Indeed, the lower value of T gi corresponds to the onset of 643 the change of curvature of the simulated DSC Thermogram. It was also found that the simulation of the DSC 644 thermograms was similar for the k p -k t average and backbiting including models. 645

The simulated T g,DSC for the batch processes has similar values of T g and a wider range of T g that 646 the experimental one as observed for B-1 in Fig. ??. This corroborates the results of the simulation. On the 647 contrary, the simulated T g,DSC for the semicontinuous processes with a composition similar to B-1 (SC1, SC-648 2, SC-3) have higher values of T g and a narrow range of T g,DSC that the experimental one. Besides, the 649 final values of T g were similar for the experimental and simulated semicontinuous processes. The discrepancy 650 between the experimental and simulation results can be due to the fact that homogeneous nucleation was present 651 in SC-1, SC-2 and SC-3 and then lower values of Tg were obtained. On the other hand, it is interesting to 652 note that the simulation of T g of the semicontinuous SC-4 with a feed composition rich in BuA was correctly 653 simulated by the T g,DSC program. This indicates that in the semicontinuous process SC-4 the homogenous 654

⁶⁵⁵ nucleation was not important and that the range of micelar nucleation was given by T g,DSC . In addition, T ⁶⁵⁶ g,DSC for the semicontinuous process SC-2 (See above) was better simulated than that for the processes SC-1 ⁶⁵⁷ and SC-3. For example, for SC-1: Experimental T g : 29-61 °C; Simulated T gi by backbiting model: 58-61 ⁶⁵⁸ °C. SC-2: Experimental T g : 27-69 °C; Simulated T gi by backbiting model: 45-61 °C. In principle, SC-2 had ⁶⁵⁹ an intermediate monomers addition rate between SC-1 and SC-3. These results indicate a higher homogeneous ⁶⁶⁰ nucleation at lower and higher monomers addition rates, but not at intermediate monomers addition rate.

⁶⁶¹ 15 VII.

⁶⁶² 16 Discussion a) Number of j-ended radicals

The rate of generation of tertiary radicals R ncbb (Pijk) was more important at the end of the reaction for the 663 batch B-3 and for the semicontinuous SC-4, as seen in Fig. 5. In consequence, the amount of tertiary radicals 664 in the particle was appreciable at the end of the reaction, as seen in Fig. 6. At all time, the number of tertiary 665 radicals was mainly diminished by the propagation reaction R p,ncbb. On the same way, the rate of propagation 666 of the tertiary radicals R p,ncbb was higher in the process semicontinuous SC-4 than in the batch process B-3 at 667 the beginning of the reaction (See the dashed line in Fig. 5 used as a reference). Then, there was more branching 668 in SC-4 than in B-3 since the beginning of the reaction, as seen below in Fig. 12. So, the batch process B-3 did 669 not present tertiary radicals until X O = 65 wt% as seen in Fig. 6 and in consequence B-3 had no branching. On 670 the other hand, the increment of BuA-ended tertiary radicals n BuA in SC-4 is caused by having these radicals a 671 degree of polymerization greater than 3 because the backbiting needs a reaction of a BuA-secondary radicals with 672 the antepenultimate BuA monomeric unit of the chain. Since the model considers only the monomeric radical 673 desorption (degree of polymerization of 1) and also due to the low reactivity of the BuA-ended tertiary radicals, 674 it is produced an accumulation of these radicals in the particle. 675 It noteworthy to clear up that the abrupt changes in the number of radicals in Fig. 5 is due to the transition 676

⁶⁷⁶ It noteworthy to clear up that the abrupt changes in the number of radicals in Fig. 5 is due to the transition ⁶⁷⁷ of interval II to interval III of emulsion polymerization (X O ? 40 wt % in B-3), the presence of almost only ⁶⁷⁸ tertiary radicals in the particle (X O ? 80 wt % in B-3), the end of addition of monomers in semicontinuous (X O ⁶⁷⁹ ? 80 wt % in SC-4) and the beginning of the increment for kp, BuA due to the gel effect. The abrupt change of ⁶⁸⁰ the number of radicals can also be due to the increment of the k p ,BuA due to the k p gel effect, as it happens ⁶⁸¹ in SC-3 (X O ? 16 %). These abrupt changes in the number of radicals or k p,BuA produced abrupt changes or ⁶⁸² shoulders in the values of conversion, diffusion, total kp and instantaneous branching of the terpolymer, as seen ⁶⁸³ in Figs. 2-11.

We have compared the number of j-ended radicals simulated to the number of j-ended radicals of the BuAbackbiting model with the k p -k t average model for the batch and the semicontinuous processes. We have found the kinetic variation of the radicals in both models is attenuated when we evaluate the ratio of the product of k p,Tot n T between the BuA backbiting model and the k p -k t average model, R KpnT .el average Kt Kp n k el including backbiting BuA n k R T Tot p T Tot p KpnT mod) (mod) (, , ? =(15a)

In Supporting Information Section S-7 is given the example for batch B-3.

