

New Nonlinear Damage Law by Fatigue based on the Curve of Bastenaire

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Abstract

This article focuses on the improvement of the nonlinear damage law by fatigue of Chaboche. It is a solution to the dependency problem of parameters of the law vis-à-vis the SN curve of the material used for their production. The determination of the parameters, or wedging of the law, has the drawback of smoothing by linear regression the points of SN curve in a particular space specific to the law, called wedging space. So doing, the law is based on the regression line points, different from the actual SN curve of the material. The evolution of fatigue damage and hence the lifetime are then modified. The main idea is to develop a new damage law model, such as the SN curve generated by this formalism is identical to the one used to describe the fatigue behavior of the material under constant amplitude. In the present case, it's obviously the SN curve of Bastenaire model.

Index terms— uniaxial fatigue; damage law; lifetime; wedging; bastenaire.

1 Introduction

The existence in the literature of a large number of damage laws by fatigue for predicting lifetime of structures subjected to varying loads in service illustrates the difficulties of actually having a universal law to forecast lifetime [2]. Although the phenomenon of failure by fatigue of mechanical components subjected to cyclic mechanical strain was discovered more than a century by Wöhler, this type of damage remain still an outstanding event in terms of reliability. However, much progress has been made both in terms of its phenomenological characterization as of understanding of its mechanisms.

Among the proposed damage laws since several decades, the law of Chaboche has always seemed promising although its practical application raises some issues. The attractive aspects of this law are multiple: nonlinear evolution and accumulation of damage, influence of "small" cycles (cycles below the endurance limit) as soon as the damage is initiated, sequence effect (influence of the appearance order of cycles) and the effect of mean stress [3]. The implementation of Chaboche law faces an important challenge from the material parameters determination point of view. It requires the knowledge of the SN curve of the material which undergoes a linear regression in a reference particular and own to the law. Doing so, it significantly changes the SN curve and therefore deviates from the actual behavior of the material. This work is aimed toward the study and the resolution of this disadvantage. First are presented the issues of wedging of the Chaboche law and its impact on the estimated lifetime. An alternative is then proposed by modifying the formalism of the law in order to clear its sensitivity to the wedging field.

2 II.

3 Presentation of the Chaboche Law

The implementation of the law of Chaboche is presented here; it helps to highlight the issue faced during its wedging.

The disadvantage of the law vis-à-vis its wedging makes the law not useful on its state. Depending on the wedging window chosen, the calculated lifetimes vary very importantly. The failure of the formalism of Chaboche law is in reality due to the fact that the SN curve of the material within the meaning of the law is a straight line in the wedging reference, which does not correspond to the usual SN curves of materials (Bastenaire model used here, but also those of Wöhler, Basquin or Stromeyer [4]).

In other words, the problem of the sensitivity of the law vis-à-vis the wedging window used is the fact that the actual SN curve of the material does not match the one stipulated by the law, namely a straight line in the wedging space. Based on this observation, the main goal of the work done is to modify the formalism of the law to find the actual SN curve of the material when is realized the cumulative damage under constant amplitude loading.

The proposed model uses here also stress as mechanical state parameter, and it ties the increase ΔD of damage D to the number N of cycles that generated it under the following differential form:

$$\frac{dD}{dN} = \left(\frac{\sigma_a - \sigma_b}{\sigma_f} \right)^m$$

The variables used in this law are similar to those used in Chaboche model. The only new variable, denoted σ_a, represents the Y axis at origin of Goodman diagram passing through the point representative of the cycle analyzed. This variable is given by the expression:

$$\sigma_a = \sqrt{\sigma_m^2 + b^{-1}}; \text{the slope } b \text{ of Goodman line is usually determined from the fatigue limits in symmetrical alternated traction and in repeated traction (-1 and } \rho_0 \text{ respectively).}$$

The integration results in the SN curve modeled by Bastenaire expression :

$$S_N = C_B D^{C_D} m (\log e) m (\log .)$$

(Aσ_a/σ_f)^mR(D)(1+x)⁻¹D(m-1)ΔD^{m-1}N^{C_B}(log e)^m(log l)/(a f j N^{C_D})

B and C are the Bastenaire model parameters calculated by smoothing experimental points used in the determination of the SN curve of the material.

V.

Comparison of the New Proposed Law with the Chaboche Law Wedged on Several Different Windows and the Milner Law

Life Forecasts are made for steel 20MV6 subject to a sequence of variable amplitude loading CARLOS LATERAL used as reference in the automotive industry.

