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New Nonlinear Damage Law by Fatigue based on the Curve of Bastenaire

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7 Abstract

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 $_{\ensuremath{\mathbb S}}$ This article focuses on the improvement of the nonlinear damage law by fatigue of Chabobe.

⁹ It is a solution to the dependency problem of parameters of the law vis-à-vis the SN curve of

¹⁰ the material used for their production. The determination of the parameters, or wedging of

the law, has the drawback of smoothing by linear regression the points of SN curve in a

¹² particular space specific to the law, called wedging space. So doing, the law is based on the

¹³ regression line points, different from the actual SN curve of the material. The evolution of

14 fatigue damage and hence the lifetime are then modified. The main idea is to develop a new

¹⁵ damage law model, such as the SN curve generated by this formalism is identical to the one

¹⁶ used to describe the fatigue behavior of the material under constant amplitude. In the present

¹⁷ case, it?s obviously the SN curve of Bastenaire model.

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19 Index terms— uniaxial fatigue; damage law; lifetime; wedging; bastenaire.

20 1 Introduction

he existence in the literature of a large number of damage laws by fatigue for predicting lifetime of structures
subjected to varying loads in service illustrates the difficulties of actually having a universal law to forecast lifetime
[2]. Although the phenomenon of failure by fatigue of mechanical components subjected to cyclic mechanical
strain was discovered more than a century by Wöhler, this type of damage remain still an outstanding event in
terms of reliability. However, much progress has been made both in terms of its phenomenological characterization
as of understanding of its mechanisms.

27 Among the proposed damage laws since several decades, the law of Chaboche has always seemed promising although its practical application raises some issues. The attractive aspects of this law are multiple: nonlinear 28 evolution and accumulation of damage, influence of "small" cycles (cycles below the endurance limit) as soon 29 as the damage is initiated, sequence effect (influence of the appearance order of cycles) and the effect of mean 30 stress [3]. The implementation of Chaboche law faces an important challenge from the material parameters 31 determination point of view. It requires the knowledge of the SN curve of the material which undergoes a 32 linear regression in a reference particular and own to the law. Doing so, it significantly changes the SN curve 33 and therefore deviates from the actual behavior of the material. This work is aimed toward the study and the 34 resolution of this disadvantage. First are presented the issues of wedging of the Chaboche law and its impact on 35 the estimated lifetime. An alternative is then proposed by modifying the formalism of the law in order to clear 36 its sensitivity to the wedging field. 37

38 **2** II.

³⁹ 3 Presentation of the Chaboche Law

The implementation of the law of Chaboche is presented here; it helps to highlight the issue faced during itswedging.

⁴² 4 a) Differential expression of the law

The increment ?D of damage by fatigue generated by ?N amplitude cycles ?a and of ?m average value is given by:

(1) With: -b, ? and M 0 are coefficients specific to the material; b is the slope of Haigh traction diagram, modeled linearly as following:

47 5 ?

is the amplitude of the fatigue limit of the material under average stress is fatigue limit of the material in alternating symmetrical tensile (R= ?1). ? The coefficient ? is defined by:

- ⁵⁰ ? For a cycle located above the endurance limit of the material (and called "large" cycle),
- ⁵¹ ? For a "small" cycle, b) Integration of differential law

parameter ? depending on the type of cycle met ("small" or "large" cycle) generate two different integration formalisms of the damage.

60 6 i. Integration of damage in case of small cycle

The application of small cycle defined by (?a, ?m), change the damage from Di value to Dj value. The integration of the damage in this case is given by:

- 63 (2) By putting :
- 64 (3)
- $_{65}$ The cumulative damage after applying the small cycle (
- 66) is given by: (

X appears as a functional damage whose characteristic is to cancel or be equal to unity at the same time as
D. Note that if the level damage Di is zero initially, it remains after the application of small cycle. Small cycles
do not contribute to material damage once the damage is initiated.

70 7 ii. Integration of damage in case of large cycle

71 The application of a large cycle defined by (?a, ?m), moves the material damage from Di value to Dj value. The 72 integration of damage is then given by the following:

(5) Under constant amplitude, the integration leads to the SN curve expression within the meaning of the

⁷⁴ law of Chaboche; it is given by: (6) Where: N f is the number of cycles at crack initiation within the material

⁷⁵ under constant amplitude loading defined by the (?a, ?m). By repeating, the equation (??) of the integration of ⁷⁶ damage becomes:

77 (7) III.