⁶⁹² 17 b) Gel effect

The increment of BuA k p was analyzed through the behavior of the free volume V f, the fraction of free volume of BuA in the terpolymer X Vfc and the fraction of polymer W p for SC-2 in Fig. ?? (The batch B-1 is analyzed in Supporting Information Section S-3.1).

In the case of the semicontinuous process SC-2, the limit of X Vfc2 = 0.84 was exceeded since the beginning 696 of the reaction (X O = 11 wt%) as seen in Fig. ??. If we included the limit of X Vfc2 = 0.84 for the increment of 697 the k p of BuA as occurred for the Ray and Hamielec k p free volume gel models with Method 1, the conversion 698 would be higher. On the opposite, the limit W p = 0.7945 in the semicontinuous process SC-2 was gotten at 699 almost the end of the addition of the monomers and then W p model with Method 1 fitted better the conversion 700 experimental curve than Ray and Hamielec k p free volume gel models with Method 1. On the other hand, 701 Methods 1 and 2 gave similar results because the critical value W p = 0.7945 was the value that was relevant 702 and gotten at the end of the reaction, but Method 2 was slightly better. For this reason, Method 2 was the one 703 704 selected.

705 In order to find a microscopic explanation for the fact that R p indicated what k p -gel model was used to 706 simulate the conversion curve, we have encountered that the batch B-4 had more radicals per mol of monomer 707 #R/n (Equation (5c)) than the batch B-1, as seen in Fig. ??. We have considered that the time required by a monomer to approach one radical was lesser in B-4 with a higher amount of radicals than in B-1. Also 708 the j-ended polymer radicals had to make shorter movements for reacting with the monomers. Thus, a higher 709 number of radicals per mol of monomer #R/n caused a minor movement by diffusion of the radicals (segmental or 710 translational) in order to react with a monomer. We have expressed the rate of polymerization R p in function of 711 #R/n in order to clarify the weight of #R/n in the selection of the k p -gel model as seen in Equation (16a)-(16b). 712

713 18 Global

⁷¹⁴ 2, 2,] [] [ApppTTTotpAppTTTotppNvVMnkNNMnkR = =(16a) 2, 22, 1000] [#
⁷¹⁵ 1000] [] [1000 AppTTotpAppTppTTTotpPNVMnRkNVMvMnkR = = (16b)

Where V p is the total volume of the particles (cm 3 p /cm 3 w), v p is the volume of one particle (cm 3 p716 (part). On this way, a higher value of R p is obtained by both increments of k p. Tot and #R/n. We can say 717 that there is a synergistic effect of the increment of k p, Tot and #R/n (through R p) to decrease the k p-gel 718 effect. This leads to select the Hamielec's free volume model (Ham) for fitting the conversion curve, as happened 719 for B-2, B-4 and SC-3, all with the same feed composition and with the higher values of #R/n as seen in Fig. 720 ??. On the other hand, the processes B-1 and SC-2 were simulated by the W p k p -gel best model (W p) and 721 the process SC-1 by the Ray's best free volume model (Ray) and then have lowers values of #R/n as seen in 722 Fig. ??. The same behavior was found for processes B-3 and SC-4 which have both the same feed composition: 723 SC-4 was simulated by the Hamielec's k p -gel effect model by having a higher value of #R/n than B-3 (Ray's 724 k p -gel effect model) as also seen in Fig. ??. On the other hand, it is also observed in Fig. ?? that the process 725 semicontinuous SC-3 has an abrupt change of slope in the variation of #R/n vs conversion curve. This abrupt 726 change was consequence of the higher polymerization rate R p at X O = 18 wt% because the critical point X 727 Vfc2 for the increment of k p of BuA was achieved. Then, the constant of the k p -gel effect changed from 0.350 728 to 0.108 in the Hamielec's Vf k p -gel effect model (See Table ??). 729

$_{730}$ 19 c) Diffusion coefficients and its relation to the k p -gel constants

Having validated the results of the model, we have calculated the diffusion coefficients in the emulsion 732 terpolymerization of St/MMA/BuA. We have found that the k p -k t average set of models had more uncertainty 733 in the values of k p diff in accordance to Equation (4). This was consequence of the lower variation of the total 734 735 propagation coefficient k p. Tot in this set of models in relation to the total propagation coefficient without gel 736 effect k p,Tot0. For this reason, there were zones in which the values of k p diff were negative, which does not have a chemical meaning. On the opposite side, the diffusion coefficients obtained in the BuA backbiting 737 738 set of models have always positive values, by this reason we have only used the values of this set of models. This is the reason why the models using backbiting are useful for the evaluation of diffusion coefficients in the 739 terpolymerization of S/MMA/BuA. 740

