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1	Determination of Exponential Smoothing Constant to Minimize
2	Mean Square Error and Mean Absolute Deviation
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7 Abstract

⁸ Exponential smoothing technique is one of the most important quantitative techniques in

⁹ forecasting. The accuracy of forecasting of this technique depends on exponential smoothing

¹⁰ constant.Choosing an appropriate value of exponential smoothing constant is very crucial to

¹¹ minimize the error in forecasting. This paper addresses the selection of optimal value of

¹² exponential smoothing constant to minimize the mean square error (MSE) and mean absolute

¹³ deviation (MAD). Trial and error method is used to determine the optimal value of

¹⁴ exponential smoothing constant. An example is presented to discuss the method.

15

16 Index terms—

17 **1 INTRODUCTION**

orecasting can be broadly considered as a method or a technique for estimating many future aspects of a 18 business or other operations. All forecasting methods can be divided into two broad categories: qualitative 19 and quantitative. Many forecasting techniques use past or historical data in the form of time series. A time 20 series is simply a set of observations measured at successive points in time or over successive periods of time and 21 forecasts essentially provide future values of the time series on a specific variable such as sales volume. Exponential 22 smoothing is one the time series techniques which is widely used in forecasting. Exponential smoothing gives 23 greater weight to more recent observations and takes into account all previous observations. In ordinary terms, 24 an exponential weighting scheme assigns the maximum weight to the most recent observation and the weights 25 decline in a systematic manner as older and older observations are included. Weight in the exponential smoothing 26 technique is given by exponential smoothing constant (??). Forecast values are varied with the values of this 27 constant. So, forecast errors are also depended on ?? . Many authors used exponential smoothing method in 28 forecasting. has shown that exponential smoothing remains appropriate under more general conditions, where 29 the variance is allowed to grow or contract with corresponding movements in the underlying level. Taylor (2003) 30 investigated a new damped multiplicative trend approach. Gardner (2006) No research paper has found which 31 determine the optimal value of exponential smoothing constant. In this paper, mean square error (MSE) and 32 mean absolute deviation (MAD) are considered to determine the forecast error and to minimize MSE and MAD, 33 optimal values of exponential smoothing constant are determined. 34

35 **2** II.

³⁶ 3 MATHEMATICAL FORMULATION FOR MSE AND MAD

Different forecasting techniques and time series analysis are described by Montgomery and Johnson (1976). From Montgomery and Johnson (1976), forecast at period t is given for exponential smoothing?? 1 = ?? 0; When ?? 1 = 1 And ?? ?? = ???? ???1 + ??(1 ? ??)?? ???2 + ??(1 ? ??) 2 ?? ???3 + ? ? ? ? ? + ??(1 ? ??) ???1 ?? 0 (1) When ?? > 1

41 About-Department of Industrial and Production Engineering Bangladesh University of Engineering and 42 Technology Email: sanjoy.ipe@gmail.com F Where, ?? ?? = Forecast at period ?? ?? ???1 = Actual value 43 of period ?? ? 1 ?? = Exponential smoothing constant From (1), for different period, it can be written as,?? 1 44 = ?? 0

45 (2)?? 2 = ???? 1 + ??(1 ? ??)?? 0(3)?? 3 = ???? 2 + ??(1 ? ??)?? 1 + ??(1 ? ??) 2 ?? 0(4)?? 4 = ???? 346 + ??(1 ? ??)?? 2 + ??(1 ? ??) 2 ?? 1 + ??(1 ? ??) 3 ?? 0 (5)?? 5 = ???? 4 + ??(1 ? ??)?? 3 + ??(1 ? ??) 2 ??47 2 + ??(1 ? ??) 3 ?? 1 + ??(1 ? ??) 4 ?? 0(6)

And so on?.. The most commonly used measures of forecast accuracy are discussed by Mentzer and Kahn (1995). In this paper, mean square error and mean absolute deviation are considered to measure forecast accuracy.

50 Now Mean Square Error (MSE) can be determined as,?????? = ? (?? ?? ?? ?? ??) 2 ?? ??=1

⁵¹ **4** /??

53 ?? ??) 2]/?? Putting the value of ?? 1 , ?? 2 , ?? 3 , ? ? ? , ?? ?? equation of MSE is found, ?????? = [{?? 0

56]/??**(7)**

57 Again, Mean Absolute Deviation (MAD) is given by,?????? = ? |(?? ?? ?? ?? ??)| ?? ??=1

58 5 /??