78 8 Wedging Principle of the Law

The damage cumulative observed in the case of a small cycle and a large cycle (equations (4), (?? The main 79 80 problem of wedging of the Chaboche law lays in the fact that the Bastenaire SN curve of the material is not 81 linear in the wedging space, even if we consider as window all the curve or only part of it. No specific guidance is made by the author of the law [1]. This will practically generate under uniaxial fatigue with constant amplitude 82 a lifetime prediction significantly different from those projected by the SN curve intrinsic of material. The use 83 under uniaxial fatigue with variable Year 2014 ume XIV Issue IV Version I?) m b? (1 o M a ? 1 ?) i D (1 1 1 84 85 86 87 j11i11j?a?) m b? (1 K ?) (1 ? o M a 1 f N ? ? ? ? ? ? ? ? ? ? a? m ? m R) m (? A ? a ? a ? 1 K ? ? 88 ????????????;?;;KiKjN1XXjj?? 89

The SN curve subtended by the damage law of Chaboche is then based on equation [9] a straight line in reference (ln ?a; ln(K.Nf)), reference that is later called the wedging space. To obtain both and ? coefficients used in the damage integration, the points of the SN curve of the material (expressed using Bastenaire model) are placed in the wedging space (Figure 1). A linear regression of all those points or of part of them leads in practice to the determination of and ?. Proposition of New Damage Law

Chaboche law was mainly applied, often successfully, to sequences containing two loading blocks commonly known as sequences High-Low or Low-High depending on the relative intensity of successive levels of stress [1]. The disadvantage of the law vis-à-vis its wedging makes the law not useful on its state. Depending on the wedging window chosen, the calculated lifetimes vary very importantly. The failure of the formalism of Chaboche law is in reality due to the fact that the SN curve of the material within the meaning of the law is a straight line in the wedging reference, which does not correspond to the usual SN curves of materials (Bastenaire model used here, but also those of Wöhler, Basquin or Stromeyer [4].

In other words, the problem of the sensitivity of the law vis-à-vis the wedging window used is the fact that the actual SN curve of the material does not match the one stipulated by the law, namely a straight line in the wedging space. Based on this observation, the main goal of the work done is to modify the formalism of the law to find the actual SN curve of the material when is realized the cumulative damage under constant amplitude loading.

The proposed model uses here also stress as mechanical state parameter, and it ties the increase ?D of damage 110 D to the number ?N of cycles that generated it under the following differential form: ??10) The variables used in 111 this law are similar to those used in Chaboche model. The only new variable, denoted ??, represents the Y axis 112 at origin of Goodman diagram passing through the point representative of the cycle analyzed. This variable is 113 given by the expression: ?? = ?a ? b?-1 ?m; the slope b of Goodman line is usually determined from the fatigue 114 limits in symmetrical alternated traction and in repeated traction (?-1 and ?0 respectively). The integration 115 results in the SN curve modeled by Bastenaire expression :(11) ?N c B D ?) m (? oo ? e D ?) m (? oo ? .) m 116 117 118 ??? 119

B and C are the Bastenaire model parameters calculated by smoothing experimental points used in the determination of the SN curve of the material.

122 V.

Comparison of the New Proposed Law with the Chaboche Law Wedged on Several Different Windows and theMilner Law

Life Forecasts are made for steel 20MV6 subject to a sequence of variable amplitude loading CARLOS LATERAL used as reference in the automotive industry.

127 The wedging of the new law on the Bastenaire SN curve of the material lead to outstanding forecasts, especially

128 for significant levels of stress, to those obtained by the law of Chaboche. Forecasts obtained from Miner linear

law is also shown (Figure 2). The proposed new model provides intermediate life forecasts between those of Miner

130 law and those of Chaboche law in the field of limited endurance.

¹³¹ 9 Conclusion

132 A new formalism of non-linear damage law by fatigue has been proposed. It is an alternative to the law of

133 Chaboche because it eliminates the problem of wedging, that Chaboche law faces, on the material data that

- makes the S-N curve. The new law gives lifetime forecasts coincident with the SN curve of material in uniaxial fatigue under constant amplitude; it keeps the essential characteristics of the Chaboche law: sequence effect, the
- influence of the mean stress and non-linear accumulation of damage. ¹



Figure 1:

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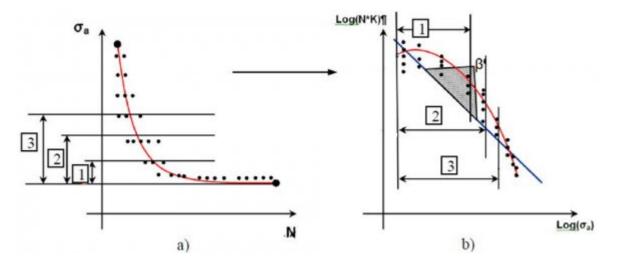


Figure 2:

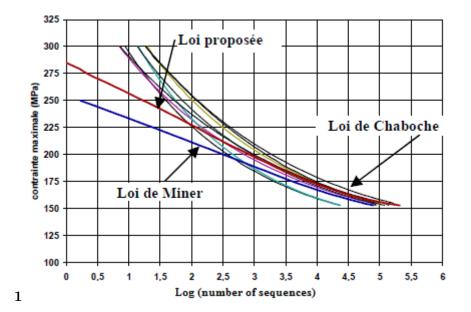


Figure 3: Figure 1 :

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