In Fig. ?? are shown the diffusion coefficient for the monomer D M, the total diffusion coefficient for the 741 742 contribution of monomers and polymer radicals D diff, the diffusion coefficient of the polymer radical associated to the termination and propagation D PR,t, the diffusion coefficient of the polymer radical D PR, the diffusion 743 744 coefficient of the dead polymer D P and the diffusion coefficient by reaction diffusion D rd . In this figure it is 745 observed that the diffusion of monomer D M is several orders of magnitude higher than D PR,t and D PR . The 746 value of D M corresponds to the diffusion of the monomers which falls down exponentially near the polymer as seen in the Fig. ?? of von Meerwall et al. for PSt [28]. In Fig. ?? is shown that the diffusion of monomers D M at 747 748 the beginning of the reaction was higher in the process B-1 than in the processes SC-1 and SC-3 in the sequence: B-1 > SC-3 > SC-1 (Vg. at X O =50 wt%: D M = 14.5 X 10 -6 cm 2 /s for B-1 at W p = 0.52 > D M = 5.3 X 10 -5.3 W p = 5.3 X 10 -5.3 W p = 5.3 W p 749 10 -6 cm 2 /s for SC-3 at W p = 0.80 > D M = 3.80 X 10 -6 cm 2 /s for SC-1 at W p = 0.80). This sequence is 750 related to the increment in the viscosity from B-1 to SC-1 and then to the lower rate of polymerization in SC-1. 751 It is worth to mention that the value of D M of these processes with BuA as third component is near to the 752 experimental values of D M = 10 X 10 -6 cm 2 /s for MMA in PMMA at W p = 0.50, and D M = 1 X 10 -6 cm 753 754 2 /s for St in PSt at W p = 0.50 [13][14]18. As it was observed for B-1 and SC-1, the terpolymer composition of 755 BuA was near to 15 mol% at X O = 50 wt% (Supporting Information Section S-4) and this increased the diffusion of the monomers, as explained above. Indeed, the DSC thermograms indicate a higher T g of the terpolymer 756 at the beginning of the reaction and a subsequent decrement with the conversion (Supporting Information Fig. 757 ??1). On the other hand, the way to evaluate the diffusion coefficient of the polymer radicals and polymers 758 was explained above. The similitude to the experimental values of the polymer diffusion coefficients D P can be 759 verified with the values of D P = 7.32×10 -9 cm 2 /s, Mw = 80,000 g/mol, St/MMA/BuA = <math>35/51/14 mol%760 and W p = 0.53 at X O = 50 wt% for B-1 in relation to PMMA D P ? 1 X 10 -8 cm 2 /s with Mw = 90,000761 g/mol, MMA = 100 mol% and W p = 0.50 with the values of Faldi and Mills [13,45]. 762

We consider then that the diffusion of the polymer radicals D PR controls the details of the k p -gel effect, in 763 this case the selection between the V f or W p model. In order to verify this hypothesis, we have evaluated the 764 765 effect of the diffusion coefficient D PR in the selection of the k p -gel model. We have weighted its influence by 766 the product of n T times D PR (cm 2 /s/particle), because a higher number of radicals increases the possibility 767 of reaction with the monomers and then the k p -gel effect is decreased. On this way, when we have analyzed the batch processes B-1, B-2 and B-4. The sequence of values of n T D PR is B-1 < B-2 < B-4 (Vg. at X O 768 =50 %: n T D PR = 16 X 10 -11 cm 2 /s/part for B-1 < n T D PR = 79 X 10 -11 cm 2 /s/part for B-2 < n 769 T D PR = 193 X 10 -11 cm 2 /s/part for B-4). This sequence is also shown in Fig. ??0 and this progression 770 is correlated to the change of using the Ray's k p -gel model in B-1 to the Hamielec's k p -gel model in B-4: A 771 lesser global diffusion of the polymer radicals indicated by the product of n T D PR implies that the friction is 772 more important in the diffusivity of the polymer radicals. On this way, the selection of the k p -gel model in 773

SC-1 (Ray's V f k p -gel model) and SC-3 (Hamielec's V f k p -gel model) was also correlated to the values of n T D PR (Vg. at X O =50 %: n T D PR = 0.16 X 10 -11 cm 2 /s/part for SC-1 < n T D PR = 0.66 X 10 -11 cm 2 /s for SC-3). As observed, in Fig. **??**0, the selection of the k p -gel model by this methodology is more limited than the selection based on the number of radicals per mol of monomer #R/n applied in Fig. **??** because we need to differentiate the batch and the semicontinuous processes. This is consequence of the lower values of n T and D PR in the semicontinuous processes.