This can be written as,?????? = [|(?? 1 ? ?? 1)| + |(?? 2 ? ?? 2)| + |(?? 3 ? ?? 3)| + ? ? ? ? ? + |(?? ?? ? $?? ??)|]/?? Putting the value of ?? 1, ?? 2, ?? 3, ? ? ?, ?? ?? equation of MAD is found ?????? = <math>[|{?? 0 ?$ $1 ?? 1}| + |{???? 1 + ??(1 ? ??)?? 0 ? ?? 2}| + |{???? 2 + ??(1 ? ??)?? 1 + ??(1 ? ??) 2 ?? 0 ? ?? 3}| + ? ? ?$ $+ |{???? ???1 + ??(1 ? ??)?? ???2 + ??(1 ? ??) 2 ?? ???3 + ? ? ? + ??(1 ? ??) ???1 ?? 0 ? ?? ?}]]/??(8)$ Now Trial and Error method is used to find minimum value of exponential smoothing constant. Putting thedifferent values within 0 to 1 for exponential smoothing constant, MSE and MAD are calculated.III.

66 **RESULT AND DISCUSSION**

The method is described by considering a problem. A company's historical sales data are given for some previous periods. Actual values of sales are given in Table 1. 1. MAD is decreased with increasing ?? up to 0.83 and after that MAD is increased. Variation of MAD with ?? is shown in Figure 2. The value of exponential smoothing constant is 0.88 and 0.83 for minimum MSE and MAD respectively. To find the optimal value of exponential smoothing constant, minimum values of MSE and MAD are selected and corresponding value of exponential smoothing constant is the optimal value for this problem.

Minimum values of MSE and MAD and corresponding value of exponential smoothing constant is given inTable 4.

75 7 Conclusions

An exponential smoothing technique is widely used by many organizations to predict the future events. But 76 problems are raised to assign the value of exponential smoothing constant. In this paper, this problem is solved 77 by determining the optimal value of exponential smoothing constant. Mean square error and mean absolute 78 deviation are minimized to get optimal value of the constant and optimal values are 0.88 and 0.83 for minimum 79 mean square error and mean absolute deviation respectively. In this method, any organization can compute 80 the optimal value of exponential smoothing constant to enhance the accuracy of forecasting. This work can 81 82 be extended to minimize some other forecast errors such as mean absolute percent error (MAPE), cumulative forecast error (CFE) etc. 83

©2011 Global Journals Inc. (US) a sale at sixth period is also forecasted. Forecasts at sixth period are 12.455 thousand and 12.068 thousands for minimum MSE and MAD respectively. is shown is Table 5. From the five period actual values, From the optimal value of ??, forecast values for different period are determined using

87 equation (??

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Figure 1: Figure 1 :

McKenzie

and Gardner (2010) provided a theoretical rationale for the damped trend method based on Brown's original thinking about the form of underlying models for exponential smoothing. Hyndman (2002) provided a new approach to automatic forecasting based on an extended range of exponential smoothing methods. Corberan-Vallet et al. (2011) presented the Bayesian analysis of a general multivariate exponential smoothing model that allows us to forecast time series jointly, subject to correlated random disturbances.

Figure 2:

1

April 2011 32 Volume XI Issue III	Determination of Exponential Smoothing Constant To Minimize Mean Square Error and Mean Abso- lute Deviation			
Version I				
Global Journal of	For different values of exponential smoothing constant, MSE			
	and MAD are calculates. Mean square			
neering				
	error for different values of exponential smoothing			
	constant are determined using equation (7) . Table 2			
	shows the MSE values for different ??.			
Period (t)	Actual Value $(?? ??)$ (In thousands)			
0	10			
1	8			
2	14			
3	13			
4	12			
5	12.5			
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Figure 3: Table 1 :

3

Exponential smoothing constant (??) 0 0.1 0.2 0.3 0.4 0.5 0.6 0.7 0.75 0.78 0.8	Mean Absolute Deviation (MAD) 10.7 8.038 6.028 4.535 3.443 2.663 2.241 2.041 1.961 1.919 1.894
0.8 0.82	$1.894 \\ 1.869$
0.83	1.858
0.84	1.867
0.88	1.921
0.9	1.949
0.95	2.022
0.98	2.068
1	2.1

Figure 4: Table 3 :

 $\mathbf{4}$

Criteria	Minimum Value Optimal value of ??	
Mean Square Error	8.031	0.88
Mean Absolute	1.858	0.83
Deviation		

Figure 5: Table 4 :

 $\mathbf{2}$

Exponential smoothing constant (??)	Mean Square Error (MSE)
0	133.85
0.1	76.374
0.2	45.241
0.3	28.3
0.4	18.95

Figure 6: Table 2 :

 $\mathbf{5}$

Period Actual values		Forecast values	Forecast
	(in thousands)	(in thousands)	values (in
		for minimum	thousands)
		MSE	for minimum
			MAD
0	10		
1	8	10	10
2	14	8.096	8.051
3	13	13.291	12.750
4	12	13.034	12.765
5	12.5	12.124	11.794
6		12.455	12.068

Figure 7: Table 5 :

7 CONCLUSIONS

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