The wedging of the new law on the Bastenaire SN curve of the material lead to outstanding forecasts, especially for significant levels of stress, to those obtained by the law of Chaboche. Forecasts obtained from Miner linear law is also shown (Figure 2). The proposed new model provides intermediate life forecasts between those of Miner law and those of Chaboche law in the field of limited endurance.

9 Conclusion

A new formalism of non-linear damage law by fatigue has been proposed. It is an alternative to the law of Chaboche because it eliminates the problem of wedging, that Chaboche law faces, on the material data that makes the S-N curve. The new law gives lifetime forecasts coincident with the SN curve of material in uniaxial fatigue under constant amplitude; it keeps the essential characteristics of the Chaboche law: sequence effect, the influence of the mean stress and non-linear accumulation of damage. ¹



Figure 1:

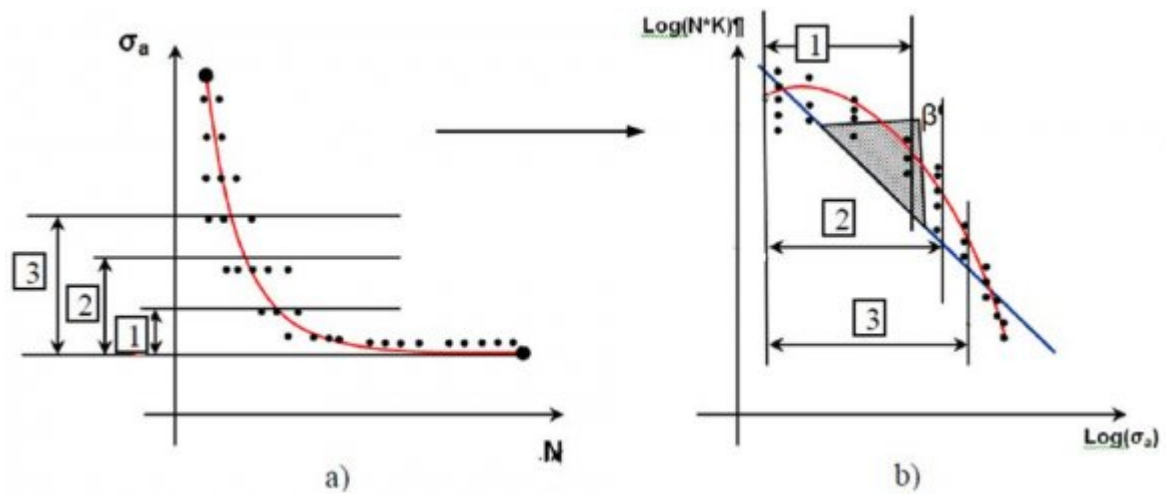
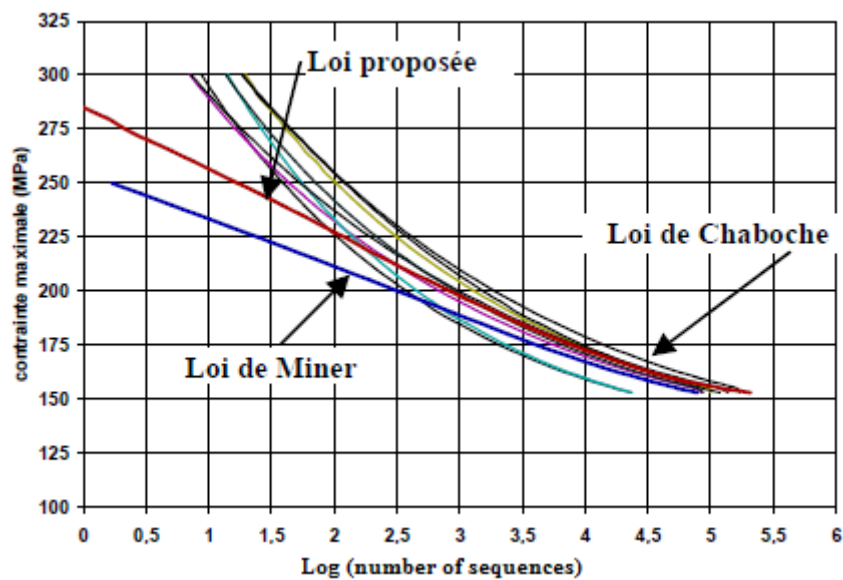


Figure 2:



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Figure 3: Figure 1 :

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