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In the batch B-1 is also observed that the diffusion of the polymer radical D PR was lower than the diffusion 781 782 of the (dead) polymer D P (Vg. D PR = 153 X 10 -11 cm 2 /s, D P = 732 X 10 -11 cm 2 /s at X O = 50 783 wt %) because the degree of polymerization was lower in the dead polymer (N PR = 652, N P = 242 for B-1) and the exponent in Equation (??) for obtaining D PR and D P is higher than 1. This was not the case for 784 the semicontinuous processes in which the degrees of polymerization of the polymer radicals and dead polymers 785 were similar (SC-1: N PR = 312, N P = 321). On the other hand, as a consequence of the low amount of 786 j-ended radicals in the particle (in general, n T < 0.5), the reaction diffusion D rd was negligible in emulsion 787 terpolymerization of St/MMA/BuA, as seen in Fig. ??. 788

When we compare the diffusion of the polymer radicals associated to termination D PR,t with the diffusion of 789 the polymer radicals D PR obtained by the method of moments of the molecular weight in the batch processes, it 790 is observed a similar order of magnitude. This indicates that in the batch processes the termination is produced 791 by the long radical polymer chains. On the other side, in the semicontinuos processes the diffusion of the polymer 792 radicals associated to termination D PR,t is higher than the diffusion of the total polymer radicals D PR. This is 793 due to the lower degree of polymerization N PR.t of the short radicals associated to termination than the degree 794 795 of polymerization of the total radicals N PR which was obtained by the method of moments as discussed above. This corroborates the hypothesis that the short radicals have more influence in the termination rate [41,45]. On 796 the other hand, the diffusion of the polymer radicals obtained by the method of moments D PR for the batch 797 B-1 (with a higher proportion of styrene, an aromatic monomer) was lower than those of the batch B-3 (with a 798 higher proportion of aliphatic acrylic monomers) (Vg. at X O = 50 wt %; D PR = 153 X 10 -11 cm 2 /s in B-1; 799 D PR = 653 X 10 -11 cm 2 /s in B-3) as is also affirmed by Griffiths et al. [19] for aliphatic radicals. However, 800 the diffusion coefficients of the polymer radicals associated to the termination reaction D PR,t are similar to (D 801 $PR_{,t} = 438 \times 10 - 11 \text{ cm } 2 \text{ /s in B-1; } D PR_{,t} = 416 \times 10 - 11 \text{ cm } 2 \text{ /s in B-3 at } X \text{ O} = 50 \text{ wt } \%$). 802

In Fig. 11 are shown the total propagation rate coefficient without gel effect k p,Tot0, the total propagation 803 rate coefficient with gel effect k p, Tot, the propagation rate coefficient for the monomer k p M, the propagation 804 rate coefficient of the total diffusion contribution of monomers and polymer radicals k p diff, and the propagation 805 rate coefficient for the reaction diffusion k p rd for the batch process B-1, and the semicontinuous SC-3 and SC-1. 806 The k p -gel effect was higher in the process SC-1 and for this reason k p, Tot was almost one order of magnitude 807 lesser than k p,Tot0 (Fig. 11) As a consequence, the ratio k p diff /k p,Tot0 for SC-1 was lower than the 808 corresponding ones of batch B-1 and semicontinuous SC-3 (see Equation (??)). In other words, the diffusion of 809 monomers was more important in SC-1 than in B-1 or in SC-3. 810

In Fig. 11 is also observed that the k t -gel effect was stronger than the k p -gel effect. In particular, the ratio of k t diff /k t,Tot0 at the beginning of batch B-1 was higher than those of the semicontinuous processes SC-1 and SC-3 (Fig. 11), indicating a lower influence of the polymer radical diffusion on the batch B-1 termination rate.

$_{815}$ 21 d) Branching in the terpolymerization of St/MMA/BuA

We have calculated the averages of branching density BD and branching fraction BF. As seen in Fig. 12, the 816 branching was not present in the batch process B-3, with a higher proportion of BuA, since the beginning of 817 the reaction until X O < 65 wt%. On the opposite side, the processes BS-1 and SC-4, in which the monomers 818 were added in semicontinuous, presented branching in the terpolymer since the beginning of the addition of the 819 monomers. Nevertheless, these processes at the end of the reaction had a lower proportion of branching than B-3 820 $(BD = 18 \times 10^{-4} \text{ in } B^{-3}) > BD = 12 \times 10^{-4} \text{ in } BS^{-1} > BD = 10 \times 10^{-4} \text{ in } SC^{-4} \text{ at } X = 96 \text{ wt\%})$. Then, the 821 kinetic behavior of R p, cbb / R p (Equation (12a)-(12c)) in the reaction determines the accumulated branching 822 at the end of the reaction. The seeded process BS-1 had a lower proportion of BuA and a lower amount of the 823 chain transfer agent n-DDM than SC-4. The first condition caused that the branching fell down and the second 824 that the branching went up (see Introduction section). The final result was that the branching density BD in 825 826 BS-1 was higher than the branching of the semicontinuous SC-4. Besides, the values of BD are consistently one 827 order lower than the experimental value of BD for a homopolymer of BuA without transfer agent (BD = 131 X828 10 - 4 at 60° C) and of the same order when is used a chain transfer agent (BD experimental = 28 X 10 - 4 with CBr 4 at 60°C) [3]. On the other hand, the branch fraction BF is not a factor which determines the degree of 829 branching BD. On this way, the seeded process BS-1 had the highest BF at X O = 96 wt% (Vg. at X O = 96 830 wt%: BF = 30×10^{-4} in B-3, BF = 46×10^{-4} in BS-1 and BF = 19×10^{-4} in SC-4), but the branching of 831 BS-1 was not as important as in B-3. As observed in Fig. 12, a higher addition rate of monomers B-3 > SC-4832

833 produces a higher branching.

In principle, the rate of propagation of the tertiary BuA-ended radicals R p,cbb depends on the number of these radicals in the particle n c,bb (Table 1 and Figs. 5 and 6). We have not considered the length dependency of the propagation coefficient nor a lesser backbiting by a lesser degree of polymerization (2 nd and 3 rd hypothesis, respectively, see above), but have obtained a degree of branching similar to the experimental results. Then, it could be possible that only the abstraction of the hydrogen of the transfer agent n-DDM by the tertiary electrophylic radical was the ground for the decrement of the branching (1 st hypothesis, see above).

We have also compared the branching in the processes B-1, SC-3 and SC-1 (with a sequence to lower addition 840 rate and consequently lesser amount of monomers in the particle from left to right in Fig. ??3). It was found 841 a maximum of the branching density BD and fraction branching FB at X O = 96 wt% in the semicontinuous 842 process SC-3 with the intermediate addition rate of the monomers (BD = 14×10 -4) and a minimum degree 843 of branching in B-1 (BD = 5 X 10 -4). On the other hand, the middle degree of branching was found in SC-1 844 $(BD = 10 \times 10^{-4})$ but at a conversion higher than 96 % the higher branching was in the order B-1 > SC-3 845 > SC-1 (sequence of less rate of addition of monomers), see Fig. ??3. We consider that not only the depletion 846 of the monomers in the particle is an important factor for branching, but also the ratio R p, cbb / R p, at what 847 conversion the branching begins and until what conversion are allowed to react with the monomers. 848

⁸⁴⁹ 22 VIII.

850 23 Conclusion

851 From the k p -k t average model for the emulsion terpolymerization of St/MMA/BuA previously developed, the inclusion of the reaction of BuA backbiting with the associated k p -gel effect in the model allows to know in 852 more exact detail the kinetic phenomena of the emulsion terpolymerization of this system. Indeed, the k p -k t 853 average model is used as a guide in order to improve the results of the model which includes the BuA backbiting 854 reaction with the associated k p -gel effect. On this way, it is realized that the rate of desorption of monomeric 855 radicals has influence on the molecular weight and branching of the terpolymer of St/MMA/BuA. In a synergistic 856 way, the results of both set of models support the hypothesis that the internal chemical structure of the particles 857 grown in semicontinuos processes are different that the internal chemical structure of the particles produced in 858 batch. This indicates that the distribution of sequences of monomers in the terpolymer throughout the particle 859 in both kinds of processes was different. On the other hand, we have found that the gel effect depends on the 860 ratio of the radicals to monomers and when this ratio goes up, the free volume model of Hamielec for the k pgel 861 effect is more suitable for predicting the kinetic of the terpolymerization. When we have associated the gel effect 862 to the diffusion of the monomers and polymer radicals, we have found that the diffusion of the total polymer 863 radicals in the particle determines what k p -gel model is adequate for simulating the gel effect. In this sense we 864 can say that the k p -gel model is a discrete one which takes into account these variables (#R/n or n T *D PR 865) for the selection of the most convenient k p -gel model. This selection was also dependent of the viscosity in 866 the particle, and then we have used three methods in orders to give importance to the influence of the viscosity 867 in the selection of the best method. Besides, the BuA backbiting including model allowed the evaluation of the 868 average diffusion coefficients of the monomers, polymers and polymers radicals. On the other hand, based on the 869 definition of branching density BD, ratio of rate of reaction of tertiary radicals to overall rate of polymerization 870 for all the monomers, we have encountered that the evolution in time of the rate of addition of monomers modifies 871 the percentage of branching. 872

⁸⁷³ 24 a) Supporting Information

874 Supporting Information is available from the Wiley Online Library or from the author.

875 25 Notation A jk

Constant "j" (j = 1 before; j = 2 after the critical point for BuA), for the k p -gel effect of the different "k" models of the propagation rate coefficient k p . b Bond length (cm). BD i , BD Instantaneous branching density or average branching density.

879 26 BF i , BF

Instantaneous branching fraction or average branching fraction. c^* Concentration for the overlap of the polymers in which they interpenetrate (g/cm 3). c^{**} Critical concentration of polymer for the onset of entanglements (g/cm 3). Diffusion coefficient, of the monomer near the polymer, of polymer radical or of polymer radical associated to the termination or of the dead polymer (cm 2/s). D rd, D com,PR D com,PR,t, D P Diffusion coefficient induced by the reaction or the movement of the center of mass of the polymer radical or associated to the termination or the dead polymer (cm 2/s).

886 27 Global

887 28 F c

Correction factor for the diffusion of the n-DDM from the droplets to the particles. f j,bb Steric factor of the penultimate monomers "j" in the backbiting reaction of the BuA ended secondary radicals. k B Boltzman constant (g cm/s 2 /K).

⁸⁹¹ 29 K c

⁸⁹² Coefficient to calculate the beginning of critical concentration for the beginning of the entanglements (cm 3 ⁸⁹³ (monomeric units) n /g) k cbb

Backbiting rate coefficient of the backbiting reaction of the BuA ended secondary radicals (dm 3 w /mol rad /s). K f,j K f Average desorption coefficient from the particle for monomeric radical "j" or for all the monomeric radicals(1/s). k p chem Propagation coefficient dependent only on the reactivity of the monomers and j-ended radicals without considering the diffusion of the monomer and the polymer radical (dm 3 w /mol mon /s). k p diff Propagation coefficient dependent on the reaction diffusion of the monomer and the polymer radical (dm 3 w /mol mon /s). k p M = k p rd,M

Propagation coefficient dependent on the reaction diffusion of the monomer (dm 3 w /mol mon /s). k dr rd = k p rd,PR Propagation coefficient dependent on the reaction diffusion of the polymer radical (dm 3 w /mol mon %). k p,Tot , k p,Tot0

Overall propagation coefficient in the particle considering or not considering the gel effect (dm 3 w /mol mon 903 /s). k t chem Termination coefficient dependent only on the reactivity of j-ended radicals without considering the 904 diffusion of the polymer radical (dm 3 w /mol mon /s). k t diff Termination coefficient dependent on the reaction 905 diffusion of the polymer radical (dm 3 w /mol mon /s). k t, Tot , k t, Tot 0 Overall termination coefficient in the 906 particle considering or not considering the gel effect (dm 3 w /mol mon /s). k tp Overall termination coefficient 907 in the particle considering the gel effect (dm 3 w /mol rad /s) . $k v_{ij} w v = termination "t" (k t, ii according to$ 908 the german or USA convention k' t,ii) rate coefficient of i-ended radical to j-ended radical or polymerization "p" 909 rate coefficient of radical "i" to monomer "j" considering the gel effect at w = time "t" or without gel effect "0" 910 (dm 3 p /mol rad /s). L pers, L pers, i Length of persistence of homopolymer "i" (cm). 911

$_{\scriptscriptstyle 912}$ 30 $[{ m M~j}]~{ m p}$, $[{ m M~T}]~{ m p}$

⁹¹³ Instantaneous monomer "j" or total monomer concentration in the particle "p" (mol/dm 3 p).

914 **31** MSE

⁹¹⁵ Mean square error. n 1, n 2 Exponents associated to the dependence of the diffusion coefficient to the degree of ⁹¹⁶ polymerization. n 3, n 4 Exponents associated to the dependence of the diffusion coefficient to the concentration

917 of polymer. n,n j , n T ,n ncbb

Average number of j-ended radicals without considering the tertiary electrophylic radicals or radical "j" in the particle or total average of radicals or ended tertiary radicals in the particle (rad/part). N, N**, N PR, N, PR,t, N, PR,t max, N, PR,t min, N P Degree of polymerization in a the chain associated to the freely rotating segments or critical number of freely rotating segments which consider entanglements or degree of polymerization in a polymer radical in base to the moments of the molecular weight distribution or polymer radicals associated to the termination or maxima or minimum distribution of polymer radicals associated to termination in semicontinuous or degree of polymerization of a dead polymer. N A Avogadro's constant.

925 **32** N p

Number of particles per unit volume of water ($\#/cm \ 3 \ w$). P ijk (i,j,k) Probability of occurrence of the triad ijk with the j-ended radical "k". <r 0 2 > 1/2 Root mean square end to end distance of the homopolymer (cm). #R/n = #M/n Number of polymer radicals which react with the same number of monomers per mol of monomers (rad/mol).

930 33 R f

931 Desorption rate of all j-ended monomeric radicals (rad/part/s).

932 34 Rg

Gyration radius (cm). R KpnT Ratio of the product of the k p,tot times n T of the BuA backbiting including
model between the same product for the k p -k t average model. R m , Radical transfer rate to monomers of all
j-ended radicals (rad/part/s). R ncbb Backbiting rate of the BuA-ended secondary radicals (rad/part/s).

936 **35 R T**

937 Chain transfer rate for all j-ended radicals to the chain transfer agent (rad/part/s).

938 **36 R p**

⁹³⁹ Total propagation rate of all j-ended radicals on mole basis (mol/cm 3 w /s).

940 **37** R p

941 Propagation rate j-ended radicals (rad/part/s).

942 38 R t

 $_{\rm 943}$ $\,$ Termination of the j-ended radicals (rad/part/s).

⁹⁴⁴ **39** SBD, SBF

Accumulated branching density or branching fraction at n iterations. Fig. ??: Accumulated conversion X ac 945 for the semicontinuous processes SC-1 to SC-4, and for the seeded process BS-1 of the k p -k t average (dashed 946 lines) and the backbiting-including BuA set of models (solid lines). The intersection of the lines A to E with the 947 conversion curves of SC-1, BS-1, SC-4, SC-3, SC-2, respectively, indicates the conversion in which the addition 948 of monomers has ended. Rad/part/s B-3 Iteration in the values of n 0 , n 1 and n 2 until finding a distribution 949 of N PR,t similar a N PR. Evaluation of the values of D PR,t in Equation (9bi)-(9biii). Substitution of N PR,t 950 by N PR and N P in order to evaluate D PR and D P (without D rd), respectively. As reference is calculated 951 952 D PR.t,2 with n 1 = 2 and n 2 = 2. a. For the semicontinuous processes the higher value of the range of T gi was obtained by the intersection of the tangent to the curve of T gi versus X O at the beginning of the reaction 953 and the tangent when the conversion goes from 10 to 30 wt%. b. It was difficult to define the onset of the 954 experimental T g of B-3. 955

⁹⁵⁶ 40 Global Journal of Researches in Engineering () Volume ⁹⁵⁷ XVII Issue III Version

⁹⁵⁸ I 63 Year 2017 C ? ? ? 0,seg , ? 0,i μ 0 , μ 1 ,? 1 ,? 2 ? LJ M , ? LJ R ? SH, ? SH,i ?R r ? ?R ncbb (Pijk) R ⁹⁵⁹ m,ncbb R t,ncbb R p,ncbb ?R r R T,ncbb R m,ncbb R T,ncbb R t,ncbb R p,ncbb ?R r R ncbb (Pijk) SC-4 X O X O pA p T cbb t ncbb t N v n k R 3 2 , ,**10** =) **2** (**1**, ,; , **2** 2 , ^{1 2 3 4 5 6}

Dd, Dp

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		of Researches in Engineering (
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		sion I C
		Journal
C m,ij	Monomer transfer con-	"i"-ended
	stant for	
polymeric radical to mono	mer "j".	
C m,iT	Chain transfer constant o	f i-ended radical to
chain transfer agent T.		

Figure 1:

1

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Figure 2: Table 1 :

6

B-1	B-2	B-3 b	SC-1	SC-2	SC-3	SC-4
19-70	25 - 55	20-44	29-61	27-69	27-63	12-23
9-70	32-70	12-42	67-70	46-64	59-64	9-32
9-70	32-70	-24-42	67-68	45-62	59-62	9-29
9-70	17-70	16-42	60-69	45-60	59-65	21 - 32
9,-70	17-70	-24-42	58-61	45-61	59-63	4-23
	B-1 19-70 9-70 9-70 9-70 9-70	B-1 B-2 19-70 25-55 9-70 32-70 9-70 32-70 9-70 17-70 9,-70 17-70	B-1 B-2 B-3 b 19-70 25-55 20-44 9-70 32-70 12-42 9-70 32-70 -24-42 9-70 17-70 16-42 9,-70 17-70 -24-42	B-1B-2B-3 bSC-1 $19-70$ $25-55$ $20-44$ $29-61$ $9-70$ $32-70$ $12-42$ $67-70$ $9-70$ $32-70$ $-24-42$ $67-68$ $9-70$ $17-70$ $16-42$ $60-69$ $9,-70$ $17-70$ $-24-42$ $58-61$	B-1B-2B-3 bSC-1SC-2 $19-70$ $25-55$ $20-44$ $29-61$ $27-69$ $9-70$ $32-70$ $12-42$ $67-70$ $46-64$ $9-70$ $32-70$ $-24-42$ $67-68$ $45-62$ $9-70$ $17-70$ $16-42$ $60-69$ $45-60$ $9,-70$ $17-70$ $-24-42$ $58-61$ $45-61$	B-1B-2B-3 bSC-1SC-2SC-3 $19-70$ $25-55$ $20-44$ $29-61$ $27-69$ $27-63$ $9-70$ $32-70$ $12-42$ $67-70$ $46-64$ $59-64$ $9-70$ $32-70$ $-24-42$ $67-68$ $45-62$ $59-62$ $9-70$ $17-70$ $16-42$ $60-69$ $45-60$ $59-65$ $9,-70$ $17-70$ $-24-42$ $58-61$ $45-61$ $59-63$

Figure 3: Table 6 :

 $\mathbf{5}$

	B-1	B-2	B-3	B-4	SC-1	SC-2	$\frac{\text{SC-}}{3}$	SC-4
n 0	1.40	1.40	1.40	1.40	-	-	-	-
n 1	1.40	1.50	1.47	1.60	-	-	-	-
n 2	1.59	1.62	1.72	1.41	1.85	1.78	1.78	1.89
Conditions b $0,1,2,4$		$0,\!1,\!2$	$0,\!1,\!2$	0,1,2	$2,\!4$	2,4	4	$1,\!2,\!4$
	Almost 2			Almost	Almost	Almost		Almost
				2	2	4		2
Range W p c	0.48-0.96 0	.48-	0.45-	0.47-	0.79-	0.80-	0.62-	0.74-
		0.97	0.92	0.96	0.82	0.91	0.82	0.89
a. n $3 = 0.75$, n $4 = 1.75$ b. See Equation (9).	(See Text).							

c.

Figure 4: Table 5 :

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 $^{^{2}}$ Year 2017 C Emulsion Terpolymerization of St/MMA/BuA: III. Modeling of the BuA backbiting, diffusion of monomers and polymers in the particle, and BuA induced branching.

³Emulsion Terpolymerization of St/MMA/BuA: III. Modeling of the BuA backbiting, diffusion of monomers and polymers in the particle, and BuA induced branching.© 2017 Global Journals Inc. (US)

 $^{^4{\}rm X}$ O = 0.78 (b) W p = 0.79 X Vf, St X Vf,MMA V f X O = 0.11 SC-2 X O X Vf,BuA X Vf = 0.84 (c) Emulsion Terpolymerization of St/MMA/BuA: III. Modeling of the BuA back biting, diffusion of monomers and polymers in the particle, and BuA induced branching. © 2017 Global Journals Inc. (US)

 $^{^{5}}$ /s)Emulsion Terpolymerization of St/MMA/BuA: III. Modeling of the BuA backbiting, diffusion of monomers and polymers in the particle, and BuA induced branching.© 2017 Global Journals Inc. (US)

 $^{^{6}1\}text{E-4}$ 1 10,000 1E8 k t,Tot
0 k t,Tot or k t diff k p rd k p,Tot k p M or k p diff k p,Tot
0(c)X O B-1(a)k t,Tot 0 k t,Tot or k t diff k p M or k p diff k p rd k p,Tot k p,Tot 0 (b) X O SC-3 k t,Tot 0 k t,Tot or k t diff

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after the critical point j = 2; or total free volume of the pure element I. T, T g Temperature, glass transition temperature or fusion temperature (K, °C). T g,i , T gDSC , Instantaneous , accumulated and obtained by simulated by DSC glass transition temperature (°C).

Critical free volume for the beginning of the monomer or segment of the terpolymer to jump. v p Volume of one particle (cm 3 p).

₉₆₅ .1 V p

- Total volume of the particles (cm 3 p /cm 3 w). W p , W pcj Mass fraction of the terpolymer in the particle or
- critical mass fraction before the critical point j = 1 or after the critical point j = 2.
- 968 x Exponent associated to the micelar nucleation.

969 .2 X ac

970 Accumulated mass conversion a time "t".

971 .3 X O

Monomers overall conversion (experimental o calculated). X Vf, X Vfc Proportion of BuA in the free volume of the terpolymer or critical value for the same parameter.

974 .4 Greek Symbols j

Ratio of the water mass transfer side resistance to overall mass transfer for desorbed radical " j ". t Time step for the iteration of the program (s). Jump frequency of the polymer segments or monomer (1/s).

277 zero and first moments, of the living j-ended radicals; first and second moment of the dead polymers in the 278 molecular weight distribution.

- Diameter of Lennard Jones of the monomer or of the average of the j-ended radicals in the terpolymer (cm).
- 980 Hindrance factor or steric hindrance of monomer in terpolymer.
- Sum of all the reactions of the BuA tertiary electrophylic radicals (rad/part/s).
- 982 Angle between bonds ($^{\circ}$).

seg Friction coefficient of the segment of the polymer, in this case the monomer in the terpolymer (g/s). ??:Equations used to evaluate the gel effect of the polymerization rate constant k p of the BuA-ended radicals (dm 3 /mol) [12].

986 .5 Global

- 987 1. Before X Vfc2 = 0.84, j = c, cbb.
- 988 2. After the critical value X Vfc2 = 0.84; j = c, cbb
- a. We consider that the gel constants and critical values of V f and W p are equal for the secondary and tertiary radical of BuA. b. The monomers are indicated by "i" and the kind of k p -gel model by "k".
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